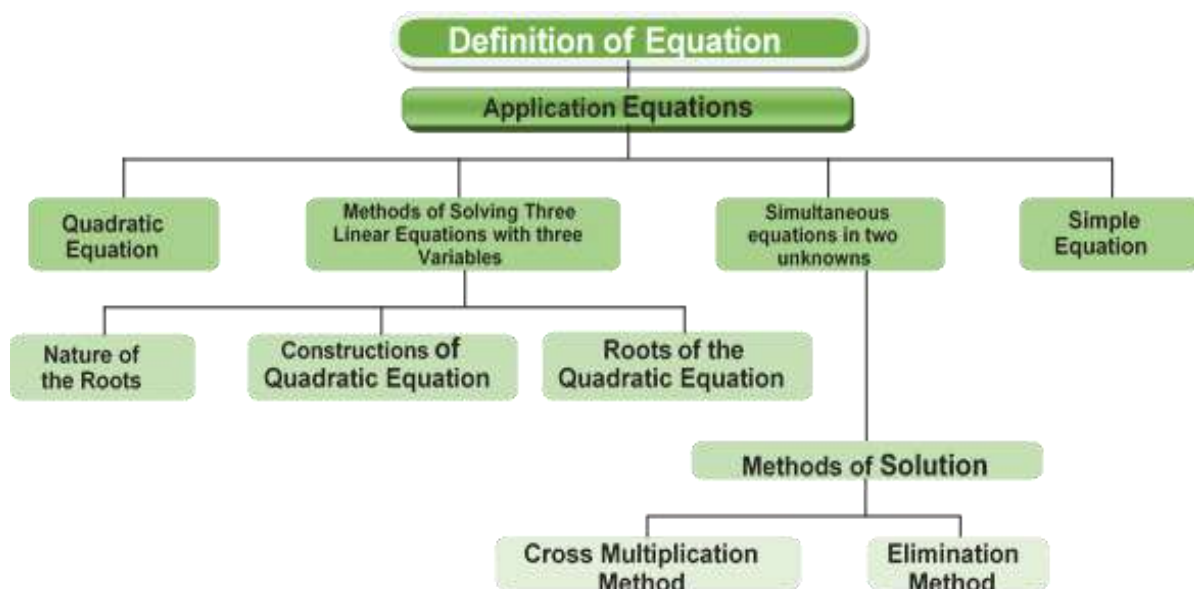


CHAPTER - 2

UNIT I: EQUATIONS



EQUATION	Equation is defined to be a mathematical statement of equality. If the equality is true for certain value of the variable involved, the equation is often called a conditional equation and equality sign '=' is used; while if the equality is true for all values of the variable involved, the equation is called an identity.
TYPES OF EQUATION	<p>Simultaneous Linear Equations: Two or more linear equations involving two or more variables.</p> <p>Quadratic equation: An equation of degree 2 (highest Power of the variable is 2)</p> <p>Cubic Equation: The equation of degree 3</p>
SIMPLE EQUATION	A simple equation in one unknown x is in the form $ax + b = 0$. Where a, b is known constants and $a \neq 0$
SIMULTANEOUS LINEAR EQUATIONS IN TWO UN KNOWNNS	<p>The general form of a linear equations in two unknowns' x and y is $ax + by + c = 0$ where</p> <p>a, b are non-zero coefficients and c is a constant. Two such equations $a_1x + b_1y + c_1 = 0$ and $a_2x + b_2y + c_2 = 0$ form a pair of simultaneous equations in x and y. A value for each unknown which satisfies simultaneously both the equations will give the roots of the equations.</p>

ELIMINATION METHOD	In this method two given linear equations are reduced to a linear equation in one unknown by eliminating one of the unknowns and then solving for the other unknown.
CROSS MULTIPLICATION METHOD	Let two equations be: $a_1x + b_1y + c_1 = 0$ $a_2x + b_2y + c_2 = 0$ $x = \frac{b_1c_2 - b_2c_1}{a_1b_2 - a_2b_1}$ $x = \frac{c_1a_2 - c_2a_1}{a_1b_2 - a_2b_1}$
QUADRATIC EQUATION	An equation of the form $ax^2 + bx + c = 0$ where x is a variable and a, b, c are constants with $a^1 \neq 0$ is called a quadratic equation or equation of the second degree. When $b=0$ the equation is called a pure quadratic equation; when $b \neq 0$ the equation is called an affected quadratic. The roots of a quadratic equation: $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
CONSTRUCT A QUADRATIC EQUATION	$x^2 - (\text{Sum of the roots})x + \text{Product of the roots} = 0$

**Question: 1**

If one root of a equation is $2 + \sqrt{5}$, then the quadratic equation is :

(a) $x^2 + 4x - 1 = 0$

(b) $x^2 - 4x - 1 = 0$

(c) $x^2 + 4x + 1 = 0$

(d) None of these

Answer: b**Explanation:**

One root of the equation is $2 + \sqrt{5}$. So, the next root will be $2 - \sqrt{5}$

$$\therefore x = 2 + \sqrt{5} \text{ and } x = 2 - \sqrt{5}$$

$$\therefore (x - (2 + \sqrt{5}))(x - (2 - \sqrt{5})) = 0$$

$$\therefore (x^2 + (4 - 5) - 2x - \sqrt{5x} - 2x + \sqrt{5x}) = 0$$
$$\therefore x^2 - 4x - 1 = 0 \text{ is the required quadratic equation.}$$

Question:2

The equation of a line which is perpendicular to $5x - 2y = 7$ and passes through the mid - point of line joining $(2, 7)$ and $(-4, 1)$ is:

- (a) $2x - 5y - 18 = 0$ (b) $2x + 5y + 18 = 0$
(c) $2x + 5y - 18 = 0$ (d) None of these

Answer: c

Explanation:

First let us find out the coordinates of the midpoint of the line joining $(2,7)$ and $(-4,1)$ using midpoint formula and let this point be P.

$$P(x, y) = [(x_1+x_2)/2, (y_1+y_2)/2]$$

$$\Rightarrow P(x,y) = [(2-4)/2, (7+1)/2]$$

$$\Rightarrow P(x, y) = (-1, 4)$$

as we have coordinates of P, to form an equation, we need to get the slope of this line.

Since the line passing through P is perpendicular to the line $5x-2y=7$, we can find the required slope by using the formula $M_1 \times M_2 = -1$, where M_1 is the slope of the given line and M_2 is the slope of the line we are supposed to form an equation for.

to find M_1 , let us rewrite the given equation in $y = M_1X + C$ form.

$$5x - 2y = 7$$

$$\Rightarrow -2y = -5x + 7$$

$$\Rightarrow y = -5x/-2 + 7/(-2)$$

$$\Rightarrow y = 5/2 x - 7/2$$

On comparing this equation with $y = M_1X + c$

$$\text{We get } M_1 = 5/2$$

Now using the equation $M_1 \times M_2 = -1$, we get

$$5/2 \times M_2 = -1$$

$$\text{Therefore } M_2 = -2/5$$

Now as we know M_2 and coordinates of P $(-1,4)$ can use slope point form to get the equation

$$\Rightarrow (y - y_1) = M_2(x - x_1)$$

$$\Rightarrow y - 4 = -2/5(x - (-1))$$

$$\Rightarrow y - 4 = -2/5(x + 1)$$

$$\Rightarrow 5(y - 4) = -2(x + 1) \text{ [by cross multiplication]}$$

$$\Rightarrow 5y - 20 = -2x - 2$$

$$\Rightarrow 2x + 5y - 18 = 0 \text{ is the answer}$$

Question:3

Find the positive value of k for which the equations: $x^2 + kx + 64 = 0$ and $x^2 - 8x + k = 0$ will have real roots:

- (a) 12 (b) 16
(c) 18 (d) 22

Answer: b

Explanation:

For real roots, discriminant = $b^2 - 4ac = 0$

$$\text{For } x^2 + kx + 64 = 0$$

$$= k^2 - 4 \times 1 \times 64 = 0$$

$$\begin{aligned}
 &= k^2 - 256 = 0 \\
 &= k^2 = 256 \\
 &= k = 16 \\
 \text{For } x^2 - 8x + k &= 0 \\
 &= (-8)^2 - 4 \times 1 \times k = 0 \\
 &= 64 - 4k = 0 \\
 &= 4k = 64 \\
 &= k = 16 \\
 \text{Hence, } k &= 16
 \end{aligned}$$

Question:4

A man starts his job with a certain monthly salary and earns a fixed increment every year. If his salary was f 1,500 after 4 years of service and 1,800 after 10 years of service, what was his starting salary and what is the annual increment in rupees?

- (a) 1300, 50 (b) 1100,50
 (c) 1500, 30 (d) None

Answer: a

Solution:

Let the starting salary be x and the annual increment be y. Then, $x + 4y = 1500$

$$X + 10y = 1800$$

Subtracting (1) and (2)

$$X + 10y = 1800$$

$$X + 4y = 1500$$

$$6y = 300$$

$$Y = 50$$

Substituting $y = 50$ in (1), we get $x = 1,300$

Therefore, starting salary = $x = 1,300$

Annual increment = $y = 50$.

Question:5

The value of k for which the points (k, 1), (5,5) and (10,7) may be collinear is:

- (a) $k = -5$ (b) $k = 7$
 (c) $k = 9$ (d) $k = 1$

Answer: a

Solution:

The given points are collinear

$$\Rightarrow \begin{vmatrix} 5 & 5 & 1 \\ k & 1 & 1 \\ 10 & 7 & 1 \end{vmatrix} = 0$$

$$\Rightarrow \begin{vmatrix} 5 & 5 & 1 \\ k-5 & -4 & 0 \\ 5 & 2 & 0 \end{vmatrix} = 0 \quad [R_2 \rightarrow R_2 - R_1 \text{ and } R_3 \rightarrow R_3 - R_1]$$

$$\Rightarrow 1 \cdot [2(k-5) + 20] = 0$$

$$\Rightarrow 2k + 10 = 0$$

$$\Rightarrow K = -5$$

Hence, $k = -5$

Question: 6

A man went to the Reserve Bank of India with - 1,000. He asked the cashier to give him Rs.5 and 10 notes only in return. The man got 175 notes in all. Find how many notes of 5 and f 10 did he receive?

- (a) (2, 150) (b) (40, 110)
(c) (150,25) (d) None

Answer: c

Solution:

Let the number of notes of, 5 be x and notes of 10 be y.

$$\text{Then } x + y = 175$$

$$5x + 10y = 1000$$

Solving (1) and (2) simultaneously, we get

$$5x + 5y = 875$$

$$5x + 10y = 1000$$

$$\underline{(-)(-)(-)}$$

$$- 5y = -125$$

$$Y = 25 \quad X = 150$$

Question: 7

If $(2+y\sqrt{3})$ is a root of a quadratic $x^2 + px + q = 0$, then find the value of p and q.

- (a) (4,-1) (b) (4,1)
(c) (-4,1) (d) (2,3)

Answer: c

Solution:

If one of the roots of the quadratic is $2 + \sqrt{3}$, then other root is $2 - \sqrt{3}$

$$\text{Sum of roots} = (2 + \sqrt{3}) + (2 - \sqrt{3}) = 4$$

$$\text{Product of roots} = (2 + \sqrt{3})(2 - \sqrt{3}) = 4 - 3 = 1$$

Required equation is:

$$X^2 - (\text{sum of roots})x + \text{product of roots} = 0$$

$$\text{Or } x^2 - 4x + 1 = 0$$

Now comparing with $x^2 + px + q = 0$

We get, $p = -4$ and $q = 1$

Required answer is (-4,1)

Question: 8

The length of the rectangle is 5 cm more than its breadth if the perimeter of the rectangle is 40 cm find the area of rectangle

- (a) 7.5 cm, 2.5 cm (b) 10 cm, 5cm
(c) 12.5 cm, 7.5 cm (d) 15.5 cm, 10.5cm

Answer: c

Solution:

Let the breadth of the rectangle be x cm.

$$\text{Length} = x + 5 \text{ cm}$$

$$\text{Perimeter} = 2(l + b) =$$

$$2(x + 5 + x) = 4x + 10 \text{ cm}$$

$$4x + 10 = 40$$

$$4x = 30$$

$$X = 30/4 = 7.5$$

So breadth = 7.5 cm; length = 12.5 cm

$$\text{Area} = l \times b = 12.5 \times 7.5 = 93.75$$

$$\text{So area} = 93.75\text{cm}^2$$

Question: 9

A straight line of $x = 15$ is

- (a) Parallel to y axis
(b) Parallel to x axis
(c) A diagonal line
(d) Passes through origin

Answer: a

Solution:

A straight line $x = 15$ is parallel to y axis.

The equation clearly depicts that the line passes through the point P (15 , 0).

Question: 10

The point of intersection of the lines $2x - 5y = 6$ and $x + y = 3$

- (a) (0,3)
(b) (3 , 0)
(c) (3,3)
(d) (0, 0)

Answer: b

Solution:

$$2x - 5y = 6 \text{ ---- (1)}$$

$$x + y = 3 \text{ (2)}$$

Multiplying eq. (2) by 5 for make be co - efficients of eq. (1) and eq. (2) same, we get :-

$$5x + 5y = 15 \text{ (3)}$$

Adding eq. (1) and eq. (3)

$$2x - 5y = 6$$

$$5x + 5y = 15$$

$$\hline 7x = 21$$

$$x = \frac{21}{7}$$

$$x = 3$$

Substituting the value of x in eq (1)

$$2x - 5y = 6$$

$$2 \times 3 - 5y = 6$$

$$6 - 5y = 6$$

$$5y = 6 - 6$$

$$y = 0$$

Point of intersection is (3, 0).

Question: 11

Find the equation of the line passing through the point (1, 1) and parallel to the line $3x + 5y + 17 = 0$

- (a) $3x + 5y + 8 = 0$
(b) $5x + 3y + 8 = 0$
(c) $5x + 3y - 8 = 0$
(d) $3x + 5y - 8 = 0$

Answer: d

Solution:

Let the equation be $3x + 5y + k = 0$. This equation passes through the point 1(1, 1).

Therefore, substituting (1, 1). Therefore, substituting (1,1) in the equation, we get : $3x$

$$+ 5y + k = 0$$

$$3 \times 1 + 5 \times 1 + k = 0$$

$$3 + 5 + k = 0.$$

$$K = -8$$

So, the equation of the straight line is $3x + 5y - 8 = 0$.

Question: 12

If one root of the equation $x^2 - 3x + k = 0$ is 2, then value of k will be:

- (a) 1 (b) 0
(c) 2 (d) 10

Answer: c

Solution:

$$X^2 - 3x + k = 0$$

$$\text{One root} = 2$$

Putting $x = 2$, we get

$$(2)^2 - 3(2) + k = 0 \Rightarrow 4 - 6 + k = 0$$

$$K = 2$$

Question: 13

If $|x - 2| + |x - 3| = 7$ then, 'x' will be equal to

- (a) 6 (b) -1
(c) 6 and -1 (d) none

Answer: a

Solution:

$$\text{If } |x - 2| + |x - 3| = 7$$

$$\text{If } x - 2 \geq 0 \text{ and } x - 3 \geq 0$$

$$(x - 2) + (x - 3) = 7$$

$$x - 2 + x - 3 = 7$$

$$2x = 7 + 2 + 3$$

$$2x = 12 \Rightarrow x = 6$$

Question: 14

If thrice of A's age 6 years ago be subtracted from twice his present age, the result would be equal to his present age. Find A's present age.

- (a) 9 (b) 10
(c) 11 (d) 12

Answer: a

Solution:

Let x years be A's present age by the question

$$2x - 3(x - 6) = x$$

$$\text{Or } 2x - 3x + 18 = x$$

$$\text{Or } -x + 18 = x$$

$$\text{Or } 2x = 18$$

$$\text{Or } x = 9$$

A's present age is 9 years.

Question: 15

A number consist of two digits the digit in the ten's place is twice the digit in the unit's place. If 18 be subtracted from the number, the digits are reversed. Find the number.

- (a) 40 (b) 42

(c) 39

(d) 21

Answer: b

Solution:

Let x be the digit in the unit's place .so the digit in the ten's Place is 2x. Thus the number becomes $10(2x) + x$. By the question

$$20x + x - 18 = 10x + 2x$$

$$\text{Or } 21x - 18 = 12x$$

$$\text{Or } 9x = 18$$

$$\text{Or } x = 2$$

So the required number is $10 (2 \times 2) + 2 = 42$

Question: 16

For a certain commodity the demand 'd' in kg, for a price 'p' in rupees per kg, is $d = 100(10 - p)$. The supply equation giving the supply s in kg. for a price p in rupees per kg . is $s = 75(p - 3)$. The market price is such at which demand equals supply. Find the market price and quantity that will be bought and sold.

(a) 230

(b) 300

(c) 600

(d) 390

Answer: b

Solution:

Given $d = 100(10 - p)$ and $s = 75 (p - 3)$

Since the market price is such that demand (d) = supply

(s)

We have $100(10 - p)$ and $s = 75 (p - 3)$

$$\text{Or } 1000 - 100p = 75p - 225$$

$$1000 + 225 = 75p + 100p$$

$$1225 = 175p$$

$$P = 7$$

So, market price of the commodity is 7 per kg.

The required quantity bought = $100 (10-7) = 300$ kg.

And the quantity sold = $75(7-3) = 300$ kg.

Question: 17

The denominator of a fraction exceeds the numerator by 5 and if 3 be added to both the fraction becomes $\frac{3}{4}$, find the fraction.

(a) $\frac{11}{17}$

(b) $\frac{12}{17}$

(c) $\frac{13}{17}$

(d) $\frac{14}{18}$

Answer: b

Solution:

Let x be the numerator and the fraction be $\frac{x}{x+5}$

By the question $\frac{x+3}{x+5+3} = \frac{3}{4}$ or

$$4x + 12 = 3x + 24 \text{ or } x = 12$$

The required fraction is $\frac{12}{17}$

Question:18

Solve $2x + 5y = 9$ and $3x - y = 5$.

(a) $x = 2, y = 1$

(b) $x = 2, y = 2$

(c) $x = 1, y = 1$

(d) $x = 2, y = 0.$

Answer: a

Solution:

$2x + 5y = 9$ (i)

$3x - y = 5$ (ii)

By making (i) $\times 1, 2x + 5y = 9$

and by making (ii) $\times 5, 15x - 5y = 25$

Adding $17x = 34$ or $x = 2$. Subtracting this value of x in (i) i.e. $5y = 9 - 2x$ we find:

$5y = 9 - 4 = 5$

$Y = 1$

$X = 2, y = 1$

Question: 19

The age of a man three times the sum of the ages of his two sons and 5 years hence his age will be double the sum of their ages. Find the present age of the man?

(a) 40 years

(b) 41years

(c) 55 years

(d) 45 years

Answer: d

Solution:

Let x years be the present age of the man and sum of the present ages of the two sons be y years.

By the condition $x = 3y$ (i)

And $x + 5 = 2(y + 5 + 5)$ (ii)

From (i) & (ii) $3y + 5 = 2(y + 10)$

Or $3y + 5 = 2y + 20$

Or $3y - 2y = 20 - 5$

Or $y = 15$

$X = 3 \times y = 3 \times 15 = 45$

Hence the present age of the main is 45 years

Question: 20

Examine the nature of the roots of the following equations $x^2 - 8x + 16 = 0$

(a) roots are real and equal

(b) roots are real, rational and unequal

(c) roots are imaginary and unequal

(d) roots are real irrational and unequal

Answer: a

Solution:

$a = 1, b = -8, c = 16$

$b^2 - 4ac = (-8)^2 - 4.1.16 = 64 - 64 = 0$

The roots are real and equal.

Question: 21

Two times a number, decreased by 12 equals three times the number, decreased by 15. Which is the number?

(a) 3

(b) -62

(b) -64

(d) 6

Answer: a

Solution:

Let us denote the number with n. We rewrite the problem as $2n-12=3n-15$. We subtract $2n$ from both sides and get $-12=n-15$. Then we add 15 to both sides in order to get $n=3$.

Question: 22

The roots of a quadratic equation:

- (a) $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ (b) $\frac{b \pm \sqrt{b^2 - 4ac}}{2a}$
 (c) Either a or b (d) None

Answer: a

Solution:

The nature of the roots α and β of equation $ax^2+bx+c=0$ depends on the quantity or expression $(b^2 - 4ac)$ under the square root signHence the expression $(b^2 - 4ac)$ is called the discriminant of the quadratic equation $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

Question:23

Which of the following is correct?

- I. If $b^2-4ac = 0$ the roots are real and equal;
- II. If $b^2-4ac > 0$ then the roots are imaginary;
- III. If $b^2-4ac < 0$ then the roots are equal;
- IV. If b^2-4ac is a perfect square (0) the roots are real, rational and unequal
- V. If $b^2-4ac > 0$ but not a perfect square the roots are real, irrational and unequal.

- (a) All the correct (b) ii & iii
 (c) all are correct expect ii & iii (d) i& iii & iv is correct

Answer: c

Solution:

- I. If $b^2-4ac = 0$ the roots are real and equal
 - II. If $b^2-4ac > 0$ then the roots are real and unequal (or distinct);
 - III. If $b^2-4ac < 0$ then the roots are imaginary;
 - IV. If b^2-4ac is a perfect square (0) the roots are real, rational and unequal (distinct);
 - v. If $b^2-4ac > 0$ but not a perfect square the roots are real, irrational and unequal
- Since b^2-4ac discriminates the roots b^2-4ac is called the discriminant in the equations $ax^2 + bx + c = 0$ as it actually discriminates between the roots.

Question: 24

Find the roots of the quadratic equation: $x^2 + 2x - 15 = 0$?

- (a) 5, 3 (b) 3,-5
 (c) -3 ,5 (d) -3, -5

Answer: b

Solution:

$$X^2 + 5x - 3x - 15 = 0$$

$$X(x + 5) - 3(x + 5) = 0$$

$$(x - 3)(x + 5) = 0$$

$$\Rightarrow x = 3 \text{ or } x = -5.$$

Question: 25

The sum of the squares of two consecutive positive integers exceeds their product by 91. Find the integers?

- (a) 9, 10 (b) 10, 11
(c) 11, 12 (d) 12, 13

Answer: a

Solution:

Let the two consecutive positive integers be x and $x + 1$

$$X^2 + (x + 1)^2 - x(x + 1) = 91$$

$$X^2 + x - 90 = 0$$

$$(x + 10)(x - 9) = 0 \Rightarrow x = -10 \text{ or } 9.$$

As x is positive $x = 9$

Hence the two consecutive positive integers are 9 and 10.

Question: 26

A number is equal to 4 times this number less 75. What is the number?

- (a) 15 (b) 35
(c) 25 (d) 20

Answer: c

Solution:

Let us denote the number with n . The problem can be rewritten as $n=4n-75$. By subtracting n from both sides, we get $3n-75=0$ Now we divide both sides by 3 to get $n-25=0$, or $n=25$.

Question: 27

If $\sqrt{3 - 2x} + \sqrt{7 + 2x} = 4$, then find the positive value of x ?

- (a) -3, 1 (b) 3, -1
(c) 3, -2 (d) 3, 2

Answer: a

Solution:

$$\text{Given, } \sqrt{3 - 2x} + \sqrt{7 + 2x} = 4$$

$$\text{Or, } \sqrt{3 - 2x} = 4 - \sqrt{7 + 2x}$$

Squaring on both sides, we get

$$(\sqrt{3 - 2x})^2 = (4 - \sqrt{7 + 2x})^2$$

$$\rightarrow 3 - 2x = 16 + 7 + 2x - 8\sqrt{7 + 2x}$$

$$\rightarrow 4x + 20 = 8\sqrt{7 + 2x}$$

$$\rightarrow X + 5 = 2\sqrt{7 + 2x}$$

Again squaring on both sides, we get

$$(x + 5)^2 = (2\sqrt{7 + 2x})^2$$

$$\rightarrow x^2 + 10x + 25 = 4(7 + 2x)$$

$$\rightarrow x^2 + 10x + 25 = 28 + 8x$$

$$\rightarrow x^2 + 2x - 3 = 0$$

$$\rightarrow x^2 + 3x - x - 3 = 0$$

$$\rightarrow (x + 3)(x - 1) = 0$$

$$\rightarrow X = -3 \text{ or } x = 1$$

Possible value of $x = 1, -3$

Hence, A is the correct option.

Question: 28

I. $a^2 + 11a + 30 = 0$

II. $b^2 + 6b + 5 = 0$ to solve both the equations to find the values of a and b?

(a) If $a < b$

(b) If $a \leq b$

(c) If the relationship between a and b cannot be established

(d) If $a > b$

Answer: b

Solution:

(i) $(a+6)(a+5) = 0$

$a = -6, -5$

(ii) $(b+5)(b+1) = 0$

$b = -5, -1 \Rightarrow a \leq b$

Question: 29

A number is equal to 7 times itself minus 18. Which is the number?

(a) -3

(b) 3

(c) 2

(d) -2

Answer: b

Solution:

The statement is equivalent to the following equation:

$X = 7x - 18x$

$18 = 7x - x$

$6x = 18$

$X = 3$

Question: 30

If a and b are the roots of the equations $x^2 - 9x + 20 = 0$, find the value of $a^2 + b^2 + ab$

(a) -21

(b) 1

(c) 61

(d) 21

Answer: c.

Solution:

$a^2 + b^2 + ab = a^2 + b^2 + 2ab - ab$

i.e., $(a + b)^2 - ab$

from $x^2 - 9x + 20 = 0$, we have

$a + b = 9$ and $ab = 20$. Hence the value of required expression $(9)^2 - 20 = 61$.

Question: 31

If $a + b = 29$, $b + c = 45$, $a + c = 44$. Find $a + b + c$?

(a) -21

(b) 1

(c) 59

(d) 118

Answer: c

Solution:

$(a + b) + (b + c) + (a + c) = 29 + 45 + 44$

$a + b + b + c + a + c = 118$

$2a + 2b + 2c = 118$

$2(a + b + c) = 118$

$a + b + c = 59$

Question: 32

A simple equation in one unknown x is in form $ax + b = 0$. Is true or not?

- (a) true (b) false
(c) not sure (d) partial

Answer: a

Solution:

A simple equation in one unknown x is in the form $ax + b = 0$. Where a, b are known constants and $a \neq 0$

Question: 33

If both the roots of $k(6x^3 + 3) + rx + 2x^2 - 1 = 0$ and $6k(2x^2 + 1) + px + 4x^2 - 2 = 0$ are common, then $2r - p$ is equal to

- (a) -1 (b) 0
(c) 1 (d) 2

Answer: b

Solution:

The two equations can be written as

$$x^2(6k + 2) + rx + (3k - 1) = 0 \quad \dots (1)$$

$$\text{and } x^2(12k + 4) + px + (6k - 2) = 0 \quad \dots (2)$$

Divide by 2

$$\therefore x^2(6k + 2) + \frac{p}{2}x + (3k - 1) = 0 \quad \dots (3)$$

Comparing (1) and (3), we get $r = \frac{p}{2}$

$$\therefore 2r - p = 0.$$

Question: 34

If a root of the equations $x^2 + px + q = 0$ and $x^2 + \alpha x + \beta = 0$ is common then its value will be (where $p \neq \alpha$ and $q \neq \beta$) Condition for common roots is $\frac{12k+4}{6k+2} = \frac{p}{e}$

- (a) $\frac{q-\beta}{\alpha-p}$ (b) $\frac{p\beta-\alpha q}{q-\beta}$
(c) $\frac{q-\beta}{\alpha-p} - \frac{p\beta-\alpha q}{q-\beta}$ (d) None

Answer: b

Solution:

Let the common root be y . Then $y^2 + py + q = 0$ and $y^2 + \alpha y + \beta = 0$ on solving by cross multiplication, we have $\frac{y^2}{p\beta - q\alpha} = \frac{y}{q - \beta} = \frac{1}{\alpha - p} \implies y = \frac{q - \beta}{\alpha - p}$ and $\frac{y^2}{y} = y = \frac{p\beta - q\alpha}{q - \beta}$

Question: 35.

If the two equations $x^2 - cx + d = 0$ and $x^2 - ax + b = 0$ have one common root and the second has equal roots then $2(b + d) =$

- (a) $a + c$ (b) 0
(c) ac (d) $-ac$

Answer: c

Solution:

Given quadratic equations

$$x^2 - cx + d = 0 \quad \dots (1)$$

Let α, β be the roots of equation (1)

$$x^2 - ax + b = 0 \quad \dots (2)$$

Let α, α be the roots of equation (2)

$$2\alpha = a$$

$$\alpha = \frac{a}{2}$$

$$\text{Also, } \alpha^2 = b$$

Since, α is a root of (1),

$$\alpha^2 - c\alpha + d = 0$$

$$b + d = \frac{ac}{2}$$

$$2(b + d) = ac$$

Question: 36.

If $x^2 - hx - 21 = 0, x^2 - 3hx + 35 = 0 (h > 0)$ has a common root then, the value of h is equal to

- (a) 1 (b) 2
(c) 3 (d) 4

Answer: d

Solution:

Subtracting we get $2hx = 56$ or $hx = 28$ putting in any,

$$x^2 - 3(28) + 35 = 0$$

$$x^2 - 84 + 35 = 0$$

$$x^2 = 49$$

$$x = 7$$

$$hx = 28$$

$$h = 4$$

Question:37

If Every pair of the equations $x^2 + px + qr = 0, x^2 + qx + rp = 0, x^2 + rx + pq = 0$ have a common root. Then the sum of three common roots is

- (a) $\frac{-(p+q+r)}{2}$ (b) $\frac{-(p-q+r)}{2}$
(c) $-(p+q+r)$ (d) $-p+q+r$

Answer: a

Solution:

Let the roots be $(\alpha, \beta), (\beta, \lambda)$ and (λ, α) respectively

$\alpha + \beta = -p, \beta + \lambda = -q, \lambda + \alpha = -r$ adding all, we get $\sum\alpha = -(p + q + r) / 2$ etc.

Question: 38

If the equation $x^2 + px + q = 0$ and $x^2 + qx + p = 0$, have a common root, then $p + q + 1$

- (a) 0 (b) 1
(c) 2 (d) -1

Answer: a

Solution:

Let α is the common root, so $\alpha^2 + p\alpha + q = 0 \dots(i)$ and $\alpha^2 + q\alpha + p = 0 \dots (ii)$

From (i) - (ii), $\Rightarrow (p - q)\alpha + (q - p) = 0 \Rightarrow \alpha = 1$ put the value of α in (i), $p + q + 1 = 0$

Question: 39

If $x^2 + \alpha x + 10 = 0$ and $x^2 + bx - 10 = 0$ have a common root, then, $a^2 - b^2$ is equal to

- (a) 10 (b) 20
(c) 30 (d) 40

Answer: d

Solution:

Let α be a common root, then $\alpha^2 + \alpha\alpha + 10 = 0$ (i) and $\alpha^2 + b\alpha - 10 = 0$

?... (ii) form (i) - (ii), $(a - b)\alpha + 20 = 0 \Rightarrow \alpha = -\frac{20}{a-b}$ substituting the value of α in (i).

We get $\left(-\frac{20}{a-b}\right)^2 + a\left(-\frac{20}{a-b}\right) + 10 = 0 \Rightarrow 400 - 20a(a-b) + 10(a-b)^2 = 0$
 $\Rightarrow 40 - 2a^2 + 2ab + a^2 + b^2 - 2ab = 0 \Rightarrow a^2 - b^2 = 40.$

Question: 40

$x^2 - 11x + a$ and $x^2 - 14x + 2a$ will have a common factor, if $a = 42$

- (a) 24 (b) 0, 24
(c) 3, 24 (d) 0, 3

Answer: b

Solution:

Expression are $x^2 - 11x + a$ and $x^2 - 14x + 2a$ will have a common factor, then

$\Rightarrow \frac{x^2}{-22a+14a} = \frac{x}{a-2a} = \frac{1}{-14+11} \Rightarrow \frac{x^2}{-8a} = \frac{1}{-3} \Rightarrow x^2 = \frac{8a}{3}$ and $x = \frac{a}{3}$

$\left(\frac{a}{3}\right)^2 = \frac{8a}{3} \Rightarrow \frac{a^2}{9} = \frac{8a}{3}$ $pa = 0, 24$. Trick we can check by putting the values of a from the options.

Question: 41

If x be real, then the minimum value of $x^2 - 8x + 16$ is.

- (a) -1 (b) 0
(c) 1 (d) 2

Answer: c

Solution:

$[x^2 - 8x + 16]$ since x is real, so $(x - 4)^2$ is always positive and its least value is 0 and so the minimum value of given expression is 1.

Question: 42

Solve the equations $8+2(x-4) = 16$

- (a) -1 (b) 8
(c) 10 (d) 2

Answer: b

Solution:

First, we removed the parentheses and get $8 + 2(x - 4) = 16$, or $8 + 2x - 8 = 16$, which gives us $2x=16$. We divide by 2 in order to get $x = 8$.

Question: 43

Solve the equation: $x^3 + 10 = 2x$ $x^3 + 10 = 2x$.

- (a) 6 (b) 8
(c) 10 (d) 2

Answer: a

Solution:

We multiply both sides by 3 to get free of the denominator. This gives us $x+3-10=3.2x$, or $x+30=6x$ by subtracting x from both sides we get $30=5x$. Dividing both sides by 5 gives us the answer, $x = 6$.

Question: 44

$$2(3x - 7) + 4(3x+2) = 6(5x+9)$$

- (a) 6 (b) -5
(c) 10 (d) 2

Answer: b

Solution:

$$\begin{aligned} 2(3x-7)+4(3x+2) &= 6(5x+9) \\ 6x - 14 + 12x + 8 &= 30x + 54 \\ 6x + 12x - 30x &= 14 - 8 + 54 \\ -12x &= 60 \\ X = 60 \div (-12) &= -5 \end{aligned}$$

Question: 45

Find the solution x to the equations $x^3-x^4=2 \times 3-x^4=2$.

- (a) 69 (b) 51
(c) 0 (d) 24

Answer: d

Solution:

We first find the lowest common multiple of 4 and 3. It is 12. Multiplying both sides by 12 gives us $x^3 \cdot 12 - x^4 \cdot 12 = 2 \cdot 12 \times 3 - x^4 \cdot 12 = 2 \cdot 12$, or $4x - 3x = 24$, which means that $x = 24$.

Question: 46

A number, multiplied by 5, equals itself minus 48. Which is the number

- (a) 6 (b) -5
(c) 0 (d) -12

Answer: d

Solution:

$$\begin{aligned} 5x &= x - 48 \\ 4x &= -48 \\ X &= -12 \end{aligned}$$

PAST EXAMINATION QUESTIONS:

MAY 2018

Question: 1

The value of K for which the points $(k, 1)$, $(5,5)$ and $(10,7)$ may be collinear is

- (a) $k = -5$ (b) $k = 7$
(c) $k = 9$ (d) $k = 1$

Answer: a

Solution:

Let $A(x_1, y_1) = (K, 1)$,
 $B(x_2, y_2) = (5, 5)$, and
 $C(x_3, y_3) = (10, 7)$ are three collinear points

Area of triangle ABC = 0

$$\frac{1}{2} |x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)| = 0$$

$$|x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)| = 0$$

$$\Rightarrow |k(5 - 7) + 5(7 - 1) + 10(1 - 5)| = 0$$

$$\Rightarrow |-2k + 5 \times 6 + 10(-4)| = 0$$

$$\Rightarrow |-2k + 30 - 40| = 0$$

$$\Rightarrow |-2k + 10| = 0$$

$$\Rightarrow -2k = 10$$

$$\Rightarrow K = \frac{10}{-2}$$

$$\Rightarrow K = -5$$

Therefore,

Value of $k = -5$

Question: 2

If $\alpha + \beta = -2$ and $\alpha\beta = -3$, then α, β are two roots of the equations, which is:

(a) $x^2 - 2x - 3 = 0$

(b) $x^2 + 2x - 3 = 0$

(c) $x^2 + 2x + 3 = 0$

(d) $x^2 - 2x + 3 = 0$

Answer: b

Solution:

If $\alpha + \beta = -2$

Q.E. is

$$X^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$X^2 - (-2)x + (-3) = 0$$

$$X^2 + 2x - 3 = 0$$

Question: 3

If $2^{x+y} = 2^{2x-y} = \sqrt{8}$, then the respective values of x and y are

(a) $1, \frac{1}{2}$

(b) $\frac{1}{2}, 1$

(c) $\frac{1}{2}, \frac{1}{2}$

(d) None

Answer: a

Solution:

$$2^{x+y} = 2^{2x-y} = \sqrt{8}$$

$$2^{x+y} = \sqrt{8} \quad \text{and} \quad 2^{2x-y} = \sqrt{8}$$

$$2^{x+y} = (2^3)^{1/2} \quad 2^{2x-y} = (2^3)^{1/2}$$

$$2^{x+y} = 2^{3/2} \quad 2^{2x-y} = 2^{3/2}$$

On Comparing

$$x + y = 3/2 \quad \text{----- (1)}$$

Add: (1) & (2)

$$x + y = \frac{3}{2} \quad \text{----- (1)}$$

$$2x - y = \frac{3}{2} \quad \text{----- (2)}$$

$$3x = 3$$

$$x = 1$$

Putting $x = 1$ in equation (1)

$$X + y = \frac{3}{2}$$

$$1 + y = \frac{3}{2}$$

$$Y = \frac{1}{2}$$

$$X = 1, y = \frac{1}{2}$$

Question: 4

The triangle formed by lines $x+2y=3$, $2x-y=1$ and $y=0$ is

- (a) Right angled (b) Equilateral
(c) Isosceles (d) None

Answer: a

Solution:

Given Equation

$$X + 2y = 3 \text{ ----- (1)}$$

$$2x - y = 1 \text{ ----- (2)}$$

$$Y = 0 \text{ ----- (3)}$$

Slope of line (1) is

$$m_1 = \frac{\text{Coefficient of } x}{\text{coefficient of } y} = \frac{-1}{2}$$

Slope of line (2) is

$$m_2 = \frac{\text{coefficient of } x}{\text{coefficient of } y} = \frac{-2}{-1} = 2$$

$$m_1 \times m_2 = -\frac{1}{2} \times 2$$

$$m_1 \times m_2 = -1$$

Both lines are 1 or to each triangle are also perpendicular.

Question: 5

If $\frac{3}{x+y} + \frac{2}{x-y} = -1$ and $\frac{1}{x+y} - \frac{1}{x-y} = \frac{4}{3}$ then x, y is:

- (a) (2, 1) (b) (-1, 2)
(c) (1, 2) (d) None

Answer: c

Solution:

$$\text{If } \frac{3}{x+y} + \frac{2}{x-y} = -1 \text{ and } \frac{1}{x+y} - \frac{1}{x-y} = \frac{4}{3}$$

By hits and trial (1, 2) satisfied both equation so answer is (1, 2)

Question: 6

If the sides of an equilateral triangle are shortened by 3 units, 4 units and 5 units respectively and a right triangle is formed then the sides of equilateral triangle is:

- (a) 6 units (b) 7 units
(c) 8 units (d) 10units

Answer: c

Solution:

Let the side of equilateral triangle is x

In $\triangle ABC$

$$\begin{aligned}(\text{hypo})^2 &= (\text{Base})^2 + (\text{per})^2 \\(x-3)^2 &= (x-4)^2 + (x-5)^2 \\X^2 + 9 - 6x &= x^2 + 16 - 8x + x^2 + 25 - 10x \\X^2 - 18x + 41 + 6x - 9 &= 0 \\X^2 - 12x + 32 &= 0 \\X^2 - 8x - 4x + 32 &= 0 \\X(x-8) - 4(x-8) &= 0 \\(x-8)(x-4) &= 0 \\X-8=0 \text{ if } x-4=0 \\X=8 \text{ and } x=4 \text{ Impossible side of the triangle is } 8\end{aligned}$$

Question: 7

IF α, β are the roots of equation $x^2 + x + 5 = 0$ then $\frac{\alpha^2}{\beta} + \frac{\beta^2}{\alpha}$ is equal to

- (a) $\frac{16}{5}$ (b) 2
(c) 3 (d) $\frac{14}{5}$

Answer: d

Solution:

Given equation:

$$x^2 + x + 5 = 0$$

$$a=1, b=1, c=5$$

if α & β are root of equation

$$\alpha + \beta = \frac{-b}{a} = \frac{-1}{1} = -1$$

$$\alpha\beta = \frac{c}{a} = \frac{5}{1} = 5$$

$$\frac{\alpha^2}{\beta} + \frac{\beta^2}{\alpha} = \frac{\alpha^3 + \beta^3}{\alpha\beta} = \frac{(\alpha + \beta)^3 - 3\alpha\beta(\alpha + \beta)}{\alpha\beta}$$

$$\frac{(-1)^3 - 3 \times 5 \times (-1)}{5}$$

$$\frac{-1 + 15}{5} = \frac{14}{5}$$

NOV 2018

Question: 1

Let α and β be the roots of $x^2 + 7x + 12 = 0$. Then the value of $\frac{\alpha^2}{\beta} + \frac{\beta^2}{\alpha}$ will be

- (a) $\frac{7}{12} + \frac{12}{7}$ (b) $\frac{49}{144} + \frac{144}{49}$
(c) $-\frac{91}{21}$ (d) None

Answer: c

Solution:

If α & β are the roots of equation

$$X^2 + 7x + 12 = 0$$

$$\text{Then } \alpha + \beta = \frac{-b}{a} = \frac{-7}{1} = -7$$

$$\alpha \times \beta = \frac{c}{a} = \frac{12}{1} = 12$$

$$\frac{\alpha^2}{\beta} + \frac{\beta^2}{\alpha} = \frac{\alpha^3 + \beta^3}{\alpha\beta}$$

$$\frac{(\alpha+\beta)^3 - 3\alpha\beta(\alpha+\beta)}{\alpha\beta} = \frac{(-7)^3 - 3 \times 12(-7)}{12}$$

$$\frac{-343+252}{12} = \frac{-91}{12}$$

Question: 2

When two roots of quadratic equation are $\alpha, \frac{1}{\alpha}$ then what will be the quadratic equation:

- (a) $ax^2 - (a^2 + 1)x + a = 0$ (b) $ax^2 - (a^2x + 1) = 0$
 (c) $ax^2 - (a^2 + 1)x + 1 = 0$ (d) None

Answer: a

Solution:

If roots of Q.E. are $\alpha, \frac{1}{\alpha}$ then $\alpha + \frac{1}{\alpha} = 1$, $\alpha \cdot \frac{1}{\alpha} = 1$

Sum of roots (S) = $\alpha + \frac{1}{\alpha}$

$$= \alpha + \frac{1}{\alpha} = 1$$

Product of Roots (P) = $\alpha \cdot \frac{1}{\alpha}$

$$= \alpha \cdot \frac{1}{\alpha} = 1$$

Q.E. is given by

$$X^2 - 5x + p = 0$$

$$X^2 - \left[\frac{a^2+1}{a}\right]x + 1 = 0$$

$$ax^2 - (a^2 + 1)x + a = 0$$

MAY 2019

Question: 1

Find the condition that one root is double the other of $ax^2 + bx + c = 0$

- (a) $2b^2 = 3ac$ (b) $b^2 = 3ac$
 (c) $2b^2 = 9ac$ (d) $2b^2 > 9ac$

Answer: c

Explanation:

Let m be the one root of the given equation

Then the other root will be 2m.

Then $m + 2m = -b/a$ or, $3m = -b/a$ or, $m = -b/3a$.

Now, $m(2m) = c/a$ or, $(-b/3a)(-2b/3a) = c/a$ or, $2b^2 = 9ac$.

Question: 2

$$\begin{pmatrix} x+y & 1 \\ 1 & x-y \end{pmatrix} + \begin{pmatrix} 2 & 3 \\ 2 & -4 \end{pmatrix} = \begin{pmatrix} 12 & 4 \\ 3 & 0 \end{pmatrix} \text{ then}$$

- (a) $x = 7, y = -3$ (b) $x = -7, y = -3$
 (c) $x = -7, y = 3$ (d) $x = 7, y = 3$

Answer: d

Explanation:

By option method, Taking D as option

$$\begin{pmatrix} 7+3 & 1 \\ 1 & 7-3 \end{pmatrix} + \begin{pmatrix} 2 & 3 \\ 2 & -4 \end{pmatrix}$$

$$\begin{pmatrix} 10 & 1 \\ 1 & 4 \end{pmatrix} + \begin{pmatrix} 2 & 3 \\ 2 & -4 \end{pmatrix} = \begin{pmatrix} 12 & 4 \\ 3 & 0 \end{pmatrix}$$

NOV 2019

Question: 1

Roots of the equation $x^3+9x^2-x-9=0$

(a) 1, 2, 3

(b) 1, -1, -9

(c) 2, 3, -9

(d) 1, 3, 9

Answer:(b)

Solution:

$$x^3 + 9x^2 - x - 9 = 0$$

By factorization method

$$X^2(x+9)-1(x+9) = 0$$

$$(x^2 - 1) (x + 9) = 0$$

$$(x + 1) (x - 1) (x - 9) = 0$$

$$(x + 1) = 0 \quad (x - 1) = 0$$

$$X = -1$$

$$x = 1$$

$$[a^2-b^2=(a+b)(a-b)]$$

$$(x+9) = 0$$

$$x = -9$$

Question: 2

$$\frac{2x+5}{10} + \frac{3x+10}{15} = 5$$

(a) 10.58

(b) 9.58

(c) 9.5

(d) None

Answer:(b)

Solution:

$$\frac{2x+5}{10} + \frac{3x+10}{15} = 5$$

$$\frac{15(2x+5)+10(3x+10)}{150} = 5$$

$$30x + 75 + 30x + 100 = 750$$

$$60x = 575$$

$$X = \frac{575}{60}$$

$$X = 9.58(\text{approx})$$

Question: 3

Find value of $x^2-10x+1$ if $x = \frac{1}{5-2\sqrt{6}}$

(a) 25

(b) 1

(c) 0

(d) 49

Answer:(c)

Solution:

$$x^2 - 10x + 1 = 0 \Rightarrow \text{give equation}$$

$$X = \frac{1}{5-2\sqrt{6}}$$

Multiplying by conjugate

$$X = \frac{1}{5-2\sqrt{6}} \times \frac{5+2\sqrt{6}}{5+2\sqrt{6}}$$

$$X = \frac{5+2\sqrt{6}}{(5)-(2\sqrt{6})} (a+b)(a-b) = a^2 - b^2$$

$$X = \frac{5+2\sqrt{6}}{25-24}$$

$$\begin{aligned}
 X &= 5 + 2\sqrt{6} \\
 X^2 &= (5 + 2\sqrt{6})^2 = a^2 + b^2 + 2ab \\
 &= 25 + 24 + 2 \times 5 \times 2\sqrt{6} \\
 X^2 &= 49 + 20\sqrt{6} \quad \text{----- (1)} \\
 10x &= 10(5 + 2\sqrt{6}) = 50 + 20\sqrt{6} \quad \text{----- (2)} \\
 X^2 - 10x + 1 & \\
 &= 49 + 20\sqrt{6} - 50 - 20\sqrt{6} + 1 \quad \{\text{from equation ---- (1) \& (2)}\} \\
 &= 0 \\
 \text{So, } x^2 - 10x + 1 &= 0
 \end{aligned}$$

Question: 4

Find the value of k in $3x^2 - 2kx + 5 = 0$

If $x = 2$

- | | |
|----------|-----------|
| (a) 15 | (b) -7/14 |
| (c) 17/4 | (d) -4/17 |

Answer: (c)

Solution:

$3x^2 - 2kx + 5 = 0$ { give equation } as it is given $x = 2$

Then put in place of $x = '2'$

$$3 \times (2)^2 - 2k(2) + 5 = 0$$

$$3 \times 4 - 2k(2) + 5 = 0$$

$$12 - 4k + 5 = 0$$

$$-4k = -12 - 5$$

$$-4k = -17$$

$$K = \frac{17}{4}$$

DEC 2020

Question 1

If $2x^2 - (a + 6)2x + 12a = 0$ then roots are

- | | |
|------------------------|------------|
| (a) 4 & a ² | (b) 6 & a |
| (c) 3 & 2a | (d) 6 & 3a |

Answer: b

Explanation:

Given:

$$2x^2 - (a + 6)2x + 12a = 0$$

$$\Rightarrow 2x^2 - 2ax - 12x + 12a = 0$$

$$\Rightarrow 2x(x - a) - 12(x - a) = 0$$

$$\Rightarrow (2x - 12)(x - a) = 0$$

On equation both the factors with '0' we get

$$\Rightarrow 2x - 12 = 0 \quad \rightarrow x - a = 0$$

$$\Rightarrow 2x = 12 \quad \rightarrow x = a$$

$$\Rightarrow X = 6$$

∴ Two roots are 6 and a

∴ Option B is the correct answer.

Question 2

Solving equation $3g^2 - 14g + 16 = 0$, we get roots as

(a) 0

(c) 8 and $\frac{2}{3}$

(b) ± 5

(d) 2 and $\frac{8}{3}$

Answer: d

Explanation:

By option d

Putting value 2

$$3 \times 2^2 - 14(2) + 16 = 0$$

$$0=0$$

putting value $\frac{8}{3}$

$$3 \times \left(\frac{8}{3}\right)^2 - 14 \times \frac{8}{3} + 16$$

$$0=0$$

Question 3

Solving equations $m + \sqrt{m} = \frac{6}{25}$ the value of $\sqrt{m} = \frac{6}{25}$ the value of 'm' works out to works out to:

(a) $\frac{2}{25}$

(b) $\frac{1}{25}$

(c) $\frac{3}{25}$

(d) 1

Answer: b

Explanation:

Correct option is B $\frac{1}{25}$

$$m + \sqrt{m} = \frac{6}{25}$$

let $m = t^2$

$$\therefore t^2 + t = \frac{6}{25}$$

$$\Rightarrow 25t^2 + 25t - 6 = 0$$

$$\Rightarrow t = \frac{-25 \pm \sqrt{625 + 4 \times 25 \times 6}}{2 \times 25}$$

$$t = \frac{-25 \pm \sqrt{1225}}{50}$$

$$t = \frac{-25 \pm 35}{50}$$

$$t = \frac{10}{50} \text{ and } t = \frac{-60}{50}$$

\therefore , $t = \frac{1}{5}$ is correct answer

$$\text{Now, } m = t^2 = \frac{1}{25}$$

\therefore , Option B is correct.

JULY 2021

Question 1

If α and β are the roots of the equation $2x^2 + 5x + k = 0$, and $4(\alpha^2 + \beta^2 + \alpha\beta) = 23$, then which of the following is true?

(a) $k^2 + 3k - 2 = 0$

(b) $k^2 - 2k + 3 = 0$

(c) $k^2 - 2k - 3 = 0$

(d) $k^2 - 3k + 2 = 0$

Answer: Options (d)

Question 2

The cost of 2 oranges and 3 apples is ₹ 28. If the cost of an apple is doubled then the cost of 3

oranges and 5 apples is ₹ 75. The original cost of 7 oranges and 4 apples (in ₹) is.

- (a) 59 (b) 47
(c) 71 (d) 63

Answer: Options (a)

Question 3

The value of 'K' is _____, if 2 is a root of the following cubic equation: $x^3 - (k+1)x + k = 0$

- (a) 2 (b) 6
(c) 1 (d) 4

Answer: Options (b)

Question 4

The sum of square of any real positive quantities and its reciprocal is never less than

- (a) 1 (b) 2
(c) 3 (d) 4

Answer: Options (b)

Explanation:

Let the positive real number be a then its reciprocal will be $\frac{1}{a}$.

So using property $AM \geq GM$ we could say that

$$\frac{a + \frac{1}{a}}{2} \geq \sqrt{a \times \frac{1}{a}} \text{ Or}$$

$$\left(a + \frac{1}{a}\right) \geq 2 \times 1$$

$$\text{Therefore } \left(a + \frac{1}{a}\right) \geq 2.$$

Question 4

If $A = \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix}$ then the value of A^5 is

- (a) $\begin{bmatrix} 1 & 0 \\ -1 & 5 \end{bmatrix}$ (b) $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$
(c) $\begin{bmatrix} 1 & 0 \\ -5 & 1 \end{bmatrix}$ (d) $\begin{bmatrix} 1 & -5 \\ 0 & 1 \end{bmatrix}$

Answer: Options (c)

DEC 2021

Question 1

If one root is half of the other of a quadratic equation and the difference in roots is a , then the equation is

- (a) $x^2 + ax + 2a^2 = 0$ (b) $x^2 - 3ax - 2a^2 = 0$
(c) $x^2 - 3ax + 2a^2 = 0$ (d) $x^2 + 3ax - 2a^2 = 0$

Answer:

Explanation:

Let one root be a , and another root be $\frac{1}{2} \times a = \frac{a}{2}$. Since one root is half of the other root, we have $p = \frac{1}{2}a = q$ Since the difference of the roots is a , we have:

$$a - \frac{a}{2} = a$$

$$\frac{2\alpha - \alpha}{2} = a$$

$$\frac{\alpha}{2} = a$$

$$\alpha = 2a$$

$$\text{Therefore, } \beta = \frac{\alpha}{2} = \frac{2a}{2} = a$$

$$\text{Sum of roots} = 2a \times a = 2a^2$$

When the roots are known, the equation is given by:

$$x^2 - (\text{Sum of Roots})x + \text{Product of Roots} = 0$$

Therefore, the equation is:

$$x^2 - 3ax + 2a^2 = 0$$

Question 2

In a multiple choice question paper consisting of 100 questions of 1 mark each, a candidate gets 60% marks. If the candidate attempted all wrong answer, the difference between number of right answers questions and there was a penalty of 0.25 marks for and wrong answers is:

(a) 32

(b) 36

(c) 40

(d) 38

Answer:

Explanation:

Let the number of right answers be x ; then the number of wrong answers be $100 - x$. Total marks = 60

$$(1 \times x) - 0.25(100 - x) = 60$$

$$= x - (25 - 0.25x) = 60$$

$$-x - 25 + 0.25x = 60$$

$$= 1.25x = 60 + 25$$

$$= 1.25x = 85$$

$$x = \frac{85}{1.25} = 68$$

Therefore, the number of correct answers = 68.

Hence, the number of wrong answers = $100 - 68 = 32$.

Therefore, the difference between the correct answers and wrong answers = $68 - 32 = 36$.

Question 3

If the square of a number exceeds twice of the number by 15, then number that satisfies the condition is

(a) -5

(b) 3

(c) 5

(d) 15

Answer: c

Explanation:

Let the number be x .

As per the question, $x^2 - 2x = 15$

Now, try the options.

Option (a) = -5

$$\text{LHS} = (-5)^2 - 2(-5) = 25 + 10 = 35 \neq \text{RHS}$$

Option (b) = 3

$$\text{LHS} = (3)^2 - 2(3) = 9 - 6 = 3 = \text{RHS}$$

Option (c) = 5

$$\text{LHS} = (5)^2 - 2(5) = 25 - 10 = 15 = \text{RHS}$$

Therefore, option (c) is the answer.

Question 4

Solve $x^3 - 7x + 6 = 0$

(a) $x = 6, 7, -4$

(b) $x = -1, -2, -3$

(c) $x = 1, 2, -3$

(d) $x = 2, 4, 6$

Answer:

Solve $x^3 - 7x + 6 = 0$

$$x^3 - x^2 + x^2 - 7x + 6 = 0$$

$$x - (x - 1) + x^2 - x - 6x + 6 = 0$$

$$x^3 (x - 1) + x(x - 1) - 6(x - 1) = 0$$

$$(x - 1)(x^2 + x - 6) = 0$$

$$(x - 1)(x^2 + 3x - 2x - 6) = 0$$

$$(x - 1)[x(x + 3) - 2(x + 3)] = 0$$

$$(x - 1)(x + 3)(x - 2) = 0$$

If $x - 1 = 0$ If $x + 3 = 0$ If $x - 2 = 0$

$$x = 1 \quad x = -3 \quad x = 2$$

$$= 1, 2, -3$$

JUNE 2022

Question 1

The values of x and y satisfying the equations

$\frac{3}{x+y} + \frac{2}{x-y} = 3, \frac{2}{x+y} + \frac{2}{x-y} = 3\frac{2}{3}$ are given by:

(a) (1, 2)

(b) (-1, -2)

(c) (1, 1/2)

(d) (2, 1)

Answer: Options (d)

Explanation:

Given $\frac{3}{x+y} + \frac{2}{x-y} = 3$ _____ (1)

$\frac{2}{x+y} + \frac{3}{x-y} = 3\frac{2}{3}$ _____ (2)

By Hits/ Trial

Putting $x = 2, y = 1$ in equation (1)

$$\frac{3}{2+1} + \frac{2}{2-1} = 3$$

$$1 + 2 = 3$$

$$3 = 3 \text{ (which is satisfied)}$$

and putting $x = 2, y = 1$ in equation (2)

$$\frac{2}{2+1} + \frac{3}{2-1} = 3\frac{2}{3}$$

$$\frac{2}{3} + \frac{3}{1} = \frac{11}{3}$$

$$\frac{11}{3} = \frac{11}{3} \text{ (which is satisfied)}$$

Question 2

If the second root of the given equation is reciprocal of first root then value of 'k' in the equation $5x^2 - 13x + k = 0$

- (a) 3 (b) 2
(c) 1 (d) 5

Answer: Options (d)

Explanation:

Given Q.E. $5x^2 - 13x + k = 0$
 on comparing $ax^2 + bx + c = 0$
 We get, $a = 5, b = -13, c = k$
 if one root is reciprocal to other
 Roots then $c = a$
 $k = 5$

Question 3

A Plumber can be paid, either ₹ 600 and ₹ 50 per hour or ₹ 170 per hour. If the job takes 'n' hour, for what value of 'n' the method earns better wages for the plumber?

- (a) 5 (b) 6
(c) 4 (d) 7

Answer: Options (a)

Explanation:

Let Plumber takes 'n' hour to complete the jobs
 Given, $600 + 50 \times n = 170 \times n$
 $600 + 50n = 170n$
 $600 = 170 - 50n$
 $600 = 120n$
 $n = \frac{6000}{120}$
 $n = 5$

Question 4

If a person has cloth of total 91 cm. If he divides it into 3 parts then longest part is twice the shortest one and another part is 3 cm more than shortest one. What is the shortest one?

- (a) 25 (b) 44
(c) 22 (d) 46

Answer: Options (c)

Explanation:

Let shortest part = x
 longest part = 2x
 other part = (x + 3)
 Given total length of cloths = 91
 $x + 2x + (x + 3) = 91$
 $x + 2x + x + 3 = 91$
 $4x + 91 - 3$
 $4x = 88$
 $x = \frac{88}{4}$
 $x = 22$

