## CHAPTER-6 SEQUENCE AND SERIES-ARITHMETIC AND GEOMETRIC PROGRESSIONS



SEQUENCE

ARITHMETIC PROGRESSION

An ordered collection of numbers $a_{1}, a_{2}, a_{3}, a_{4}$ $\qquad$
$a_{n}$ is a sequenceifaccordingtosomedefiniteruleorlaw,thereisadefinitevalueofan ,called the term or element of the sequence, corresponding to any value of the natural number $n$

An expression of the form $\mathrm{a}_{1}+\mathrm{a}_{2}+\mathrm{a}_{3}+\ldots . . .+\mathrm{a}_{\mathrm{n}}+$ which is the sum of the elements of the sequence $\left\{a_{n}\right\}$ is called a series. If the series contains a finite number of elements, it is called a finite series, otherwise called an infinite series.

A sequence $\mathrm{a}_{1}, \mathrm{a}_{2}, \mathrm{a}_{3}, \ldots . . ., \mathrm{a}_{\mathrm{n}}$ is called an Arithmetic Progression (A.P.) when $\mathbf{a}_{\mathbf{2}}-\mathbf{a}_{\mathbf{1}}=\mathbf{a}_{\mathbf{3}}-\mathbf{a}_{\mathbf{2}}=\ldots . . .=\mathbf{a}_{\mathbf{n}}-\mathbf{a}_{\mathbf{n}-\mathbf{1}}$. That means A. P. is a sequence in which each term is obtained by adding a constant $d$ to the preceding term. This constant ' d ' is called the common difference of the
A.P. If 3 numbers $a, b, c$ are in A.P., wesay $b-a=c-b$ or $a+c=2 b ; b$ is called the arithmetic mean between a and $c$.
$\mathbf{n}^{\text {th }}$ term $\left(\mathbf{t}_{\mathbf{n}}\right)=\mathbf{a}+(\mathbf{n - 1})$
Where $\mathrm{a}=$ First Term
$D=$ Common difference $=t_{n}-t_{n-1}$
Sum of 1st n natural or counting numbers

| Sum of $\boldsymbol{n}$ terms of AP | $s=\frac{n}{2}[2 a+(n-1) d]$ |
| :---: | :---: |
| Sum of the first $n$ terms | Sum of 1 st n natural or counting numbers $S=n(n+1) / 2$ |
| Sum of 1st n odd number | $\mathrm{S}=\mathrm{n}^{2}$ |
| Sum of the Squares of the first, n natural numbers | $n(\underline{n}+1)(2 n+1)$ |

If in a sequence of terms each term is constant multiple of the proceeding term, then the sequence is called a Geometric Progression (G.P). The constant multiplier is called the common ratio.

> GEOMETRIC PROGRESSION (G.P)

GEOMETRIC MEAN
$\frac{\text { Anyterm }}{\text { Precedingterm }}=\frac{t_{n}}{t_{n-1}}$

$$
=a r^{n-1} / a r^{n-2}=r
$$

| Sum of first n terms <br> of a GP | $\mathbf{S}_{\mathbf{n}}=\mathbf{a}\left(\mathbf{1}-\mathbf{r}^{\mathbf{n}}\right) /(\mathbf{1}-\mathbf{r})$ when $\mathbf{r}<\mathbf{1}$ <br> $\mathbf{S}_{\mathbf{n}}=\mathbf{a}\left(\mathbf{r}^{\mathbf{n}} \mathbf{- 1}\right) /(\mathbf{r}-\mathbf{1})$ when $\mathbf{r}>\mathbf{1}$ |
| :--- | :---: |
| Sum of infinite <br> geometric series | $\mathbf{S} \boldsymbol{\infty}=\mathbf{a} /(\mathbf{1}-\mathbf{r})$ where $\mathbf{0}<\mathbf{r}<\mathbf{1}$ |

## A.M. of $\mathrm{a} \& \mathrm{~b}$ is $=(\mathrm{a}+\mathrm{b}) / 2$

If $a, b, c$ are in G.P we get $b / a=c / b=>b^{2}=a c, b$ is called the geometric mean between $a$ and $c$

Questions

Question: 1
Find the $7^{\text {th }}$ term of the A.P. $8,5,2,-1,-4, \ldots$
(a) 10
(b) -10
(c) 8
(d) -8

Answer: b
Explanation:
Here $a=8, d=5-8=-3$
Now $\mathrm{t}_{7}=8+(7-1) \mathrm{d}$
$=8+(7-1)(-3)$
$=8+6(-3)$
$=8-18$
$=-10$

## Question: 2

If $5^{\text {th }}$ and $12^{\text {th }}$ terms of an A.P. are 14 and 35 respectively, find the A.P.
(a) $2,5,8,11,14$,
(b) $2,3,8,11,12$,
(c) $2,3,4,11,14$...
(d) $2,5,8,1,4$,

Answer: a

## Explanation:

Let a be the first term \& d be the common difference of A.P.
$t_{5}=\mathrm{a}+4 \mathrm{~d}=14$
$t_{12}=\mathrm{a}+11 \mathrm{~d}=35$
On solving the above two equations
$7 \mathrm{~d}=21=$ i.e. $\mathrm{d}=3$
And $\mathrm{a}=14-(4 \times 3)=14-12=2$
Hence, the required A.P. is $2,5,8,11,14$, $\qquad$

## Question: 3

Divide 69 into three parts are in A.P. and are such that the product of the first two parts is 483 .
(a) $21,23,25$.
(b) 21, 22, 23,
(c) $22,23,25$.
(d) $21,22,25$.

## Answer: a

## Explanation:

Given that three parts are in A.P., let the three parts which are in A.P. be $a-d, a, a+d . . . .$.
Thus $a-d+a+a+d=69$
Or $3 \mathrm{a}=69$
Or $\quad a=23$
So the three parts are $23-\mathrm{d}, 23,23+\mathrm{d}$
Since the product of first two parts is 483 , therefore, we have $23(23-d)=483$
Or $23-\mathrm{d}=\frac{483}{23}=21$
Or $d=23-21=2$
Hence, the three parts which are in A.P. are $23-2=21,23,23+2=25$
Hence the three parts are 21, 23, and 25
Question: 4
Find the arithmetic mean between 4 and 10 .
(a) 5
(b) 7
(c) 10
(d) 3

Answer: b

## Explanation:

We know that the A.M. of $\mathrm{a} \& \mathrm{~b}$ is $=(\mathrm{a}+\mathrm{b}) / 2$
Hence, The A.M. between $4 \& 10=(4+10) / 2=7$

## Question: 5

Find the G.P. series where $4^{\text {th }}$ term is 8 and $8^{\text {th }}$ term is $128 / 625$
(a) $125,50,20,9$,
(b) $125,50,20,10, \ldots .$.
(c) $125,5,20,8 \ldots$
(d) $125,50,20,8 \ldots$

Answer: d
Explanation:
$\mathrm{t} 4=\mathrm{ar}^{3}=8$
$\mathrm{T} 8=128 / 625 \rightarrow \mathrm{ar}^{\wedge} 7=128 / 625$
T8/T4 $=128 / 625 \times 1 / 8$
$\rightarrow \mathrm{ar}^{\wedge} 7 / \mathrm{ar}^{3}=16 / 625$
$\rightarrow \mathrm{r}^{\wedge} 4=2^{\wedge} 4 / 5^{\wedge} 4$
$\Rightarrow r=2 / 5$

$$
\begin{aligned}
\mathrm{ar}^{3} & =8 \\
& \rightarrow \mathrm{a}(2 / 5)^{3}=8 \\
& \rightarrow \mathrm{a} \times 8 / 125=8 \\
& \rightarrow \mathrm{a}=125
\end{aligned}
$$

Therefore, $\mathrm{a}=125$, $\mathrm{ar}=125 \times 2 / 5=50, \mathrm{ar}^{2}=125 \times 4 / 125=20 \ldots$. Or $125,50,20,8$... Forms a G.P.

## Question: 6

Insert three geometric means between $\frac{1}{9}$ and 9
(a) $\frac{1}{9}, \frac{1}{3}, 1,3,9$
(b) $\frac{1}{8}, \frac{1}{5}, 1,3,9$
(c) $\frac{11}{9}, \frac{1}{3}, 1,3,9$
(d) $\frac{121}{9}, \frac{1}{3}, 1,3$

## Answer: a

Explanation:
G.P. Series $\frac{1}{9},--,--,--,--, 9$

Here t1 $=\mathrm{a}=\frac{1}{9}$
$\mathrm{t} 5=\mathrm{a} . \mathrm{r}^{4}=9$
Now, $\mathrm{t} 5=\frac{1}{9} \cdot \mathrm{r}^{4}=9$
= $\mathrm{r}^{4}=81$
$=r^{4}=3^{4}$
= $\mathrm{r}=3$
$\mathrm{t} 2=\mathrm{ar}=\frac{1}{9} \times 3=\frac{1}{3}$
$\mathrm{t} 3=\mathrm{ar}^{2}=\frac{1}{9} \times 3^{2}=1$
$t 4=\operatorname{ar} 3=\frac{1}{9} \times 3^{3}=3$
Thus the series $\frac{1}{9}, \frac{1}{3}, 1,3,9$

## Question: 7

Find the sum of $1^{\text {st }}$ term of G.P. series $1+2+4+8+\ldots .$.
(a) 155
(b) 255
(c) 185
(d) -822

Answer: b
Explanation:
Here $\mathrm{a}=1, \mathrm{r}=2, \mathrm{n}=8$
$\mathrm{S}_{\mathrm{n}}=\mathrm{a} \cdot \frac{\left(\frac{\left.r^{n}-1\right)}{(r-1)} \text { When } \mathrm{r}>1\right.}{}$
$S_{8}=1$. $\frac{\left(2^{8}-1\right)}{(2-1)}$
$=1(256-1)=255$
Thus $\mathrm{S}_{8}=255$

## Question: 8

Find the sum of the series $-2,6,-18$..... 7 terms?
(a) 1554
(b) -1094
(c) 1094
(d) -8223

Answer: b
Explanation:
Here $\mathrm{a}=-2, \mathrm{r}=-3, \mathrm{n}=7$
$\mathrm{S}_{\mathrm{n}}=\mathrm{a} \cdot \frac{\left(1-r^{n}\right)}{(1-r)}$ When $<1$
$S_{7}=(-2) \frac{\left[1-(-3)^{7}\right]}{[1-(-3)]}$
$=(-2) \frac{(1+2187)}{4}$
$=(-2) \frac{(2188)}{4}$
$S_{7}=-1094$
Question: 9
In a G.P. the product of the $1^{\text {st }}$ three terms $27 / 8$. The middle term is
(a) $\frac{27}{8}$
(b) $\frac{3}{2}$
(c) $\frac{2}{9}$
(d) $\frac{8}{27}$

Answer: b
Explanation:
Let the three terms Of GP are $\frac{\text { a }}{\frac{a}{r}}$ a, ar
Now product of terms
$\frac{\mathrm{a}}{\mathrm{r}} \times \mathrm{a} \times \mathrm{ar}=\frac{27}{8}$
$\mathrm{a}^{3}=\frac{27}{8}$
$\mathrm{a}^{3}=\left(\frac{3}{2}\right)^{3}$
$\mathrm{a}=\frac{3}{2}$
Thus the middle term, $a=\frac{3}{2}$
Question: 10
If you save 1 paisa today, 2 paisa the next day and 4 paisa the succeeding day and so on, then your total savings in two weeks will be.
(a) Rs. 168.32
(b) Rs. 163.98
(c) Rs. 163.83
(d) None

Answer: c
Explanation:
Here the pattern of savings the G.P series $0.01,0.02,0.04 \ldots$
Here $\mathrm{a}=0.01, \mathrm{r}=2, \mathrm{n}=14$
$\mathrm{S}_{\mathrm{n}}=\mathrm{a} \cdot \frac{\left(r^{n}-1\right)}{(r-1)}$ When $\mathrm{r}>1$
$S_{14}=0.01 \frac{\left(2^{14}-1\right)}{(2-1)}$
$=0.01 \frac{(16384-1)}{1}$
$=0.01 \times 16383$
$\mathrm{S}_{14}=163.83$
Thus the total savings in 14 days would be Rs. 163.83.

## Question: 11

The sum of the infinite G.P series $1-\frac{1}{3}+\frac{1}{9}-\frac{1}{27} \ldots .$.
(a) 0.75
(b) 75
(c) 0.57
(d) 57

Answer: a
Explanation:
Here $a=1, r=\left(\frac{-1}{3}\right)$
$\mathrm{S}_{\infty}=\frac{a}{(1-r)}=\frac{1}{\left[1-\left(\frac{-1}{3}\right)\right]}$
$=$
= $1 /[4 / 3]$
$=3 / 4$
$=0.75$
Question: 12
Find the $10^{\text {th }}$ term of the A.P.: $2,4,6, \ldots$.
(a) 20
(b) 40
(c) 2
(d) 0.20

Answer: a
Explanation:
Here the first term (a) = 2 and common different d=4-2=2
Using the formula $t_{n}=a+(n-1) d$, we have
$t_{10}=2+(10-1) 2=2+18=20$
Hence, the $10^{\text {th }}$ term of the given A.P. is 20

## Question: 13

The $10^{\text {th }}$ term of an A.P. is -15 and $31^{\text {st }}$ term is -57 , find the $15^{\text {th }}$ term
(a) -20
(b) 20
(c) -25
(d) 25

Answer: c
Explanation:
Let a be the first term and d be the common $d$ be the common difference of the A.P. Then from the formula:
$t_{n}=a+(n-1) d$, we have
$\mathrm{t}_{10}=\mathrm{a}+(10-1) \mathrm{d}=\mathrm{a}+9 \mathrm{~d}$
$\mathrm{t}_{31}=\mathrm{a}+(31-1) \mathrm{d}=\mathrm{a}+30 \mathrm{~d}$
We have,
$\mathrm{a}+9 \mathrm{~d}=-15$
$a+30 d=-57$
Solve equations (1) and (2) to get the values of a and d. Subtracting (1) from (2), we have $21 \mathrm{~d}=-57+15=-42$
$-42 \div 21=2$
Again from (1), $a=-15-9 d=-15-9(-2)=-15+18=3$
Now $\mathrm{t}_{15}=\mathrm{a}+(15-1) \mathrm{d}$
$=3+14(-2)=-25$
Question: 14
Which term of the A.P.: $5,11,17$... is $119 ?$
(a) $\mathrm{n}=20$
(b) $\mathrm{n}=2$
(c) $\mathrm{n}=30$
(d) $n=19$

Answer: a
Explanation:
Here $\mathrm{a}=5, \mathrm{~d}=11-5=6$
$t_{n}=119$ we know that
$\mathrm{t}_{\mathrm{n}}=\mathrm{a}+(\mathrm{n}-1) \mathrm{d}$
? $119=5+(\mathrm{n}-1) \times 6$
$(\mathrm{n}-1)=\frac{119-5}{6}=19$
$n=20$, therefore, 119 is the $20^{\text {th }}$ term of the given A.P.

## Question: 15

Is 600 a term of the A. P.: $\mathbf{2 , 9 , 1 6 , \ldots . . \text { ? }}$
(a) yes
(b) no
(c) not sure
(d) none

Answer: b
Explanation:
Here, $\mathrm{a}=2$, and $\mathrm{d}=9-2=7$.
Let 600 be the $n^{\text {th }}$ term of the A.P. We have $t_{n}=2+(n-1) 7$
According to the question
$2+(\mathrm{n}-1) 7=600$
$(\mathrm{n}-1) 7=598$
Or $\mathrm{n}=\frac{598}{7}+1$

$$
\mathrm{n}=86 \frac{3}{7}
$$

Since $n$ is a fraction, it cannot be a term of the given A.P. Hence, 600 is not a term of the given A.P.

## Question: 16

The common difference of an A.P. is 3 and the $15^{\text {th }}$ term is 37 . Find the first term.
(a) -5
(b) 5
(c) 42
(d) -42

## Answer: a

## Explanation:

Here $\mathrm{d}=3, \mathrm{t}_{15}=37$, and $\mathrm{n}=15$ Let the first term be a. we have

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\(\mathrm{t}_{\mathrm{n}}=\mathrm{a}+(\mathrm{n}-1) \mathrm{d}\)
\(37=a+(15-1) 3\)
Or, \(\quad 37=a+42\)
    \(a=-5\)
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Thus, first term of the given A.P. is -5
Question: 17
Geometric mean $G$ between two numbers $a$ and $b$ id
(a) ab
(b) $\mathrm{ab}^{2}$
(c) $a^{2} b$
(d) $\sqrt{a b}$

Answer: d

## Explanation:

If a single geometric mean ' $G$ ' is inserted between two given numbers ' $a$ ' and ' $b$ ', then $G$ is known as the geometric mean between ' $a$ ' and ' $b$ '.
G.M. $=\mathrm{G}=\mathrm{G}^{2}=\sqrt{a b}$

Question: 18
If $A$ and $G$ are arithmetic and geometric mean respectively between two positive numbers $a$ and $b$, then $A(A M)<G(G M)$ is correct?
(a) yes
(b) no
(c) not sure
(d) none

Answer: b
Explanation:
We have
A.M. $=\mathrm{A}=\frac{a+b}{2}$ and G.M. $=\mathrm{G}=\mathrm{G}^{2}=\sqrt{a b}$
$\mathrm{A}-\mathrm{G}=\frac{a+b}{2}-\sqrt{a b}$
$=\frac{a+b-2 \sqrt{a b}}{2}$
$=(\sqrt{\mathrm{a}}-\sqrt{\mathrm{b}})^{2}$
Root will be open automatically
$\mathrm{A}-\mathrm{G}>0$
$\rightarrow \mathrm{A}>\mathrm{G}$

## Question: 19

Find the sum of the AP: 11, 17, 23, and 29... of first 10 terms.
(a) 380
(b) 568
(c) 960
(d) 593

Answer: a
Explanation:
$=>$ nth term for the given $\mathrm{AP}=5+6 \mathrm{n}$
=> First term = 5+ 6 = 11
=> Tenth term $=5+60=65$
=> Sum of 10 terms of the AP $=0.5 \mathrm{n}$ (first term + last term) $=0.5 \times 10(11+65)$
=> Sum of 10 terms of the $\mathrm{AP}=5 \times 76=380$
Question: 20
Find the G. M. between $\frac{3}{2}$ and $\frac{27}{2}$
(a) $\frac{9}{2}$
(b) $\frac{2}{9}$
(c) $\frac{6}{3}$
(d) $\frac{3}{6}$

Answer: a

## Explanation:

We know that if a is the G. M. between a and b, then
$\mathrm{G}=\sqrt{\mathrm{ab}}$
G. M. between $\frac{3}{2}$ and $\frac{27}{2}=\sqrt{\frac{3}{2} \times \frac{27}{2}}$
$=\frac{9}{2}$

## Question: 21

Insert three geometric means between 1 and 256.
(a) $4,16,64$,
(b) $-4,16,-64$
(c) Both
(d) None

Answer: c
Explanation:
Let $\mathrm{G}_{1}, \mathrm{G}_{2}, \mathrm{G}_{3}$, be 3
GMS both 1, \& 256
Then,
1, $\mathrm{G}_{1}, \mathrm{G}_{2}, \mathrm{G}_{3}, 256$ will be in GP
Let common ratio be r
$\therefore \mathrm{G}_{1}=\mathrm{r}$
So $r^{4}=256$
$r= \pm 4$
$\mathrm{G}_{1}= \pm 4$
$\mathrm{G}_{2}= \pm 16$
$\mathrm{G}_{3}= \pm 64$
Question: 22
If 4, 36, 324 are in G.P. insert two more numbers in this progression so that it again forms a G.P.
(a) 12, 108
(b) 14, 180
(c) 16,120
(d) 12,10

Answer: a
Explanation:
G. M. between 4 and $36=\sqrt{4 \times 36}=\sqrt{144}=12$
G.M. between 36 and $324=\sqrt{36 \times 324}=6 \times 18=108$

If we introduce 12 between 4 and 36 and 108 between 36 and 324 , the numbers $4,12,36,108,324$ form a G.P.
The two new numbers inserted are 12 and 108.
Question: 23
The distance travelled (in cm ) by a simple pendulum in consecutive seconds are 16, 12, 9,.... How much distance will it travel before coming to rest?
(a) 64 cm
(b) 46 cm
(c) 1 am
(d) none

Answer: a

## Explanation:

The distance travelled by the pendulum in consecutive seconds are, $16,12,9 \ldots$ is an infinite geometric progression with the first term a $=16$ and $r=\frac{12}{16}=\frac{3}{4}<1$
Hence, using the formula $S=\frac{a}{1-r}$ we have
$\mathrm{S}=\frac{16}{1-\frac{3}{4}}=\frac{16}{\frac{1}{4}}=64$
Distance travelled by the pendulum is 64 cm .
Question: 24
Which term of the G.P.: $5,-10,20,-40, \ldots$ is 320 ?
(a) 7
(b) 6
(c) 3
(d) 12

Answer: a
Explanation:
In this case, $a=5 ; r=\frac{-10}{5}=-2$
Suppose that 320 is the $n^{\text {th }}$ term of the G. P.
By the formulate $=a^{\mathrm{n}-1}$, we get
$\mathrm{t}=5$. $(-2)^{\mathrm{n}-1}$, we get
$320=5 .(-2)^{n-1}=64=(2)^{6}=(-2)^{n-1}$
$\mathrm{n}-1=6$
$\mathrm{n}=7$
Hence 320 is the $7^{\text {th }}$ term of the G.P.

## Question: 25

If $\mathbf{a}, \mathbf{b}, \mathbf{c}$ is in G.P., then
(a) $a\left(b^{2}+a^{2}\right)=c\left(b^{2}+c^{2}\right)$
(b) $a\left(b^{2}+a^{2}\right)=c\left(a^{2}+b^{2}\right)$
(c) $b\left(b^{2}+a^{2}\right)=c\left(b^{2}+c^{2}\right)$
(d) None

Answer: b
Explanation:
If $\mathrm{a}, \mathrm{b}, \mathrm{c}$ is in to G.P. Then $\mathrm{b}^{2}=\mathrm{ac}$
$b^{2}(a-c)=a c(a-c)$
$b^{2} a-a c^{2}=a^{2} c-b^{2} c$
$a\left(b^{2}+c^{2}\right)=c\left(a^{2}+b^{2}\right)$
Trick: Put $\mathrm{a}=1, \mathrm{~b}=2, \mathrm{c}=4$, and check the alternates.

## Question: 26

The sum of infinity of the progression $9-3+1-\frac{1}{3}+\ldots$ is
(a) 9
(b) $9 / 2$
(c) $27 / 4$
(d) $15 / 2$

Answer: c

## Explanation:

Infinite series $9-3+1-\frac{1}{3} \ldots \ldots . . \propto$ is a G. P. with
$\mathrm{a}=9, \mathrm{r}=\frac{-1}{3} \backslash S_{\alpha}=\frac{a}{1-r}=\frac{9}{1+\frac{1}{3}}=\frac{9 \times 3}{4}=\frac{27}{4}$
Question: 27
The product (32) (32) ${ }^{1 / 6}(32)^{1 / 36}$.....To $\infty$ is.
(a) 16
(b) 32
(c) 64
(d) 0

Answer: c
Explanation:
(32) (32) $1 / 6$ (32) $1 / 36 \ldots \ldots \infty=(32)^{1+\frac{1}{6}+\frac{1}{36}+\cdots \infty}=(32)^{\left(1-\frac{1}{6}\right)}$
$(32)^{\frac{1}{5 / 6}}=(35)^{6 / 5}=2^{6}=64$
Question: 28
Obtain the sum of all positive integers up to 1000, which are divisible by 5 and not divisible by 2 .
(a) 10050
(b) 5050
(c) 5000
(d) 50000

Answer: d
Explanation:
The positive integers, which are divisible by 5, are 5, 10, 15... 1000
Out of these 10, 20, 30,.. 1000 are divisible by 2
Thus, we have to find the sum of the positive integers $5,15,25 \ldots 995$
If $n$ is the number of terms in it the sequence then
$995=5+10(n-1)$
=> $1000=10 \mathrm{n}$
Therefore, $\mathrm{n}=100$
Thus the sum of the series $=(100 / 2)(5+995)=(50)(1000)=50000$.
Question: 29
If $s$ is the sum of an infinite G.P., the first term a then the common ratio r given by
(a) $\frac{a-s}{s}$
(b) $\frac{s-a}{s}$
(c) $\frac{a}{1-s}$
(d) none

Answer: b
Explanation:
$\mathrm{S}=\frac{a}{1-r}$
$\mathrm{s}-\mathrm{sr}=\mathrm{a}$
$-s r=a-s$
$\mathrm{r}=\frac{s-a}{s}$
Question: 30
If in an infinite G.P. first term is equal to the twice of the sum of the remaining terms, then its common ratio is
(a) 1
(b) 2
(c) $1 / 3$
(d) $-1 / 3$

Answer: c
Explanation:
Given, $\mathrm{a}=2\left(\frac{a r}{1-r}\right)$
$1-\mathrm{r}=2 \mathrm{r}$
$r=\frac{1}{3}$
Question: 31

If $n$ geometric means between $a$ and $b$ be $G_{1}, G_{2}, \ldots . G_{n}$ and a geometric mean be $G$, then the true relation is
(a) $\mathrm{G}_{1}, \mathrm{G}_{2}$, $\mathrm{Gn}=\mathrm{G}$
(b) $\mathrm{G}_{1}, \mathrm{G}_{2}, \ldots . . . \mathrm{G}_{\mathrm{n}}=\mathrm{G}^{1 / n}$
(c) $\mathrm{G}_{1}, \mathrm{G}_{2}$, $. \mathrm{G}_{\mathrm{n}}=\mathrm{G}^{\mathrm{n}}$
(d) none

Answer: c
Explanation:
Here G = (a b) ${ }^{1 / 2}$ and
$\mathrm{G}_{1}=\operatorname{ar}^{1}, \mathrm{G}_{2}=\mathrm{ar}^{2}, \ldots \mathrm{G}_{\mathrm{n}}=\operatorname{ar}^{\mathrm{n}}$. therefore
$\mathrm{G}_{1} \cdot \mathrm{G}_{2} \cdot \mathrm{G}_{3} \ldots . \mathrm{G}_{\mathrm{n}}=\mathrm{a}^{\mathrm{n}} \mathrm{r}^{1+2+\cdots+\mathrm{n}}=\mathrm{a}^{\mathrm{n}} \mathrm{r}^{\mathrm{n}(\mathrm{n}+1) / 2}$ But
$a^{n+1}=b$
$r=\left(\frac{b}{a}\right)^{\frac{1}{n+1}}$
Therefore, the required product is $\mathrm{a}^{\mathrm{n}}\left(\frac{\mathrm{b}}{\mathrm{a}}\right)^{\frac{1}{(n+1)} \cdot n(\mathrm{n}+1) / 2}$
$=(\mathrm{ab})^{\mathrm{n} / 2}$
$=\left\{(\mathrm{ab})^{1 / 2}\right\}^{\mathrm{n}}$
$=\mathrm{G}^{\mathrm{n}}$
Note: It is a well-known fact.

## Question: 32

7 th term of the sequence $\sqrt{2}, \sqrt{10}, 5 \sqrt{2} \ldots$ is
(a) $125 \sqrt{10}$
(b) $25 \sqrt{2}$
(c) 125
(d) $125 \sqrt{2}$

Answer: D
Explanation:
Given sequence is $\sqrt{2}, \sqrt{10}, 5 \sqrt{2} \ldots .$. Common ratio
$\mathrm{r}=\sqrt{5}$, first term $\mathrm{a}=\sqrt{2}$, then $7^{\text {th }}$ term
$t_{7}=\sqrt{2}(\sqrt{5})^{7-1}=\sqrt{2}(\sqrt{5})^{6}=\sqrt{2}(5)^{3}$
$125 \sqrt{2}$
Question: 33
If the first term of a G.P. be 5 and common ratio be -5 , then which term is 3125 ?
(a) $6^{\text {th }}$
(b) $5^{\text {th }}$
(c) $7^{\text {th }}$
(d) $8^{\text {th }}$

Answer: b
Explanation:
Given that first term $\mathrm{a}=5$ and common ratio $\mathrm{r}=-5$. Suppose that $\mathrm{n}^{\text {th }}$ term is 3125
Then ar $^{n-1}=3125$
$5(-5)^{n-1}=\frac{5^{5}}{5} 5^{4}$
$\mathrm{n}-1=4=(\mathrm{n} \rightarrow 5)$
Question: 34
The sums of $\mathbf{n}$ terms of three A.P.'s whose first term is 1 and common differences are 1 , 2,3 are $S_{1}, S_{2}, S_{3}$ respectively. The true relation is
(a) $S_{1}+S_{2}=S_{3}$
(b) $S_{1}+S_{3}=2 S_{2}$
(c) $\mathrm{S}_{1}+\mathrm{S}_{2}=2 \mathrm{~S}_{3}$
(d) none

Answer: b

## Explanation:

We have $a_{1}=a_{2}=a_{3}=1$

$$
\mathrm{d}_{1}=1, \mathrm{~d}_{2}=2, \mathrm{~d}_{3}=3
$$

Therefore, $\mathrm{S}_{1}=\frac{\mathrm{n}}{2}(\mathrm{n}+1) \ldots . .(\mathrm{i})$

$$
S_{2}=\frac{n}{2}(2 n+1) \ldots \text { (ii) }
$$

$S_{3}=\frac{n}{2}(3 n+1)$
... (iii) Adding (i) and (iii),
$\mathrm{S}_{1}+\mathrm{S}_{3}=\frac{\mathrm{n}}{2}[(\mathrm{n}+1)+(3 \mathrm{n}+1)] \rightarrow \frac{\mathrm{n}}{2}[4 \mathrm{n}+2]$
$=2\left[\frac{\mathrm{n}}{2}(2 \mathrm{n}+1)\right]=2 \mathrm{~S}_{2}$
Hence correct relation $S_{1}+S_{3}=2 S_{2}$
Question: 35
What is the sum of all 3 digit numbers that leave a remainder of ' 2 ' when divided by 3 ?
(a) 897
(b) 164,850
(c) 164,749
(d) 149,700

Answer: b

## Explanation:

The smallest 3 digit number that will leave a remainder of 2 when divided by 3 is 101 .
The next number that will leave a remainder of 2 when divided by 3 is $104,107, \ldots$.
The largest 3 digit number that will leave a remainder of 2 when divided by 3 is 998 .
So, it is an AP with the first term being 101 and the last term being 998 and common difference being 3 .
Sum of an AP $=\frac{\text { First term }+ \text { Last term }}{2} \times$ Number of term
We know that in an A.P., the nth term $\mathrm{a}_{\mathrm{n}}=\mathrm{a}_{1}+(\mathrm{n}-1)^{*} \mathrm{~d}$
In this case, therefore, $998=101+(n-1) * 3$
i.e. $897=(n-1)^{*} 3$

Therefore $\mathrm{n}-1=299$
Or $\mathrm{n}=300$
Sum of the AP will therefore be $\frac{101+998}{2} \times 300=164,850$
Question: 36
What is the sum of the following series? -64, $-66,-68, \ldots . .,-100$
(a) -1458
(b) -1558
(c) -1568
(d) -1664

Answer: b

## Explanation:

The sequence is $-64,-66,-68, \ldots .-100$.
The given set of numbers are in an arithmetic progression
Key data: First term is -64 . The common difference is -2 . The last term is -100
Sum of the first n term is an $\mathrm{AP}=\frac{n}{2}\left[2 \mathrm{a}_{1}+(\mathrm{n}-1) \mathrm{d}\right]$
To compute the sum, we know the first term $a_{1}=-64$ and the common difference $d=-2$
We do not know the number of terms $n$. Let us first compute the number of terms and then find the sum of the terms.
Step to compute number of terms of the sequence
$\mathrm{a}_{\mathrm{n}}=\mathrm{a}_{1}+(\mathrm{n}-1) \mathrm{d}$
$-100=-64+(n-1)(-2)$
Therefore, $\mathrm{n}=19$.
Sum $S_{n}=\frac{19}{2}[2(-64)+(919-1)(-2)]$
$\mathrm{S}_{\mathrm{n}}=\frac{19}{2}[-128-36]$
$\mathrm{S}_{\mathrm{n}}=19 \times(-82)=-1558$
Question: 37
The sum of third and ninth term of an A.P. is 8 . Find the sum of the first 11 terms of the progression.
(a) 44
(b) 22
(c) 19
(d) None of these

Answer: a
Explanation:
The third term $\mathrm{t}_{3}=\mathrm{a}+2 \mathrm{~d}$
The ninth term $\mathrm{t}_{9}=\mathrm{a}+8 \mathrm{~d}$
$t_{3}+t_{9}=2 \mathrm{a}+10 \mathrm{~d}=8$
Sum of first 11 terms of an AP is given by
$S_{11}=\frac{11}{2}[2 a+10 d]$
$S_{11}=\frac{11}{2}[8]=44$
Question: 38
The sum of the three numbers in A.P is 21 and the product of the first and third number of the sequence is 45 . What are the three numbers?
(a) 9, 7 and 5
(b) 3,7 , and 11
(c) Both A \& B
(d) None of these

Answer: a
Explanation:
Let the number are be $a-d, a, a+d$
Then $\mathrm{a}-\mathrm{d}+\mathrm{a}+\mathrm{a}+\mathrm{d}=21$
$3 \mathrm{a}=21$
a=7
and $(a-d)(a+d)=45$
$\mathrm{a}^{2}-\mathrm{d}^{2}=45$
$\mathrm{d}^{2}=4$
$\mathrm{d}= \pm 2$
Hence, the number are 5,7 and 9 when $d=2$ and 9,7 and 5 when $d=-2$. In both the cases numbers are the same.

Question: 39
If the first term of G.P. is 7 , Its $\mathbf{n}^{\text {th }}$ term is 448 and sum of first $\mathbf{n}$ terms is 889 , then find the fifth term of G. P.
(a) 112
(b) 110
(c) 62
(d) 39

Answer: a
Explanation:
Given $\mathrm{a}=7$ the first term $\mathrm{t}_{\mathrm{n}}=a \mathrm{a}^{\mathrm{n}-1}=7(\mathrm{r})^{\mathrm{n}-1}=448$.
$7 r^{\mathrm{n}}=448 \mathrm{r}$---- (1)

Also $\mathrm{S}_{\mathrm{n}}=\frac{a\left(r^{n}-1\right)}{r-1}=\frac{7\left(r^{n}-1\right)}{r-1}$
$889=\frac{448 r-7}{r-1}$ \{value of $\mathrm{r}^{\mathrm{n}}$ from $\left.(1)\right\}$
R = 2
Hence $\mathrm{T}_{\mathrm{s}}=\operatorname{ar}^{4}=7(2)^{4}=112$

Question: 40
If the third and fourth terms of arithmetic sequence are increased by 3 and 8 respectively. Then the first four terms form a geometric sequence. Find
(i) the sum of the first four terms of A.P.
(a) 54
(b) 27
(c) 23
(d) 79

Answer: a
Explanation:
Sol. $a,(a+d),(a+2 d),(a+3 d)$ in A.P.
$a, a+d,(a+2 d+3),(a+3 d+8)$ are in G.P.
Hence $a+d=a r$
also $\mathrm{r}=\frac{a+d}{a}=\frac{a+2 d+3}{a+d}=\frac{a+3 d+8}{a+2 d+3}$
$\frac{d+3}{d}=\frac{d+5}{d+3}$
$\rightarrow \mathrm{d}^{2}+6 \mathrm{~d}+9=\mathrm{d}^{2}+5 \mathrm{~d} \rightarrow \quad \mathrm{~d}=-9$
$\frac{a-9}{a}=\frac{a-15}{a-9}$
$\rightarrow \mathrm{a}^{2}-18 \mathrm{a}+81=\mathrm{a}^{2}-15 \mathrm{a} \rightarrow 3 \mathrm{a}=8_{1} \rightarrow \mathrm{a}=27$
Hence A.P. is $27,18,9,0$,
Sum of the first four terms of AP $=54$

## Question: 41

Three positive numbers form a G.P. If the second term is increased by 8 , the resulting sequence is an A.P. In turn, if we increase the last term of this A.P. by 64, we get a G.P. Find the three numbers.
(a) $4,12,36$
(b) $4,8,16$
(c) $5,15,20$
(d) none

Answer: a

## Question: 42

The sum of the first five terms of a geometric series is 189 . The sum of the first six terms is $3^{81}$, and the sum of the first seven terms is $7^{6} 5$. What is the common ratio in the series?
(a) 3
(b) 2
(c) 6
(d) 56

Answer: b
Explanation:
Let the numbers be a, ar, a $r^{2}$ when $r>0$
Hence $a$, $(a r+8), a r^{2}$ in A.P. - (1)
Also a, (ar + 8), a $\mathrm{r}^{2}+64$ in G.P. - (2)
$\rightarrow(\mathrm{ar}+8)^{2}=\mathrm{a}\left(\mathrm{ar}^{2}+64\right) \mathrm{a}=4 / 4-\mathrm{r}-(3)$
Also $(1) \rightarrow 2(a r+8)=\left(a+a r^{2}\right) \rightarrow(1-r)^{2}=16 / a-(4)$
From (3) and (4) r $=3$ or -5 (rejected)
Hence $\mathrm{a}=4$ numbers are: $4,12,3^{6}$

Explanation:
$S_{5}=189 ; S_{6}=3^{81 ;} S_{7}=765 ; t_{6}=S_{6}-S_{5}=3^{81}-189=19^{2}$
$\mathrm{t}_{7}=\mathrm{S}_{7}-\mathrm{S}_{6}=765-3^{81}=3^{8} 4$
Now common ratio $=\frac{t_{7}}{t_{6}}=\frac{384}{192}=2$

## Question: 43

Find the $3^{\text {rd }}$ nth term for the AP: 11, 17, 23, 29,.....
(a) 23
(b) 17
(c) 11
(d) 6

Answer: a
Explanation:
Here, $\mathrm{a}=11, \mathrm{~d}=17-11=23-17=29-23=6$
We know that nth term of an AP is a $+(n-1) d$
$=>$ nth term for the given AP $=11+(n-1) 6$
$\Rightarrow>$ nth term for the given $A P=11+(n-1) 6$
$=>n$th term for the given $A P=5+6 n$
We can verify the answer by putting values of ' $n$ '
=> n = a -> First term = $5+6=11$
=> n = 2 -> Second term = $5+12=17$
=> n = 3 -> Third term $=5+18=23$

## Question: 44

The sum of three numbers in a GP is 26 and their product is 216 . And the numbers.
(a) 2, 6 and 18
(b) 3,7 , and 11
(c) Both
(d) None of these

Answer: a
Explanation:
Let the numbers be $\frac{a}{r}$, a ar.
$=>\left(\frac{a}{r}\right)+a+a r=26$
$\Rightarrow>\mathrm{a} \frac{\left(1+r+r^{2}\right)}{r}=26$
Also, it is given that product $=216$
$\Rightarrow\left(\frac{a}{r}\right) \times(\mathrm{a}) \times(\mathrm{ar})=216$
$\Rightarrow a^{3}=216$
$\Rightarrow \mathrm{a}=6$
$=>6 \frac{\left(1+r+r^{2}\right)}{r}=26$
$\Rightarrow>\frac{\left(1+r+r^{2}\right)}{r}==\frac{26}{6}=\frac{13}{3}$
$=>3+3 r+3 r^{2}=13 r$
$\Rightarrow 3 r^{2}-10 r+3=0$
$=>(r-3)\left(r-\left(\frac{1}{3}\right)\right)=0$
$\Rightarrow>=3$ or $r=\frac{1}{3}$
Thus, the required numbers are 2,6 and 18 .

## Question: 45

A Sequence in which the ratio of two consecutive terms is always constant $(1,0)$ is called
(a) AP
(b) GP
(c) HP
(d) NP

Answer: b

## Explanation:

A Sequence in which the ratio of two consecutive terms is always constant $(1,0)$ is called a Geometric progression (G.P.)

## Question:46

For the elements 4 and 6, verify
(a) $\mathrm{A} \geq \mathrm{G} \geq \mathrm{H}$
(b) $\mathrm{A}<\mathrm{G} \geq \mathrm{H}$
(c) A $>\mathrm{G} \geq \mathrm{H}$
(d)None

Answer: a
Explanation:
A $=$ Arithmetic Mean $=(4+6) / 2=5$
$\mathrm{G}=$ Geometric Mean $=\sqrt{4 \times 6}=4.8989$
$H=$ Harmonic Mean $=(2 \times 4 \times 6) /(4+6)=48 / 10=4.8$
Therefore, $\mathrm{A} \geq G \geq \mathrm{H}$
Question: 47
A sequence of numbers is called?
(a) Geometric Progression
(b) Arithmetic progression (AP)
(c) Harmonic Progression
(d) All

Answer: d

## Explanation:

Harmonic Progression (HP)
A sequence of numbers is called a harmonic progression if the reciprocal of the terms are in AP. In simple terms, $a, b, c, d, e, f$ are in HP if $1 / a, 1 / b, 1 / c, 1 / d, 1 / e, 1 / f$ are in AP.
Arithmetic Progression (AP)
A sequence of numbers is called an arithmetic progression if the difference between any two consecutive terms is always same.
Geometric Progression (GP)
A sequence of numbers is called a geometric progression if the ratio of any two consecutive terms is always same.

Question: 48
An AP has 13 terms whose sum is 143 . The third term is 5 , then first term is:
(a) 4
(b) 7
(c) 9
(d) None of these

## Answer: d

Explanation:
$S(13)=143$
S (13) = (n/2)(2a+(n-1)d)
$=(13 / 2) \times(2 a-12 d)$
$=13 \times(a+6 d)$
$=13 \mathrm{a}+78 \mathrm{~d}=143$
Divide both sides by 13
a+6d=11
$T(3)=a+2 d=5$
Subtract (2) from (1)
$4 d=6$
$\mathrm{d}=3 / 2$
Substituted in any of the equations .....(am using 2)
$a+2(3 / 2)=5$
$a+3=5$
$a=2$
Question: 49
The series $1^{3}+2^{3}+3^{3}+\ldots . .20^{3}$ is equal to
a) 4410
b) 4410000
c) 44100
d) None of these

Answer: c
Explanation
( $\mathrm{n}(\mathrm{n}+1) / 2)^{2}$
$(20(20+1) / 2)^{2}$
44100.

## PREPARE FOR WORST

## Question 1

What is the sum of all $\mathbf{3}$ digit numbers that leave a remainder of ' 2 ' when divided by $\mathbf{3}$ ?
(a) 897
(b) 164,850
(c) 164,749
(d) 149,700

## Question 2

A piece of equipment cost a certain factory Rs. 6, 00,000. If it depreciates in value, 15\% the first year, $13.5 \%$ the next year. $12 \%$ the third year, and so on, what will be its value at the end of $\mathbf{1 0}$ years, all percentages applying to the original cost
(a) 2,00,000
(b) $1,05,000$
(c) $4,05,000$
(d) $6,50,000$

## Question 3

If a rubber ball consistently bounces back $2 / 3$ of the height from which it is dropped, what
Fraction of its original height wills the ball bounce after being dropped and bounced four times without being stopped?
(a) $16 / 81$
(b) $16 / 27$
(c) $4 / 9$
(d) $37 / 81$

## Question 4

Find the sum of first 30 positive integer multiple of 6

## Question 5

How many numbers are there between 200 and 800 which are divisible by both?
5 and 7?

## Question 6

If $(p+q)$ th term of an A.P is $m$ and ( $p-q$ )tn term is $n$, then $p$ th
(a) $m n$
(b) $\sqrt{m n}$
(c) $\frac{1}{2}(m-n)$
(d) $\frac{1}{2}(m+n)$

## Question 7

If 7 times the 7 th term of an A.P is equal to 11 times of its 11 th term , then 18 th term is
(a) 18
(b) 9
(c) 77
(d) 0

## Question 8

There is a set of four numbers $p, q, r$ and $s$ respectively in such a manner that first three are in G.P. and the last three are in A.P with a difference of 6 . If the first and the fourth numbers are the same find the value of $P$.
(a) 8
(b) 2
(c) -4
(d) -24

## Question 9

An arithematic progression has 23 terms, the sum of the middle three terms of the arithematic progression is 270, and the sum of the last three terms of this Arithmetic progress is 1320 . What is the $\mathbf{1 8}^{\text {th }}$ term of this arithematic progression?
(a) 240
(b) 360
(c) 340
(d) 440

## Question 10

Find the value of 'a' given that the geometric mean between x and y is
(a) $-2 / 3$
(b) $-1 / 4$
(c) $-3 / 2$
(d) $-7 / 6$

## Question 11

Sum of three numbers in GP with common ratio greater than $\mathbf{1}$ is 105 If the first two numbers are multiplied by 4 and the $3^{\text {rd }}$ number is multiplied by 3 , then the resulting Terms are in AP. What is the highest of the three numbers given?
(a) 60
(b) 50
(c) 30
(d) 45

## Question 12

There are three terms x.y.z between $4 \& 40$ such that (i) their sum is 37 (ii) $4, x, y$ are consecutive terms of an $A, P$ and (iii) $y, z, 40$ are the consecutive terms of a G.P, Find the value of $Z$
(a) 20
(b) 10
(c) 12
(d) 15

## Question 13

A tortoise walks 500 m in one day, the next day it walks 250 m , the next day 125, m and so on, what is the limiting distance which it could walk?

## Question 14

In a geometric progression the sum of first $3 X$ term of the series is $S$ and the sum of first $\mathbf{2 X}$ terms of the series is $12 \mathrm{~s} / 133$. If the sum of first $X$ terms of the series is $s / k$, find the value of ' $k$ ' it is given that the common difference of the $g p$ is positive.
(a) 120
(b) 133
(c) 155
(d) 160

## Question 15

In a infinite geometric progression with common ratios less than 1 the sum of any two consecutive terms is 8 times the sum of all the terms that follow. What is the ratio of any term and the sum of all the terms that follow it?
(a) 2
(b) -2
(c) -4
(d) Cannot be determined

## Question 16

In an arithematic progression, the sum of the first 10 terms is half the sum of first 15 terms. Find the ratio of the sum of first 16 terms and first 21 terms of some AP.
(a) $7: 11$
(b) 6:10
(c) $12: 17$
(d) $8: 13$

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# PAST EXAMINATION QUESTIONS: 

## MAY 2018

## Question 1

The sum to $\mathbf{m}$ terms of the series $1+11+11+1111+\ldots .$. Upto $\mathbf{m}$ terms is equal to:
(a) $\frac{1}{81}\left(10^{m+1}-9 m-10\right)$
(b) ) $\frac{1}{27}\left(10^{m+1}-9 m-10\right)$
(c) ) $\left(10^{m+1}-9 m-10\right)$
(d) None

Answer: a
Explanation:
Given series:
1+11+111+ $\qquad$ m term
$\frac{1}{9}[9+99+999+\ldots . .$. .m term $]$
$\frac{1}{9}(10-1)+(100-1)+(1000-1)+1 \ldots \ldots .+m$ term $]$
$\frac{1}{9}\left[\frac{10 .\left(10^{\mathrm{m}-1}\right)}{10-1}-\mathrm{m}\right]$
$\frac{1}{9}\left[\frac{10^{m-1}-10}{9}-m\right]$
$\frac{1}{9}\left[\frac{10.10^{\mathrm{m}-1}-10-9 \mathrm{~m}}{9}-\mathrm{m}\right]$
$\frac{1}{81}\left(10.10^{m-1}-9 m-10\right)$

## Question 2

A person pays Rs. 975 in monthly installments; each installment is less than former by Rs.5.

## The amount

(a) 26 months
(b) 15 months
(c) both (a) \& (b)
(d) 18 months

Answer: c
Explanation:
$s_{n}=975, \mathrm{a}=100, \mathrm{~d}=-5, \mathrm{n}=$ ?
$s_{n}=\frac{n}{2}(2 a+(n-1) d)$
$975=\frac{n}{2}[2 \times 100+(n-1)(-5)]$
$1950=\mathrm{n}[200-5 \mathrm{n}+5]$
$1950=n[205-5 n]$
$1950=205 n-5 n^{2}$
$5 n^{2}-205 n+1950=0$
$5\left(\mathrm{n}^{2}-41 \mathrm{n}+390\right)=0$
$n^{2}-41 n+310+0$
$n^{2}-26 n-15 n+390=0$
$\mathrm{n}(\mathrm{n}-26)-15(\mathrm{n}-26)=0$
(n-26) $(\mathrm{n}-15)=0$
If $n-15=0$ if $n-26=0$
$\mathrm{N}=15 \mathrm{n}=26$
The entire amount will be paid in 15 months

## Question 3

If the sum of $\mathbf{n}$ terms of an $A P$ is $3 \mathbf{n}^{2} \mathbf{- n}$ and its common different is 6 , then its term is:
(a) 3
(b) 2
(c) 4
(d) 1

Answer: b

## Explanation:

Let $s_{n}$ be the sum of n terms of an AP with first term a and common difference d .
Since $s_{n}=3 n^{2}-\mathrm{n}$ and $\mathrm{d}=6$
$\rightarrow S_{n}=\frac{n}{2}(2 a+(n-1) d)=3 n^{2}-n$

$$
\begin{aligned}
= & \frac{n}{2}(2 a+(n-1) 6)=3 n^{2}-n \\
= & n(a+(n-1) 3)=3 n^{2}-n \\
= & (a+3 n-3)=3 n-1 \\
& a=2
\end{aligned}
$$

## Question 4

Insert two arithmetic means between 68 and 260.
(a) 132,196
(b) 130,194
(c) 70,258
(d) none

Answer: a

## Explanation:

Let two A.M.'S between 68 and 260 are $A_{1}, A_{2}$
68, A1, A2:260
$\mathrm{d}=\frac{b-a}{n+1}$
$d=\frac{260-68}{2+1}=\frac{192}{3}=64$
$\mathrm{A}_{1}=\mathrm{a}+\mathrm{d}=68+64=132$
$A_{1}=a+2 d=68+2 \times 64=196$

## NOV 2018

## Question:1

If the $p^{\text {th }}$ term of an A.P. is ' $q$ ' and the $q^{\text {th }}$ term is ' $p$ ', and then its $r^{\text {th }}$ term is
(a) $p+q-r$
(b) $p+q+r$
(c) $p-q-r$
(d) $p-q$

Answer: a

## Explanation:

Let $1^{\text {st }}$ term of AP is 'a'
And common different is'd'
Given $\mathrm{T}_{\mathrm{p}}=\mathrm{q}$
$a+(p-1) d=q$ $\qquad$ (i)
and $\mathrm{T}_{\mathrm{p}}=\mathrm{p}$
$a+(q-1) d=p$
$a+q d-d=p$ $\qquad$
Equation (i) and equation (ii)
$a+p d-d=q$
$a+q d-d=p$
$P d-q d=q-p$
$d(p-q)=-(p-q)$
$d=-1$
Putting $\mathrm{d}=-1$ in equation (i)
$a+p(-1)-(-1)=q$
$a=(p+q-1)$
Then, $\mathrm{T}_{\mathrm{r}}=\mathrm{a}+(\mathrm{r}-1) \mathrm{d}$

$$
\begin{aligned}
& =p+q-1+(r-1)(-1) \\
& =p+q-1-r+1 \\
& =p+q-r
\end{aligned}
$$

## Question 2

The $3^{\text {rd }}$ term G.P. is $\frac{2}{3}$ and the $6^{\text {th }}$ term is $\frac{2}{81}$, term the $1^{\text {st }}$ term is
(a) 6
(b) $\frac{1}{3}$
(c) 9
(d) 2

Answer: a
Explanation:
Let $1^{\text {st }}$ term of G.P. is ' $a$ ' and common ratio is ' $r$ ' then
Given $\mathrm{T}_{3}=\frac{2}{3}$ and $\mathrm{T}_{6}=\frac{2}{81}$
$\mathrm{ar}^{2}=\frac{2}{3}$ $\qquad$ (i)
$\operatorname{ar}^{5}=\frac{2}{81}$
Eq (2) / eq (1)
$\frac{a r^{5}}{a r^{2}}=\frac{\frac{2}{81}}{\frac{2}{3}}$
$\mathrm{r}^{3}=\frac{2}{81} \times \frac{3}{2} \rightarrow \mathrm{r}^{3}=\frac{1}{27} \rightarrow \mathrm{r}=\frac{1}{3}$
Putting $r=\frac{1}{3}$ in equation (i)
$a r^{2}=\frac{2}{3}$
$\mathrm{a}=\left[\frac{1}{3}\right]^{2}=\frac{2}{3} \rightarrow \mathrm{a} \times \frac{1}{9}=\frac{2}{3}$
$\mathrm{a}=\frac{2}{3} \times \frac{9}{1}$
$a=6$

## Question 3

The sum of the series -8,--6-4 ...n terms is 52 . The number of terms $n$ is:
a) 11
b) 12
c) 13
d) 10

Answer: c
Explanation:
Given series
$-8,-6,-4, \ldots \ldots$. n term
Let term (a) = -8
Common difference $(\mathrm{d})=(-6)-(-8)$

$$
=-6+8
$$

$$
=2
$$

Sum of ' $n$ ' term $\left(\mathrm{S}_{\mathrm{n}}\right)=52, \mathrm{n}=$ ?
We know that
$S_{n}=\frac{n}{2}(2 \mathrm{a}+(\mathrm{n}-1) \mathrm{d})$
$52=\frac{n}{2}[2 \times(-8)+(n-1)(2)]$
$104=n[2 n-18]$
$104=2 n^{2}-18 n$
$2 n^{2}-18 n-104=0$
$n^{2}-9 n-52=0$
$(n-13)(n+4)=0$
If $\mathrm{n}-13 \rightarrow \mathrm{n}=13$ and $\mathrm{n}+4=0 \rightarrow \mathrm{n}=-4$

## Question 4

The value of $K$, for which the mean the term $7 \mathrm{~K}+3,4 \mathrm{~K}-5,2 \mathrm{~K}+10$ are in A.P., is
(a) 13
(b) -13
(c) 23
(d) -23

Answer: d

## Explanation:

If $7 \mathrm{~K}+3,4 \mathrm{~K}-5,2 \mathrm{~K}+10$ are in A.P
Then,
$(4 \mathrm{~K}-5)-(7 \mathrm{~K}+3)=(2 \mathrm{~K}+10)-(4 \mathrm{~K}-5)$
$4 \mathrm{~K}-5-7 \mathrm{~K}-3=2 \mathrm{~K}+10-4 \mathrm{~K}+5$
$-3 \mathrm{~K}-8=-2 \mathrm{~K}+15$
$-8-15=-2 K+3 K$
$-23=\mathrm{K}$

## MAY 2019

## Question1

If $y=1+x+x^{2}+$ $\qquad$ $\infty$ then $x=$
(a) $\frac{y-1}{y}$
(b) $\frac{y+1}{y}$
(c) $\frac{y}{y+1}$
(d) $\frac{y}{y-3}$

Answer: a

## Explanation:

$y=1+x+x^{2}+$ $\qquad$ $\ldots$
is equivalent to $\mathrm{GP}=\frac{a}{1-r}$
$\mathrm{Y}=\frac{1}{1-x}$
$1-\mathrm{X}=\frac{1}{y}$
$1 \frac{1}{y}=\mathrm{x}$
$\frac{y-1}{y}=\mathrm{x}$

## Question2

If $\mathbf{2 + 6 + 1 0 + 1 4 + 1 8 + ~}$ $\qquad$ $+x=882$ then the value of $x$
(a) 78
(b) 80
(c) 82
(d) 86

Answer: c

## Explanation:

$2+6+10+14+18+\ldots \ldots \ldots \ldots . .+x=882$
Sum of AP
$\mathrm{S}_{\mathrm{m}}=\frac{n}{2}[2 \mathrm{a}+(\mathrm{n}-1) \mathrm{d}]$
$\mathrm{S}_{\mathrm{m}}=\frac{n}{2}[\mathrm{a}+1]$
$882=\frac{n}{2}[2+x] \ldots . . . . . . . .(1)$
$882=\frac{n}{2} \times 2[2+(n-1) 2]$
$882=n[2+2 n+2]$
$882=2 n^{2}$
$\mathrm{N}^{2}=441$
$\mathrm{n}=\sqrt{441}$
$\mathrm{n}=21$
Put n in eq 1
$882=\frac{21}{2}[2+x]$
$84=2+x$
$\mathrm{X}=84-2=82$

## Question 3

In a G.P, if the fourth term is ' 3 ' then the product of first seven terms is
(a) $3^{5}$
(b) $3^{7}$
(c) $3^{6}$
(d) $3^{8}$

## Explanation:

Let first term be a and common ratio be r.
Then according to question
$\mathrm{ar}^{3}=3$
Product of $1^{\text {st }} 7$ terms $(a)^{7}(r)^{21}=\left(a r^{3}\right)^{7}=(3)^{7}$

## Question 4

The ratio of sum of $n$ terms of the two AP's is $(n+1):(n-1)$ then the ratio of their $m^{\text {th }}$ terms is
(a) $(\mathrm{m}+1): 2 \mathrm{~m}$
(b) $(m+1):(m-1)$
(c) $(2 m-1:(m+1)$
(d) $\mathrm{m}:(\mathrm{m}-1)$

Answer: d
Explanation:
$\frac{\frac{n}{2}[2 a+(n-1) d]}{\frac{n}{2}\left[2 a^{\prime}+(n-1) d^{\prime}\right]}=\frac{n+1}{n-1}$
$\frac{a+\frac{(n+1) d}{2}}{\frac{a^{\prime}+(n-1) d^{\prime}}{2}}=\frac{n+1}{n-1}$
$\mathrm{T}_{\mathrm{n}} \mathrm{th}^{\mathrm{t}}=\mathrm{a}+(\mathrm{n}-1) \mathrm{d}$
$\frac{n-1}{1}=n-1$
$\mathrm{n}-1=2 \mathrm{n}-2$
$\mathrm{n}=2 \mathrm{~m}-2+1$
$\mathrm{n}=2 \mathrm{~m}$
$\mathrm{n}=2 \mathrm{~m}-1$
$\frac{2 \mathrm{~m}}{2 \mathrm{~m}-2}=\frac{2 \mathrm{~m}}{2(\mathrm{~m}-1)}=\frac{\mathrm{m}}{\mathrm{m}-1}$

## Question 5

## The sum of the series

0.5+0.55+0.555+ to n terms is:
a) $5 \mathrm{n} / 9+5 / 9\left[1-(* 0.1)^{\mathrm{n}}\right]$
b) $5 \mathrm{n} / 9-5 / 81\left[1-(0.1)^{\mathrm{n}}\right]$
c) $5 \mathrm{n} / 81+5 / 81\left[1-(0.1)^{\mathrm{n}}\right]$
d) $5 n / 9+5 / 81\left[1-(0.1)^{n}\right]$

## Answer: b

## Explanation:

Given series $0.5+0.55+0.555$...... n terms
we know that,

$$
\begin{aligned}
& 0.1+0.1^{2}+0.1^{3}+\ldots \ldots \ldots . .=\frac{0.1\left(1-0.1^{n}\right)}{0.9}=\frac{\left(1-0.1^{n}\right)}{9} \\
& \rightarrow 5(0.1+0.11+0.111+\ldots \ldots . .) \\
& \quad \rightarrow 5\left(\frac{1}{10}+\frac{11}{100}+\frac{111}{1000}+\ldots \ldots\right) \\
& \quad \rightarrow \frac{5}{9}\left(\frac{9}{10}+\frac{99}{100}+\frac{999}{1000}+\ldots .\right) \\
& \quad \rightarrow \frac{5}{9}\left(\left(1-\frac{1}{10}\right)+\left(1-\frac{1}{100}\right)+\left(1-\frac{1}{1000}\right)+\ldots . .\right) \\
& \quad \rightarrow \frac{5}{9}(1+1+\ldots \mathrm{n} \text { terms })-\left(\frac{1}{10}+\frac{1}{100}+\frac{1}{1000}+\ldots .\right) \\
& \quad \rightarrow \frac{5}{9}\left(n-\frac{\left(1-0.1^{n}\right)}{9}\right)
\end{aligned}
$$

## Question 1

If $\frac{(b+c-a)}{a}, \frac{(c+a-b)}{b}, \frac{(a+b-c)}{c}$ are in AP then $a, b, c$ are in
a) AP
b) GP
c) HP
d) None

Answer: (c)

## Explanation:

Given :
$\frac{(\mathbf{b}+\mathbf{c}-\mathbf{a})}{\mathbf{a}}, \frac{(\mathbf{c}+\mathbf{a}-\mathbf{b})}{\mathbf{b}}, \frac{(\mathbf{a}+\mathbf{b}-\mathbf{c})}{\mathbf{c}}$ are in A.P.
Add 2 to each
$\frac{(b+c-a)}{a}+2, \frac{(c+a-b)}{b}+2, \frac{(a+b-c)}{c}+2$
$=\frac{b+c-a+2 a}{a}, \frac{c+a-b+2 b}{b}, \frac{a+b-c+2 c}{c}$
$=\frac{a+b+c}{a}, \frac{a+b+c}{b}, \frac{a+b+c}{c}$
Now, divide by $\mathrm{a}+\mathrm{b}+\mathrm{c}$
$=\frac{1}{\mathrm{a}}, \frac{1}{\mathrm{~b}}, \frac{1}{\mathrm{c}}$ are in A.P.
We know, $\mathrm{HP}=\frac{1}{\text { A.P. }}$
$=\mathrm{a}, \mathrm{b}, \mathrm{c}$ are in H.P.
$\therefore$ Option c i.e. H.P is the correct option,

## Question 2

Sum upto infinity of series
$\frac{1}{2}+\frac{1}{3^{2}}+\frac{1}{2^{3}}+\frac{1}{3^{4}}+\frac{1}{25^{2}}+$
(a) $19 / 24$
(b) $24 / 19$
(c) $5 / 24$
d) none

Answer: (a)

## Explanation:

We know
$\mathrm{S} \infty=\frac{a}{1-r^{\prime}}, \mathrm{r}<1$
Here, $\frac{1}{2}+\frac{1}{3^{2}}+\frac{1}{2^{3}}+\frac{1}{3^{4}}+\frac{1}{25^{2}}+\ldots \ldots .$.
$\left(\frac{1}{2}+\frac{1}{3^{3}}+\frac{1}{2^{5}}+\ldots \ldots \infty\right)+\frac{1}{2}+\frac{1}{3^{3}}+\frac{1}{2^{5}}+$
$\left\{a=\frac{1}{2}, r=\frac{1}{4}<1\right\} ;\left\{a=\frac{1}{2}, r=\frac{1}{4}, 1\right\}$
$\left(\frac{\frac{1}{2}}{1-\frac{1}{4}}\right)+\left(\frac{\frac{1}{9}}{1-\frac{1}{9}}\right)$
$\frac{\frac{1}{2}}{\frac{3}{4}}+\frac{\frac{1}{9}}{\frac{8}{9}}$
$\frac{1}{2} \times \frac{4}{3}+\frac{1}{9} \times \frac{9}{8}$
$\frac{2}{3}+\frac{1}{8}$

## Question 3

Sum the series $\frac{1}{5_{5}}, \frac{1}{5^{2}}, \frac{1}{5^{3}}, \ldots . . . . \frac{1}{5^{n}}$
(a) $\frac{1}{4}\left[1-\left(\frac{1}{5}\right)^{n}\right]$
(b) $\frac{1}{5}\left[1-\left(\frac{1}{4}\right)^{n}\right]$
(c) both
(d) none

Answer: (a)
Explanation:
Series ${ }_{5^{\prime}}, \frac{1}{5^{2}}, \frac{1}{5^{3}}, \ldots \ldots . . \frac{1}{5^{n}}$
So, here $\mathrm{a}=\frac{1}{5}, \mathrm{r}=\frac{1}{5}, \frac{1}{5}<1$
$\mathrm{Sn}=\mathrm{a} \frac{\left(1-r^{n}\right)}{(1-r)}, \mathrm{r}<1$
$\mathrm{Sn}=\frac{1}{5}\left[\frac{1-\left(\frac{1}{5}\right)^{n}}{1-\left(\frac{1}{5}\right)}\right]$
$\mathrm{Sn}=\frac{1}{5} \times \frac{5}{4}\left[1-\left(\frac{1}{5}\right)^{n}\right]$
$\mathrm{Sn}=\frac{1}{4}\left[1-\left(\frac{1}{5}\right)^{n}\right]$

## Question 4

Find the no. of terms of the series $25,5,1$.............. $\frac{1}{3125}$
(a) 6
(b) 7
(c) 8
(d) 9

Answer: (c)
Explanation:
Here gives the series $25,5,1 / 5$.....
Let the Total Number of Terms = n
First Term a $=25$
Common ratio $r=1 / 5$
Last Term $\mathrm{a}_{\mathrm{n}}=\frac{1}{3125}$
we have the formula
$a_{n}=\mathrm{ar}^{\mathrm{n}-1}$

$$
\begin{aligned}
& \Rightarrow \frac{1}{3125}=25\left(\frac{1}{5}\right)^{n-1} \\
& \Rightarrow\left(\frac{1}{5}\right)^{5}=\left(\frac{1}{5}\right)^{n-3} \\
& \Rightarrow \mathrm{n}-3=5 \\
& \Rightarrow \mathrm{n}=8
\end{aligned}
$$

Yes, $1 / 3125$ is the $8^{\text {th }}$ term of the series.

## Question 5

If the sum of five terms of AP is 75. Find the third term of the series.
(a) 35
(b) 30
(c) 15
(d) 20

Answer: (c)

## Explanation:

We know
$S_{n}=\frac{n}{2}[2 \mathrm{a}+(\mathrm{n}-1) \mathrm{d}]$
$\mathrm{n}=5 \quad \mathrm{~S} 5=75$
$S_{5}=\frac{5}{2}[2 a+(5-1) d]$
$75=\frac{5}{2}[2 a+4 d]$
$15=\mathrm{a}+2 \mathrm{~d}$
$\mathrm{T}_{3}=\mathrm{a}+(3-1) \mathrm{d}$
$\mathrm{T}_{3}=\mathrm{a}+2 \mathrm{~d}$
-------From Eq (1)
$\mathrm{T}_{3}=15$

## Question6

If the AM and GM of the two numbers is $\mathbf{6 . 5}$ and $\mathbf{6}$ the no's are:
(a) 3 and 2
(b) 9 and 4
(c) 81 and 16
(d) None

Answer: (b)
Explanation:
Let the two nos.be ' $a$ ' and ' $b$ '

| AM $=\frac{a+b}{2} ;$ | GM $=\sqrt{a b}$ <br> $\sqrt{a b}=6$ |
| :--- | :--- |
| $\frac{a+b}{2}=6.5$ | On squarin <br> ab $=36$ |
| $a+b=13$ |  |
| a $=13-\mathrm{b}$ |  |
| Put Eq (1) in Eq (2) |  |
| $\mathrm{b} \times(13-\mathrm{b})=36$ |  |
| $13 \mathrm{~b}-\mathrm{b}^{2}=36$ |  |
| $b^{2}-13 \mathrm{~b}+36=0$ |  |
| $b^{2}-9 b-4 \mathrm{~b}+36=0$ |  |
| $\mathrm{~b}(\mathrm{~b}-9)-4(\mathrm{~b}-9)=0$ | $\mathrm{~b}=4$ |
| $\mathrm{~b}=9$ | $\mathrm{a}=13-4$ |
| $\mathrm{a}=13-9$ | $\mathrm{a}=9$ |
| $\mathrm{a}=4$ |  |

So the two numbers are 4 and 9

## Question: 7

If $A M$ and $H M$ for numbers are 5 and $3: 2$, respectively GM will be
(a) 20
(c) 16
(c) 4
(d) 5

Answer:(c)

## Explanation:

We know that
$(\mathrm{GM})^{2}=\mathrm{AM} \times \mathrm{HM}$
Here $(\mathrm{GM})^{2}=5 \times 3.2$
$(\mathrm{GM})^{2}=16$
$(G M)=4$.

## DEC 2020

## Question 8

The $20^{\text {th }}$ term of arithmetic progression whose $6^{\text {th }}$ term is 38 and $10^{\text {th }}$ term is $\mathbf{6 6}$ is $\qquad$
(a) 136
(b) 118
(c) 178
(d) 210

Answer: a

## Explanation:

Let a and $d$ be the first term and common difference of an AP
It is given that, $6^{\text {th }}$ term $\mathrm{a}_{6}=38$ and $10^{\text {th }}$ term $\mathrm{a}_{10}=66$.
Therefore,
$a+5 d=38$
$a+9 d=66$
Subtracting (i) from (ii), we have
$4 d=-28$
d = 7
Substituting in (i), we have
$a+5(7)=38$
Hence, the $20^{\text {th }}$ term is 136 .

## Question 9

Three numbers in G.P with their sum is $\mathbf{1 3 0}$ and their product is 27,000 are $\qquad$
(a) $90,30,10$
(b) $10,30,90$
(c) $10,20,30$
(d) Both

Answer: d

## Explanation:

Let the three number be $\frac{a}{r}$,a, ar
$\frac{a}{r}+a+a r=130$
$\frac{a}{r} \cdot a \cdot a r=27000 \rightarrow a^{3}=(30)^{3}$
$=30$
$a\left[\frac{1+r+r^{r}}{r}\right]=130$
$\frac{1+r+r^{r}}{r}=\frac{13}{3}$
$\rightarrow 3 r^{r}-10 r+3$
$\rightarrow \mathrm{r}=3$ or $\frac{1}{3}$
The numbers are 10,30 , and 90

## Question 10

Divide 69 into $\mathbf{3}$ parts which are in A.P and are such that the product of first two parts is $\mathbf{4 6 0}$
(a) $20,23,26$
(b) $21,23,25$
(c) $19,23,27$
(d) $22,23,24$

## Answer: a

Explanation:

Let the first term of the AP be 'a'
And the common difference be 'd'
Since 69 split into 3 parts such that they form an AP.
Let the three parts be $(a-d),(a)$ and $(a+d)$.
Therefore,
$(a-d)+(a)+(a+d)=69$
$3 \mathrm{a}=69$
$\mathrm{a}=23$
The product if two smaller parts $=460$
So,
(a) $\times(\mathrm{a}-\mathrm{d})=460$
$23 \times(23-d)=460$
$\Rightarrow 529-23 \mathrm{~d}=460$
$\Rightarrow-23 \mathrm{~d}=460-529$
$\Rightarrow-23 d=-69$
$\Rightarrow \mathrm{d}=63 / 23$
$\Rightarrow d=3$
Therefore,
The 3 parts are
$23-3=20$;
And $23+3=26$
Hence the parts of the given AP are 20,23 , and 26

## IAN 2021

## Question 1

The nth term of the series $3+7+13+21+31+\ldots$. is
(a) $4 \mathrm{n}-1$
(b) $n^{2}+2 n$
(c) $n^{2}+n+1$
(d) $n^{3}+2$

Answer: c
Explanation:
$3+7+13+21+\ldots . . a_{n-1}+a_{n}$
$3+7+13+21+\ldots . . a_{n-2}+a_{n-1}+a_{n}$
Eq $1-$ Eq 2
s -s $=3-0+(7+3)+(13-7)+\ldots \ldots+\left(a_{n-1}-a_{n-2}+\left(a_{n}-a_{n-1}\right)-a_{n}\right.$
$0=\left[3+4+6+\ldots .+a_{n-1}\right]-a_{n}$
$a_{n}=3+\left[4+6+8+---+a_{n-1}\right.$
Now $4+6+8+---+a_{n-1}$ are in A.P.
First term $a=4$, Common difference $d=2$
Sum of $n$ herm of AP $=\frac{n}{2}[2 a+(n-1) d]$
$=4+6+8 \pm--a_{n-1}=\frac{n-1}{2}[2 \times 4+(n-1-1) \times 2]$
$=\left(\frac{n-1}{2}\right)[8+2 n-4]$
$=\frac{n-1}{2}(2 n+4)$
$=\left(4+6+8+\ldots \ldots .+a_{n-1}=(n-1)(n+2)\right.$

By Eq 3
$a_{n}=3+\left[4+6+8+---+a_{n-1}\right]$
$a_{n}=3+(\mathrm{n}-1)(\mathrm{n}+2)$
$=3+n^{2}-n+2 n-2$
$a_{n}=\mathrm{n}^{2}+\mathrm{n}+1$

## Question 2

The number of integers from 1 to 100 which are neither divisible by 3 , nor by 5 nor by 7 , is
(a) 67
(b) 55
(c) 45
(d) 33

Answer: c
Explanation:
Total No. - 100
divide by $3=100 / 3=33$
divide by $5=100 / 5=20$
divide by $7=100 / 7=14$
$=33+20+14=67$
$3 \& 5=100 / 15=6$
$5 \& 7=100 / 35=2$
$7 \& 3=100 / 21=4$
$=6+2+4=12$
$=67-12=55$
Total Divisible by 3,5\&7 are 55
Total - divisible $=$ not divisible
$100-55=45$

## Question 3

In a geometric progression, the $3^{\text {rd }}$ and $6^{\text {th }}$ terms are respectively, 1 and $-1 / 8$. The first term (a) and common ratio are respectively.
(a) 4 and $\frac{1}{2}$
(b) 4 and $\frac{-1}{4}$
(c) 4 and $\frac{-1}{2}$
(d) 4 and $\frac{1}{4}$

Answer: c
Explanation:
By option c
$a=4 \& r=-1 / 2$
Check $3^{\text {rd }}$ GP
$1 / 2 \times 4====(4$ time equals to $)=1$
checking $6^{\text {th }}$ GP
$1 / 2 \times 4=======(7$ time equals to) $=-0.125$
$=-1 / 8=0.125$

## ULY 2021

## Question 1

The number of team of the series: $5+7+9+\ldots . . . .$. Must be taken so that the sum may be 480
(a) 20
(b) 10
(c) 15
(d) 25

Answer: Options (a)
Explanation:
5 + 7 + 9 -------
$a=5, d=2, s=480$
$\mathrm{S}=n / 2(2 \mathrm{a}+\mathrm{n}-1) \mathrm{d}$
$480=n / 2(2(5)+(n-1)(2)$
$480=n / 2(10+2 n-2)$
$480=n(2 n+8)$
$480=2 n^{2}+8 n$
$2 n^{2}+8 n-480$
$2\left(n^{2}+4 n-480\right)$
$\Rightarrow n^{2}+4 n-480$
$n^{2}+20 n+24 n-480$
$\mathrm{n}(\mathrm{n}-20)+24(\mathrm{n}-20)$
$n+24=0$
$\mathrm{n}=-24$


## Question 2

The fifth term of an AP of $\boldsymbol{n}$ terms, whose sum is $\mathbf{n}^{2}-2 n$, is
(a) 5
(b) 7
(c) 8
(d) 15

Answer: Options (b)
Explanation:-
Given: Sum of $n$ terms of an $A P=n^{2}-2 n$.
To find: The fifth term =?
Sum of ' $n$ ' terms of an AP $=n^{2}-2 n$
$\therefore$ Sum of $1^{\text {st }} 5$ terms
$\Rightarrow s_{5}=5^{2}-2$. (5)
$\Rightarrow 25-10=15$
Similarly,
Now, sum of first 4 terms
$S_{5}=5^{2}-2$. (5)
$=25-10=15$
Similarly,
Now, sum of first 4 terms
$\mathrm{S}_{4}=5^{2}-2$. (4)
$=16-8=8$
$\therefore$ The $5^{\text {th }}$ term of an AP"
$\Rightarrow \mathrm{t}_{5}=\mathrm{S}_{5}-\mathrm{S}_{4} \quad \ldots,\left(\operatorname{Using} T_{n}=S_{n}-S_{n-1}\right)$
$=15-8$
$=7$
So, option 2 is correct.

## Question 3

The sum of three numbers in a geometric progression is 28 . When 7,2 and 1 are subtracted from the first, second and third numbers respectively, then the resulting numbers are in
arithmetic progression. What is the sum of squares of the original three numbers?
(a) 510
(b) 456
(c) 400
(d) 336

Answer: Options (d)

## DEC 2021

## Question 1

If the sum and product of three number in G.P. are 7 and 8 respectively, then $4^{\text {th }}$ term of the series is
(a) 6
(b) 4
(c) 8
(d) 16

Answer: d
Explanation:-
$\mathrm{t}_{\mathrm{n}}=\mathrm{ar}^{\mathrm{n}-1}$
Let the three terms of G.P. be $a / r$, a and ar respectively.
Since the product is 8 , we have:
$\frac{a}{r} \times a \times a r=8$
$\mathrm{a}^{3}=8$
$\mathrm{A}=(8)^{1 / 3}=2$
Also, it is given that $\frac{a}{r}+a+a r=7$
$\frac{a+a r+a r^{2}}{r}=7$
$a+a r+a r^{2}=7 r$
Putting the value of $\mathrm{a}=2$ above, we get:
$2+2 r+2 r^{2}=7 r$
$2 r^{2}+2 r-7 r+2=0$
$2 r^{2}-5 r+2=0$
$2 r^{2}-4 \mathrm{r}-\mathrm{r}+2=0$
$2 r(r-2)-(r-2)=0$
$(2 r-1)(r-2)=0$
So, either $2 r-1=0-r=\frac{1}{2}$
Or r-2 = $0-r=2$
Taking $r=1 / 2$, we have $t_{4}=2\left[\frac{1}{2}\right]^{3}=0.25$
Taking $r=2$, we have $t_{4}=2(2)^{3}=16$
Since 0.25 is not in the options, option(d) is the answer.

## Question 2

The sum of series $7+14+21+\ldots$. To $17^{\text {th }}$ term is:
(a) 1071
(b) 971
(c) 1171
(d) 1271

Answer: a

## Explanation:-

Clearly, this is an AP with $a=7$; $d=14-7=7$; $n=17$
$\mathrm{S}_{\mathrm{n}}=\frac{n}{2}\{2 \mathrm{a}+(\mathrm{n}-1) \mathrm{d}\}$
$\left.S_{17}=\frac{17}{2}\{(2 \times 7)+17-1) 7\right\}=1,071$

## Question 3

The sum of first $\mathbf{n}$ terms an $A P$ is $\mathbf{3 n} \mathbf{n}+\mathbf{n}$. The series is:
(a) $8,14,20,26$,
(b) $8,22,42,68, \ldots$
(c) $22,68,114, \ldots$.
(d) $8,14,28,44, \ldots$

Answer:
Explanation:-
$\mathrm{S}_{1}=\mathrm{t}_{1}=\mathrm{a}=3(1)^{2}+5(1)=3+5=8$
$\mathrm{S}_{2}=3(2)^{2}+5(2)=22$
$\mathrm{t}_{2}=22-8=14$
$\mathrm{d}=\mathrm{t}_{2}-\mathrm{t}_{1}=14-8=6$

## Question 4

The largest value of $\mathbf{n}$ which $\frac{1}{2}+\frac{1}{2^{2}}+\cdots \frac{1}{2^{n}}<\mathbf{0 . 9 9 8 i s}$
(a) 9
(b) 6
(c) 7
(d) 8

Answer: d

## Explanation:-

The given series is a GP with $a=1 / 2 ; r=1 / 2$
Since $r<1, S_{n}=a\left[\frac{1-r^{n}}{1-r}\right]$
Try the options,
Option (a) - 9
If $\mathrm{n}=9$
$S_{9}=\frac{1}{2}\left(\frac{1-(1 / 2)^{9}}{1-(1 / 2)}\right)=0.998046875$
Option (b) - 6
If $n=6$
$S_{6}=\frac{1}{2}\left(\frac{1-(1 / 2)^{6}}{1-(1 / 2)}\right)=0.984375$
Option (c) - 7
If $\mathrm{n}=6$
$S_{7}=\frac{1}{2}\left(\frac{1-(1 / 2)^{7}}{1-(1 / 2)}\right)=0.9921875$
Option (d) - 8
If $\mathrm{n}=8$
$S_{8}=\frac{1}{2}\left(\frac{1-(1 / 2)^{8}}{1-(1 / 2)}\right)=0.99609375$
Clearly, option (d) is the answer as it is the largest value for which the sum of the series is less than 0.998 .

UNE 2022

## Question 1

The $n^{\text {th }}$ term of the series $9,7,5$, $\qquad$ and 15,12,9, $\qquad$ are same. Find the $n^{\text {th }}$ term?
(a) 7
(b) 8
(c) 9
(d) 10

Answer: Options (a)
Explanation:
Given Series
9, 7, 5 . n term
$a=9, d=7-9=-2, n=n$
$\mathrm{T}_{\mathrm{n}}=\mathrm{a}+(\mathrm{n}-1) \mathrm{d}$
$\mathrm{T}_{\mathrm{n}}=9+(\mathrm{n}-1)(-2)$
$=9-2 n+2$
$=11-2 n$
and other series
$=15,12,9 \ldots \ldots \ldots \ldots . . . . . . . . . n$ term
$a=15, d=12-15=-3, n=n$
$T_{n}=a+(n-1) d$
$=15+(n-1)(-3)$
$=15-3 n+2=18-3 n$
$=11-2 n$
Given $\mathrm{n}^{\text {th }}$ term of both series are equal

$$
\begin{aligned}
& \text { then } 11-2 n=18-3 n \\
& 3 n-2 n=18-11 \\
& n=7
\end{aligned}
$$

## Question 2

Then sun of first 8 terms of a G.P is five times the sum of the first 4 terms. Find the common ratio?
(a) $\pm \sqrt{2}$
(b) 16
(c) $\pm \sqrt{20}$
(d) 4

Answer: Options (a)
Explanation:
Let $1^{\text {st }}$ term of G.P $=\mathrm{a}$
Common Ratio (r) = r
Given
$\mathrm{S}_{8}=5 \mathrm{~S}_{4}$
$\frac{a\left(r^{8}-1\right)}{r-1}=5 \frac{a\left(r^{4}-1\right)}{r-1}$
$\mathrm{r}^{8}-1=5\left(\mathrm{r}^{4}-1\right)$
$\left(r^{4}\right)^{2}-(1)^{2}=5\left(r^{4}-1\right)$
$\mathrm{r}^{4}+1=5$
$r^{4}=4$
$\left(r^{2}\right)^{2}=(2)^{2} \Rightarrow r= \pm \sqrt{2}$

## Question 3

A person pays ₹ 975 in monthly instalments; each instalment is less then former by ₹ 5 . The amount of $1^{\text {st }}$ instalments is $₹ 100$. In what time will the entire amount be paid?
(a) 26 months
(b) 15 months
(c) Both (a) and (b)
(d) 18 months

Answer: Options (a)

## Explanation:

Given $\mathrm{Sn}=975,1^{\text {st }}$ Installment $(\mathrm{a})=100, \mathrm{~d}=-5$
Then series is
100, (100-5), (100-5-5), ..n term
100, $95,90, \ldots \ldots . . \mathrm{n}$ term
$\mathrm{Sn}=\frac{n}{2}[2 a+(n-1) d]$
$975=\frac{n}{2}[2 \times 100+(n-1)(-5)]$
$975 \times 2=n[200-5 n+5]$
$1950=n(205-5 n)$
$1950=205 n-5 n^{2}$
$5 n^{2}-205 n+1950=0$
or $n^{2}-41 n+390=0$
Solving this we get $\mathrm{n}=15$ or $\mathrm{n}=26$ (not valid)

## DEC 2022

## Question 1

If $p^{\text {th }}$ term of an AP is $q$ and its $q^{\text {th }}$ term is $p$, then what will be the value of $(p+q)^{\text {th }}$ term?
a) 0
b) 1
c) $p+q-1$
d) $2(p+q-1)$

Answer: Options (a)
Explanation:-
In the given AP, let the first be a and the common difference be d .
Then, $\mathrm{Tn}=\mathrm{a}+(\mathrm{n}-1) \mathrm{d}$
$\rightarrow \mathrm{Tp}=\mathrm{a}+(\mathrm{p}-1) \mathrm{d}=\mathrm{q}$ (1)
$\rightarrow \mathrm{Tq}=\mathrm{a}+(\mathrm{q}-1) \mathrm{d}=\mathrm{p}(2)$
On subtracting (i) from (ii), we get:
( $q-p$ ) $d=(p-c)$
$\rightarrow d=-1$
Putting $d=-1$ inn, we get
$a=(p+q-1)$
Thus , $a=(p+q-1)$ and $d=-1$
Now, $T_{p+q}=a+(p+q-1) d$
$=(p+q-1)+(p+q-1)(-1)$
$=(p+q-1)-(p+q-1)=0$

## Question 2

In a G.P. $5^{\text {th }}$ term is 27 and $8^{\text {th }}$ term is 729. Find its $11^{\text {th }}$ term.
a) 729
b) 6561
c) 2187
d) 19683

Answer: Options (d)
Explanation:-
Given, $\mathrm{a}_{5}=27$ and $\mathrm{a}_{8}=729$.
$=>\mathrm{ar}^{4}=27$ and $\mathrm{ar}^{7}=729$
On dividing we get,
$r^{3}=27 \Rightarrow r=3 \Rightarrow r=3$
$\Rightarrow \Rightarrow \mathrm{a}=27 /\left(3^{4}\right)=1 / 3$
$\Rightarrow \Rightarrow a_{11}=\operatorname{ar}^{10}=(1 / 3)\left(3^{10}\right)=3939=19683$.

## Question 3

Find the missing number in the following series?
3, 5, 5, 19, 7, 41, 9, ?, 11, 109
a) 71
b) 61
c) 69
d) 79

Answer: Options (a)
Explanation:-
First series: 3, 5, 7, 9
Second series: 5, 19, 41,?
Difference of Second series are 14, 22, 30 etc
Next term is $41+30$ i.e equal to 71

## Question 4

Find the next number in the given sequence?
$11,17,39,85$, ?, 281, 447
a) 133
b) 143
c) 153
d) 163

> Answer: Options (d)
> Explanation:-
> 11
> $11+\left(3^{2}-3\right)=17$
> $17+\left(5^{2}-3\right)=39$
> $39+\left(7^{2}-3\right)=85$
> $85+\left(9^{2}-3\right)=163$

Hence, the next number in the given sequence is 163 . Hence, option 4 is the correct answer.

