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## CHAPTER - 3 LINEAR INEQUALITIES

<b>INEQUALITIES</b>	Inequalities are statements where two quantities are unequal but a relationship exists between them. These type of inequalities occur in business whenever there is a limit on supply, demand, sales etc.		
LINEAR INQUALITIES IN ONE VARIABLE AND THE SOLUTION SPACE	Any linear function that involves an inequality sign is a linear Inequality. It may be of one variable or, of more than one variable. simple example of linear inequalities are those of one variable only ; viz., x> 0, x $\leq$ 0 etc. $\underbrace{\begin{array}{c} & & \\ \hline \hline & & \\ \hline \hline \\ \hline & & \\ \hline & & \\ \hline \hline \hline & & \\ \hline \hline \hline \\ \hline \hline \hline \hline$		
SUMMARY OF GRAPHICAL METHOD	<ul> <li>It involves: <ol> <li>Formulating the linear programming problem, i.e. expressing the objective function and constraints in the standardized format.</li> </ol> </li> <li>Plotting the capacity constraints on the graph paper. For this purpose, normally two terminal points are required. This is done by presuming simultaneously that one of the constraints is zero. When constraints concern only one factor, then line will have only one origin point and it will run parallel to the other axis.</li> <li>Identifying feasible region and coordinates of corner points. Mostly it is done by breading the graph, but a point can be identified by solving simultaneous equation relating to two lines which intersect to form a point on graph.</li> <li>Testing the corner point which gives maximum profit. For this purpose, the coordinates relating to the corner point should put in</li> </ul>		
	<ul> <li>objectives function and the optimal point should be as certained.</li> <li>v. For decision – making purpose, sometimes, it is required to know whether optimal point leaves some resources unutilized. For this purpose, value of coordinates at the optimal point should be put with constraint to find out which constraints are not fully utilized.</li> <li>vi. Linear inequalities in two variables may be solved easily by extending our knowledge of straight lines.</li> </ul>		



### **Question 1**

On solving the inequalities  $6x + y \ge 18$ ,  $x + 4y \ge 12$ ,  $2x + y \le 10$ , we get the following situation:

(a) (0, 18), (12, 0), (4, 2), & (7, 6) (c) (5, 0), (0, 10), (4, 2), (7, 6) (b) (3, 0), (0, 3), 0, 0) and (7, 6) (d) (0, 18), (12, 0), (4, 2), (0, 0) and (7, 6)

## Answer: a

## Explanation:

We draw the graph of 6x+y 218, x+4y 212, and 2x+y 210 in –the same plane. The solution set of system is that portion of the graphs of the given inequality which is represented by the intersection of the above three equations.

### Question 2

Solve x +2 < 4 (a) x < 2 (b) x > 2(c)  $x \neq 2$  (d) x < 4Answer: a Explanation: We need to subtract 2 from both sides of the inequality. X+2<4 X<4-2 X<2

## Question 3

**Solve the inequality 3 – 2x \ge 15** (a)  $x \le 6$ 

(c) x>-6

Answer: b Explanation:

We need to subtract 3 from both sides; then divide both sides by -2 (remembering to change the direction of the inequality).

(b)  $x \le -6$ 

(d) x>6

 $=3-2x \ge 15$  $=-2x \ge 15-3$  $=-2x \ge 12$  $=x \le \frac{12}{-2}$  $=x \le -6$ 

Question 4

**Solve -1 < 2x +3 < 6** (a) -2<x<3/2 (c) 2<x<3/2 **Answer: a Expectation:** = -1<2x+3<6 Subtract 3 from all 3 sides

(b) 2<x<23/2 (d) -3<x<23/3

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= -1-3<2x+3-3<6-3 = -4<2x<3 Divide all sides by 2 = -2<x<3/2

## Question5

**Solve**  $\frac{x}{2}$ >8 (a) x<8 (c) x=8 **Answer: b Explanation:**  $=\frac{x}{2}$ >8  $=x>8\times2$ =x>16

## Question 6

The graph to express the inequality x + y = 56 is:



(c) Either a or b **Answer: a Explanation:** X + y = 56 is graphically represent by



(b) x>16 (d) x=4



<u>Question 7</u> On the average, experienced person does 5 units of work while fresh one 3 units work daily but the employer have to maintain the output to at least 30 units work per day. The situation can be expressed as

(a) 5x - 3y = 30
(c) - 5x + 3y = 30
Answer: b
Explanation:
Let Experience Person x unit work per day
Fresh one = y unit work per day
So situation is 5x + 3y = 30

#### **<u>Question 8</u>** Common region of the inequalities is:



(b) 5x + 3y = 30 (d) None of these

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(a) BCDB and DEFD
(c) HFGH
Answer: d
Explanation:
Common region of the inequalities is ABDFHKA

<u>Question 9</u>

The shaded region represents:



(a) x + y s 5, x : 1'.2, y :s; 1 (c) x + y s 5, X : 1!4, y : 1; ,1 **Answer: b**  (b) x + y: 1'. 5, x : 1 '.2 , y 1 (d) None of these

(b) Unbounded

(d) ABDFHKA

## **Explanation:**

Region represented by the line x + y = 5 touch the coordinate axes at (5, 0) and (0, 5) since the shaded region lies below the line x + y = 5. Hence it is represented by the in equation x + y = 5

### Question 10

A company produces two products A and B, each of which requires processing in two machines. The first machine can be used at most for 60 hours, the second machine can be used at most for 40 hours. The product A requires 2 hours on machine one and one hour on machine one and two hours on machine two. Above situation is using linear inequalities?

False None

(a) True	(b)
(c) Partial	(d)
Answer: a	

### **Explanation**:

Let the company produce, x number of product A and y number of product B.

As each of product A requires 2 hours in machine one and one hour in machine two, x number of product A requires 2x hours in machine one and x hours in machine two. Similarly, y number of product B requires y hours in machine one and 2y hours in machine two for 40 hours. Hence 2x + y cannot exceed 40. In other words,

(b) False

(d) None

2x + y = 60 and x + 2y = 40

Thus, the conditions can be expressed using linear inequalities.

## Question 11

The inequalities  $5x_1 + 4x_2 \ge 9$ ,  $x_1 + x_2 \ge 3$ ,  $x_1 \ge 0$  and  $x_2 \ge 0$  is correct?

- (a) True
- (c) Not sure
- Answer: a

#### **Explanation**:

We draw that straight lines  $5 \times 1 + 4 \times 2 = 9$  and  $\times 1 + x^2 = 3$ .

×1	0	9/5
× 2	9/4	0

Table for $5 \times_1 + 4 \times_2 = 9$	Table for $x_1 + x_2 = 3$			
	×1	0	3	
	×2	3	0	-

Now, if we take the point (4, 4), we find  $5 \times 1 + 4 \times 2 * 9$ 

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i.e., 5.4 + 4.4 \* 9or, 36 \* 9 (True)  $x_1 + x_2 * 3$ i.e., 4 + 4 \* 38 \* 3 (True) Hence (4, 4) is in the region which satisfies the inequalities

#### **Question 12**

Solve the inequality -2(x+3)<10(a) x>-8(b) x>16(c) x>8(d) x>-16Answer: a(d) x>-16Explanation:-2x-6<10-2x-6<10</td>-2x-6+6<10+6-2x-6+6<10+6-2x-2x<16-2x<16-2x-2x<216-2x<216-2xx>-8(d) x>-16

### **Question 13**

Solve the absolute value inequality	$ x ^{2} ^{3}x + 9 ^{3}6$
(a) -9 <x>3</x>	(b) -9 <x<3< th=""></x<3<>
(c) 9 <x>3</x>	(d) 9 <x<3< td=""></x<3<>
Answer: b	
Explanation:	
2 3x + 9  < 362 3x + 9 2 < 36	
3x + 9  < 18	
-18<3x+9	
-18-9<3x	
-27<3x	
-9 <x< td=""><td></td></x<>	

### Question 14

Solve x + 2 < 4(a) x < 1 (b) x > 2(c) x > -2 (d) x < 2Answer: d Explanation: We need to subtract 2 from both sides of the inequality. X+2 < 4X < 4-2X < 2

## Question 15

Solve  $\frac{x}{2}$ >4 (a) x<4 (b) x>8 (c) x>-4 (c) x<2 Answer: b Explanation: We need to multiply both sides of the inequality by 2.  $\frac{x}{2}$ >4 x>4×2 x>8

## **Ouestion 16**

Solve the inequality  $\frac{3}{2}(1 - x) > \frac{1}{4} - x$ (a)  $x < \frac{5}{2}$  (b) x < 5(c)  $x < \frac{10}{2}$  (d)  $x < \frac{5}{6}$ Answer: a Explanation:  $\frac{3}{2}(1 - x) > \frac{1}{4} - x$  6 - 6x > 1 - 4x -6x + 4x > 1 - 6 -2x > -5 $X < \frac{5}{2}$ 

## Question 17

The solution of the inequality 8x + 6 < 12x + 14 is: (a) (-2, 2) (b) (0, -2) (c) (2,) (d) (-2, ) Answer: d Explanation: = 8x + 6 < 12x + 14 = 6 - 14 < 12x - 8x = -8 < 4x= x > -2

## **Question 18**

Solve x-1 < 2x + 2 < 3x + 1(a) (x>3 and x>1 (b) (x>-3 and x<1)(c) (x<-3 and x>1 (d) (x>1)Answer: d Explanation: We need to find the intersecting of the "true" values. X -1<2x+2 and 2x+2<3x+1 x<2x+3 and 2x-<3x-1 x>-3 and x>1 The intersection of these 2 regions is x>1.

#### Question 19

Solve -2(x+4)>1 – 5x	
(a) x<3	(b) x>3
(c) x≠3	(d) x = 3
Answer: b	
Explanation:	
-2(x+4)>1-5x	
[-2x -8]1-5x	
3x-8>1	
3x>9	
x>3	

**Question 20** Solve the inequality |2x - 1| > 5

6262969699

(a) x<3			(b) x>3
(c) x≠3			(d) $x = 3$
Answer: b			
Explanation:		_	
Applying the relations	hips discussed	earlier:	
2x-1<5or 2x-1>5			
Solving both inequalit	ies, we get:		
2x<5+1	or	2x>5+1	
2x<-4	or	2x>6	
X<-2	or	x>3	
Question 21			
Find all pair if consec such that their sum i	cutive even po s less than 23	sitive integ	gers, both of the which are larger than 5
(a) (7.8) (7.3) and (2.3)	5 iess than 25.		(h) (6.8) (8.10)and(10.12)
(c) (5,7),(7,9)and(2,6) Answer: h			(d) (2,3),(4,5)and(3,1)
Explanation			
Let x and $x+2$ be two c	onsecutive eve	n nositive i	ntegers
Since both the integer	s are larger tha	$n = \frac{1}{2} \sum_{x > 5} \frac{1}{x > 5}$	(1)
Also sum of two is less	s than 23		
X+x+2<23			
=>2x+x<23			
Adding -2 to both side	S		
2x<23-2			
2x<212			
Dividing by 2 on both	sides		
$\frac{2x}{2} < 23 - 2$			
$2^{2}_{21}$			
$X < \frac{21}{2}$			
X < 10.5			
Step 2:			
Since x is an even posi	tive integer gre	eater than 5	and less than $10.5 \times \text{can}$ take value 6,8,10.
Thus the required pair	r of number is (	6, 8), (8, 10	) and (10, 12)
Hence B is the correct	answer.		
<b>Ouestion 22</b>			
The longest side of a	triangle is thr	ee times th	e shortest side and third side is
2cmshortest than the	e longest side.	If the perin	meter of the triangle is at least 61cm. find
the minimum length	of the shortes	t side.	
(a) 9cm			(b) 3cm
(c) 5cm			(d) None of these
Answer: a			
Explanation:			
Let the length of the sh	nortest side be	x cm	
Length of the largest s	ide is 3x cm		
Length of the third sid	e is 3x-2cm		
Since the perimeter of	the triangle is	at least 61 d	cm, we get,
X+3x+3x-2≥61	_		
7x-2≥61			
Adding 2 on both sides	S		
$= > 7x \ge 61 + 2$			
7x≥ 63			
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Dividing both sides by positive number 7  $\frac{7x}{7} \ge \frac{63}{7}$   $X \ge 9$ Step 2: The minimum length of the shortest side is 9 cm. Hence A is the correct answer.

## Question 23

Solve the inequality:  $2 \le 3x - 4 \le 5$ (a) [2, 8] (b) [4, 5] (c) [3, 4] (d) [2, 3] Answer: d **Explanation**: The given inequality is  $2 \le 3x - 4 \le 5$ Adding +4+4 throughout the inequality  $2+4 \le 3x - 4 + 4 \le 5 + 4$  $= > 6 \le 3x \le 9$ Dividing by positive number 3 throughout the inequality = >  $2 \le x \le 3$  $= > 2 \le x \le 3$ Step 2: Thus all real number, which are greater than or equal to 2, and less than or equal to 3, are solutions to the given inequality. The solution set is [2, 3] Hence D is the correct answer.

### **Question 24**

Graphs of in equations are drawn below:

11111N L1: 5x+3y=30 L2: x + y = 9L3: Y = X/3L4: y = x/2The common region (Shaded part) shown in the diagram refers to the inequalities (a)  $5x+3y \le 30$ (b)  $5x + 3y \ge 30$  $X + y \le 9$  $x + y \le 9$  $Y \le 1/2x$  $y \ge x/3$  $y \le x/2$  $y \le x/2$  $x \ge 0, y \ge 0$  $x \ge 0, y \ge 0$ (c)  $5x+3y \ge 9$ (d) None of these  $X + y \ge 9$  $Y \le x/3$  $y \ge x/2$  $x \ge 0, y \ge 0$ Answer: d **Explanation**: 5x + 3y > 30X + y < 9Y > 9  $Y \le x/2$  $X \ge 0; y \ge 0$ 

# **PAST EXAMINATION QUESTIONS:**

## **MAY 2018**

**Question 1** 

The linear relationship between are variable in an inequality:

(a) <u>ax+by≤c</u>

(b)  $\underline{ax.by \leq c}$ (d)  $\underline{ax+bxy \leq c}$ 

(c) <u>axy+by≤c</u> Answer: a

The linear relationship between two variables in an inequality  $ax+by \le c$ 

## **NOV 2018**

## **Ouestion 1**

On solving the inequalities  $5x+y \le 100$ ,  $x+y \le 60$ ,  $x \ge 0$ ,  $y \ge$ , we get the following solutions: (a) (0,0), (20, 0), (10, 50), & (0, 60)

(c) (0,0), (20,0), (0,100), & (10,50)

(b) (0,0), (60,0), (10,50) & (0,60) (d) None

#### Answer: a **Explanation**:

On solving the inequalities  $5x+y \le 100$ ,  $x+y \le 60$ ,  $x+y \le 60$ ,  $x \ge 0$ ,  $y \ge$ , we get (0, 0), (20, 0) (10, 50) & (0, 0)60) all satisfied above inequalities

## **MAY 2019**

Question 1	
The solution set of the in equation	ion x + 2 > 0 and 2x - 6 > 0 is
(a) (-2, ∞)	(b) (3,∞)
(c) (-∞, -2)	(d) (-∞, -3)
Answer: b	
Explanation:	
X + 2 > 0	
X > -2	2X - 6 > 0
6	2X > 6
$X > \frac{1}{2}$	
X > 3	
X € (3,∞)	
<b>Ouestions 2</b>	
The common region represente	ed by the following in equalities
	X2
	DE
	A B Xi
$L_1 = X_1 + X_2 \le 4$ ; $L_2 = 2X_1 + X_2 \ge 6$	
(a) OABC	(b) Outside of OAB
(c) $\triangle$ BCE	(d) $\triangle$ ABE
Answer: d	
Explanation:	



## (c) 66

## Answer: d

### **Explanation**

Note: According to the given question the correct answers is Rs.553. There is no correct

## <u>IAN 2021</u>

## **Question 1**

#### The common region in the graph of the inequalities $x + y \le 4$ , $x - y \le 4$ , $x \ge 2$ , *is*. (a) equilateral triangle (b) Isosceles triangle

- (c) Quadrilateral

(d) Square

(d) None of these

## Answer: b

**Explanation**:

common region in the graph of the inequalities  $x + y \le 4$ ,  $x - y \le 4$ ,  $x \ge 2$ , *is* it made isosceles triangle

## **Question 2**

If A + B = $\begin{vmatrix} 1 & 0 \\ 1 & 1 \end{vmatrix}$ and A - 2B = $\begin{vmatrix} -1 \\ 0 \end{vmatrix}$	$\begin{bmatrix} 1 \\ -1 \end{bmatrix}$ , then A =
(a) $\begin{bmatrix} 1 & 1 \\ 2 & 1 \end{bmatrix}$	(b) $\begin{bmatrix} 2/3 & 1/3 \\ 1/3 & 2/3 \end{bmatrix}$
(c) $\begin{bmatrix} 1/3 & 1/3 \\ 2/3 & 1/3 \end{bmatrix}$	(d) $\begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix}$
Answer: c	
Explanation:	
$2(a+b) = 2\begin{bmatrix} 1 & 0\\ 1 & 1 \end{bmatrix} = 2A + 2B = \begin{bmatrix} 2\\ 2 \end{bmatrix}$	$\begin{bmatrix} 0\\2 \end{bmatrix} (1)$
$A - 2B = \begin{bmatrix} -1 & 1\\ 0 & -1 \end{bmatrix}(2)$	
$2A + 2B + A - 2B = \begin{bmatrix} 2 & 0 \\ 2 & 2 \end{bmatrix} + \begin{bmatrix} -1 & 1 \\ 0 & -1 \end{bmatrix}$	
$3A = \begin{bmatrix} 1 & 1 \\ 2 & 1 \end{bmatrix}$	
$A = \frac{1}{3} \begin{bmatrix} 1 & 1 \\ 2 & 1 \end{bmatrix}$	
Hence answer will be = $\begin{bmatrix} 1/3 & 1/3 \\ 2/3 & 1/3 \end{bmatrix}$	
Question 3	
The matrix A = $\begin{bmatrix} 1 & -2 & 3 \\ 1 & -3 & 4 \\ -1 & 1 & -2 \end{bmatrix}$ is	
(a) Symmetric	(b) Skew – symmetric
(c) Singular	(d) Non – Singular

#### Answer: c **Explanation**:

A singular matrix is one which is non-invertible i.e. there is no multiplicative inverse, B, such that the original matrix A × B = I (Identity matrix) A matrix is singular if and only if its determinant is zero.

## **Ouestion 4**

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The cost function of production is given by  $C(x) = \frac{x^3}{2} - 15x^2 + 36x$  where x denotes thee number of items produced. The level of output for which marginal cost is minimum and the level of output for which the average cost is minimum are given by, respectively (a) 10 and 15 (b) 10 and 12

(d) 15 and 10

(b) e(e - 1)

(d)  $e^2(e-1)$ 

(b)  $-4 \le y \le 8$ (d) -5 < y < 5

(a) 10 and 15 (c) 12 and 15 **Answer: a** 

## Question 5

 $\int_{1}^{0} e^{x} \left(\frac{1}{x} - \frac{1}{x^{2}}\right) dx =$ (a)  $e\left(\frac{e}{2} - 2\right)$ (c) a **Answer: a** 

## <u>JULY 2021</u>

<u>Question 1</u>	
If y = 4+9 sin 5x then which holds good?	
(a) $-5 \le y \le 13$	
(c) $0 < y < 1$	
Answer: Options (a)	

## **DEC 2021**

## **Question 1**

Xyz Company has a policy for its recruitment as: it should not recruit more than eight men (x) to three women(y). How can this fact to be express in inequality?

(a)  $3y \ge 8x$ (b)  $3y \le x/8$ (c)  $8y \ge 3x$ (d)  $8y \le 3x$ **Answer: c** Explanation: As per the company's policy, When  $y=3, x \le 8$ It can also be written as: When  $\frac{y}{3} = 1$  ----- Eq (1)  $\frac{x}{8} \le 1$  ..... Eq (2) Now, as per Eq 1, we have  $\frac{y}{z} = 1$ It can also be written as  $1=\frac{y}{3}$ ... Eq 3 Substituting the value of  $1 = \frac{y}{3}$  from eq (3) to Eq(2), we'll get:  $\frac{x}{8} \le \frac{y}{3}$  $3x \le 8y$  $8y \ge 3x$ 

## <u>DEC 2022</u>

## **Question 1**

	Foi	r enq	uiry -	6262969604 6262969699
Th	e solı	ıtior	n of t	the following system of linear equations 2x-5y+4=0 and 2x+y-8 = 0 will be
	a)	(2, -3	)	b) (1,-3)
	c)	(3, 2]	)	d) (-2, 2)
An	swer	: C		
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2x-	-5 <b>v</b> +4	l=0	.(1)	
2x-	-y−8=	:0	(2)	
Iso	late x	fron	n eq	uation (1) and find the value of x and y.
2x-	-5y+4	-=0		
or	2x=5y	7-4		
x=(	5y-4	)/2		
x:	-2	3	8	
y:	0	2	4	
Sin 2x- or y	nilarly ⊦y–8= y=8–2	7, iso =0 2x	late	x from equation (2) and find the values of x and y.
x:	1	2	3	
y:	6	4	2	
Gra Bot So,	aph: th the x=3,y	line 7=2	s int	ersect each other at point (3,2).