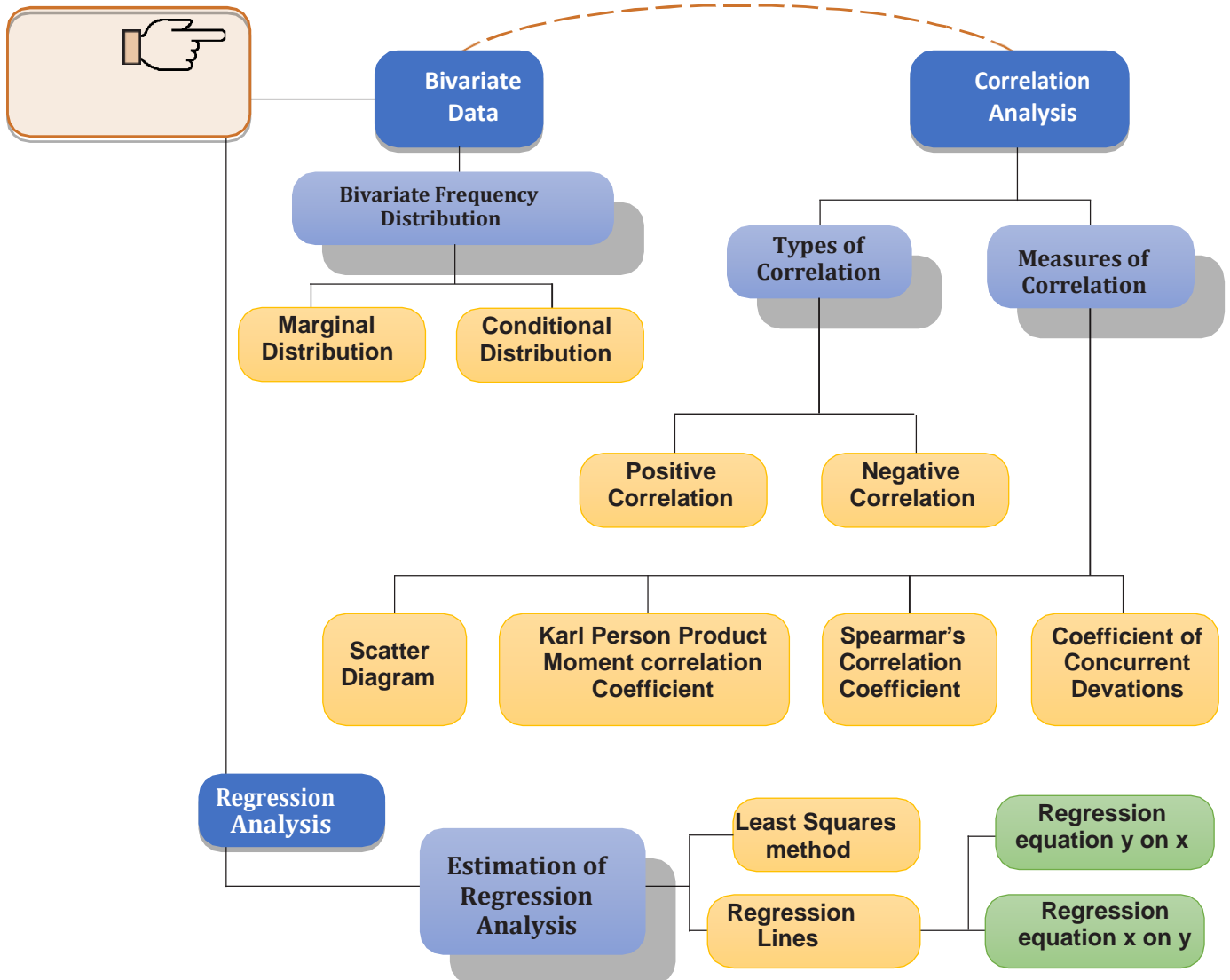


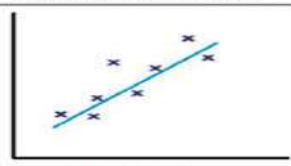
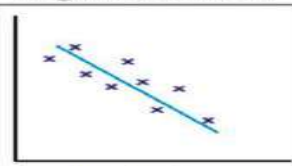
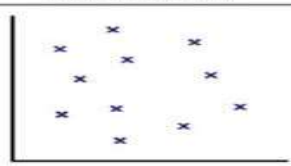
CHAPTER - 17 CORRELATION AND REGRESSION



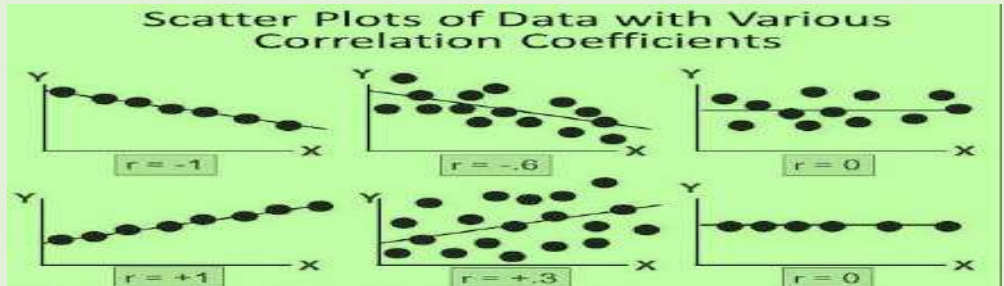
CORRELATION

The change in one variable is reciprocated by a corresponding change in the other variable either directly or inversely, then the two variables are known to be associated or correlated

TYPES OF CORRELATION

Positive correlation	Negative correlation	No correlation
		
The points lie close to a straight line, which has a positive gradient.	The points lie close to a straight line, which has a negative gradient.	There is no pattern to the points.
This shows that as one variable increases the other increases .	This shows that as one variable increases , the other decreases .	This shows that there is no connection between the two variables.

MEASURES OF CORRELATION



Rank Correlation

- The formula of Spearman's Rank correlation coefficient, is given as:

$$r_s = 1 - \frac{6 \sum d_i^2}{n(n^2 - 1)}$$

r_s : is the coefficient of rank correlation.

d_i : is the difference in rank between paired values of X and Y , it can be calculated as (rank of X_i - rank of Y_i).

n : is a sample size or the number of pairs values X and Y in the selected sample.

Correlation Coefficient

Correlation coefficient

- A measure of the strength and the direction of a linear relationship between two variables.
- The symbol r represents the sample correlation coefficient.
- A formula for r is

$$r = \frac{n \sum xy - (\sum x)(\sum y)}{\sqrt{n \sum x^2 - (\sum x)^2} \sqrt{n \sum y^2 - (\sum y)^2}} \quad n \text{ is the number of data pairs}$$

- The population correlation coefficient is represented by ρ (rho).

Pearson's Correlation Coeff.

Pearson's correlation coefficient between two variables is defined as the covariance of the two variables divided by the product of their standard deviations:

$$\rho_{X,Y} = \frac{\text{cov}(X, Y)}{\sigma_X \sigma_Y} = \frac{E[(X - \mu_X)(Y - \mu_Y)]}{\sigma_X \sigma_Y}$$

The above formula defines the *population correlation coefficient*, commonly represented by the Greek letter ρ (rho). Substituting estimates of the covariances and variances based on a sample gives the *sample correlation coefficient*, commonly denoted r :

$$r = \frac{\sum_{i=1}^n (X_i - \bar{X})(Y_i - \bar{Y})}{\sqrt{\sum_{i=1}^n (X_i - \bar{X})^2} \sqrt{\sum_{i=1}^n (Y_i - \bar{Y})^2}}$$

$$r_{xy} = \frac{\sum x_i y_i - n \bar{x} \bar{y}}{n s_x s_y} = \frac{n \sum x_i y_i - \sum x_i \sum y_i}{\sqrt{n \sum x_i^2 - (\sum x_i)^2} \sqrt{n \sum y_i^2 - (\sum y_i)^2}}$$

POINT TO SIGNIFY

The 'coefficient of non-determination' is given by $(1-r^2)$ and can be interpreted as the ratio of unexplained variance to the total variance.

The two lines of regression coincide i.e. become identical when $r = -1$ or 1 or in other words, there is a perfect negative or positive correlation between the two variables under discussion. If $r = 0$ Regression lines are perpendicular to each other

The two lines of regression intersect at the point, where x and y are the variables under consideration

There regression coefficients remain unchanged due to a shift of origin but change due to a shift of scale.



Question 1

The table below show the height, x , in inches and the pulse rate y , per minute for 9 people find the correlation coefficient and interpret your result.

X	68	72	65	70	62	75	78	64	68
Y	90	85	88	100	105	98	70	65	72

(a) 0.69

(b) 0.56

(c) 0.15

(d) None

Answer: c**Explanation:**

You may use the fact that (double check this for practice)

$$\sum x = 622, \sum y = 773, \sum x^2 = \sum y^2 = 68.007, \sum xy = 53,336$$

Calculate the numerator

$$x^2 = 43206$$

$$y^2 = 68007$$

$$n\sum(xy) - (\sum x)(\sum y) = 9.53336 - 622.773 = -782$$

$$\sqrt{n\sum x^2 - (\sum x)^2} \cdot \sqrt{n\sum y^2 - (\sum y)^2}$$

$$= \sqrt{9.43206 - (622)^2} \cdot \sqrt{9.68007 - (773)^2}$$

$$= \sqrt{1970} \cdot \sqrt{14534} = 5350.89$$

$$\text{Now, divide to get } r = \frac{-782}{5350.89} = 0.15$$

Question 2

In the previous problem the researcher decides to use data only for adults age 21 to 60 to compute a correlation coefficient what value of r should he expect?

(a) $r = 0$ (b) $r \neq 0$ (c) $r < 0$ (d) $r > 0$ **Answer: a****Explanation:**

$r = 0$. It is unexpected that mathematical ability and shoe size varies together

Question 3

The following data relate to the test scores obtained eight salesmen in an aptitude test and their daily sales in thousands of rupees:

	1	2	3	4	5	6	7	8
Scores	60	55	62	56	62	64	70	54
Sales	31	28	26	24	30	35	28	24

(a) 48

(b) 56

(c) 4.5

(d) 0.48

Answer: d**Explanation:**

$$\text{Asb} = \frac{24+35}{2} = 30$$

Scores (xi)	Sales in 1000(yi)	ui=xi =62 (3)	Vi = yi - 30	Ui vi (5)=(3)×((6) = (U i) ²	(7) (Vi) ²
----------------	----------------------	------------------	-----------------	--------------------	--------------------------	--------------------------

(i)	(2)		(4)	(4)		
60	31	-2	1	-2	4	1
55	28	-7	-2	14	49	4
62	26	0	4	0	0	16
56	24	-6	-6	36	36	36
62	30	0	0	0	0	0
64	35	2	5	10	4	25
70	28	8	-2	-16	64	4
54	24	-8	6	48	64	36
Total	-	-13	-14	90	221	122

Since correlation coefficient remain unchanged due to change of origin we have

Question 4

If $r = 0.7$; and $n = 64$ find out the probable error of the coefficient of correlation.

- (a) 0.043 (b) 0.43
 (b) 0.747, 0.657 (d) 0.7

Answer: a

Explanation:

$$r = 0.7; n = 64$$

$$P.E. = 0.67745 \times \left[\frac{1-r^2}{\sqrt{n}} \right]$$

$$\text{Probable Error (P.E)} = 0.6745 \times \frac{1-(0.7)^2}{\sqrt{64}}$$

$$= (0.6745) \times (0.06375)$$

$$= 0.043$$

Question 5

Compute the probable error assuming the correlation coefficient of 0.8 from a sample of 25 pairs of item

- (a) 0.0486 (b) 0.0456
 (c) 0.0567 (d) 0.0789

Answer: a

Explanation:

$$r = 0.8, n = 25$$

$$P.E. = 0.6745$$

$$\frac{1 - (0.8)^2}{\sqrt{25}}$$

$$= 0.6745 \times 0.07 = 0.0486$$

Question 6

Difference between Correlation and Causation

- (a) The variable mutually influence each other so that neither can be called the causes of other
 (b) The correlated variables are influenced By one or more variables.
 (c) Pure change correlation
 (d) All

Answer: d

Explanation:

The term correlation should not be misunderstood as causation if correlation exists between two variables it must not be assumed that a change in one variable is the cause of a change in over variable.

Question 7

For some bivarilate data the following result were obtained the two variable X and Y:

$$x = 53.2, y = 27.9 \quad b_{vx} = -1.5 \quad b_{xy} = -0.2$$

The most probable value of y when x = 60 is

- (a) 15.6
 (b) 13.4
 (c) 19.7
 (d) 17.7

Answer: d

Explanation:

The regression equation of y of x is:

$$y - y = b_{yx} (x - x) \\ = y - 27.9 = (-1.5) (x - 53.2)$$

$$\text{Or } y = 107.7 - 1.5x$$

When x = 60 then

$$y = 107.7 - 1.5 \times 60 = 17.7$$

Question 9

If the sum of square of the rank difference in mathematics and physics marks of 10 students is 22, then the coefficient of rank correlation is:

- (a) 0.267
 (b) 0.867
 (c) 0.92
 (d) None

Answer: b

Explanation:

Co. efficient of rank correlation

$$1 - \frac{6 \sum d^2}{n(n^2 - 1)} \\ 1 - \frac{6 \times 22}{10(10^2 - 1)}$$

$$1 - \frac{6 \times 2}{10 \times 9}$$

$$\frac{13}{15} = 0.867 \text{ (Approx.)}$$

Question 10

The coefficient of correlation r between x and y when: $\text{Cov}(x, y) = -16.5$, $\text{Var}(x) = 2.89$, $\text{Var}(y) = 100$ is:

- (a) -0.97 (b) 0.97
(c) 0.89 (d) -0.89

Answer: a

Explanation:

$$r = \frac{\text{Cov}(x,y)}{\sigma_x \sigma_y}$$

$$\text{Or } r = \frac{\text{Cov}(x,y)}{\sqrt{\text{vary}(x) \times \text{vary}(y)}}$$

$$= \frac{-16.5}{\sqrt{2.89 \times 100}}$$

$$= -0.97$$

Question 11

Two random variable have the regression line $3x + 2y = 26$ and $6x + y = 31$. The coefficient of correlation between x and y is:

- (a) -0.25 (b) -0.5
(c) 0.5 (d) 0.25

Answer: c

Explanation:

The regression lines $3x + 2y = 26$ and $6x + y = 31$ are given

Let first equation be y on x and second be x only respectively therefore, $3x + 2y = 26$

$$= \left(\frac{-3}{2}\right)x + 26$$

$$\therefore b_{yx} = -3/2$$

$$\text{and } 6x + y = 31$$

$$= x = \left(\frac{-1}{6}\right)x + \left(\frac{31}{6}\right)$$

$$b_{xy} = -1/6 \text{ Now}$$

$$r^2 = b_{yx} \cdot b_{xy}$$

$$= \left(\frac{-3}{2}\right) \times \left(\frac{-1}{6}\right)$$

$$= 0.25$$

$$r = 0.5$$

Hence, our assumption hold true hold and $r = 0.5$ (- 1 r 1)

Note r is negative because b_{yx} and $b_{xy} = 0$

Question 12

The coefficient of correlation between X and Y is 0.6 U and V are two variable defined as $U = \frac{x-3}{2}, V = \frac{y-2}{3}$, then the coefficient of correlation between U and V is:

- (a) 0.6 (b) 0.8
(c) 0.4 (d) 1

Answer: a

Explanation:

Since correlation coefficient (Karl Pearson's) is independence of both scale and origin therefore,

$$p(u,v) = p(x,y) = 0.6$$

it may be noted that if

$u = ax + b$ and $V = cY + d$ then

$r(u,v) = P(x,y)$ if a and c are of same signs

$P(x,y)$ if a and c are of opposite signs

Question 13

For the following data the coefficient of rank correlation is:

Rank in Botany	1	2	3	4	5
Rank in Chemistry	2	3	1	5	4

- (a) 0.93 (b) 0.4
(c) 0.6 (d) None

Answer: c

Explanation:

S No.	Rank in Botany(x_i)	Rank in Chem (y_i)	$d = (x_i) - (y_i)$	d^2
1	1	2	-1	1
2	2	3	-1	1
3	3	1	2	4
4	4	5	-1	1
5	5	4	1	1
Total			0	8

Hence coefficient of rank correction

$$1 - \frac{6 \times 8}{5(5^2 - 1)}$$

$$S = 1 - \frac{2}{5} = 0.6$$

Question 14

The following data is given on 450 students for marks in statistics and Economic at a certain examination

Mean marks in statistics = 40
Mean marks in economics = 48
S.D. of marks (statistics) = 12
Variance of marks (Economics) = 256

Sum of the products of deviation of

Marks from their respective mean = 42075

The average marks in economics of candidates who obtained 50 marks in statistics is:

- (a) 45 (b) 54
(c) 54.5 (d) 47.5

Answer: c

Explanation:

Let x = marks statistics
and y = marks in Economics
we know that

$$r_{xy} = \frac{\sum dx \times dy}{n \times \sigma_x \sigma_y}$$

Where dx = $x_1 - \bar{x}$ and dy = $y_1 - \bar{y}$

$$r_{xy} = \frac{(42075)}{450 \times 12 \times 16} = 0.49$$

Now regression equation of y on x

$$y - \bar{y} = \frac{r \sigma_y (x - \bar{x})}{\sigma_x}$$

$$= y - 48 = x \frac{0.49 \times 16}{12} (x - 40)$$

$$= y = 0.65 \text{ then}$$

$$y = 0.65x - 26 + 48$$

$$y = 0.65x + 22$$

$$x = 50$$

Question 15

For 10 pair of observation, number of concurrent deviation was found to be 4. what is the value of the coefficient deviation?

- (a) $\sqrt{0.2}$ (b) $-\sqrt{0.2}$
(c) $1/3$ (d) $-1/3$

Answer: d

Explanation:

Here C = 4, N = 10, So

$$n = N - 1 = 10 - 1 = 9$$

$$r_c = \pm \sqrt{\frac{\pm (2c - n)}{n}}$$

$$r_c = \pm \sqrt{\frac{\pm (2 \times 4 - 9)}{9}}$$

Here $(2c - n)$ is negative so negative sign is take at both the place so $rc = (-1)/3$

Question 16

Karl Pearson's formula:

$$(a) \frac{[N \sum XY - (\sum X)(\sum Y)]}{\sqrt{[N \sum X^2 - (\sum X)^2]}}$$

$$(b) r = \frac{n(\sum xy) - (\sum X)(\sum Y)}{\sqrt{[n \sum x^2 - (\sum x)^2][n \sum y^2 - (\sum y)^2]}}$$

(c) Either a or b

(d) None

Answer: b

Explanation:

$$r = \frac{n(\sum xy) - (\sum X)(\sum Y)}{\sqrt{[n \sum x^2 - (\sum x)^2][n \sum y^2 - (\sum y)^2]}}$$

Where

N = number of pairs of scores

$\sum xy$ = sum or the products or paired scores

$\sum x$ = sum of x scores

$\sum y$ = sum of y scores

$\sum x^2$ = sum of squared x scores

$\sum y^2$ = sum of squared y scores

Question 17

If the coefficient of correlation between x and Y variable is +0.90 then what will be coefficient of determination?

(a) 0.39

(b) 0.81

(c) 0.94

(d) None of these

Answer: b

Explanation:

If Coeff. of Correlation $R = 0.90$

Coeff. of Determination = r^2

$$= (0.90)^2$$

$$= 0.81$$

Question 18

The two lines of regression become identical when

(a) 0.4

(b) 0.6

(c) 0.36

(d) 0.64

Answer: c

Explanation:

If $r = 0.6$

Then Coeff, of determination = r^2

$$= (0.6)^2$$

$$= 0.36$$

Question 19**There two regression lines passing through**

- (a) Represent means (b) Represent S. Ds
 (c) (a) and (b) (d) None of these

Answer: a**Explanation:**

The two regressions lines passing through or (Intersect) at their means.

Question 20**The regression equation x and y is $3x + 2y = 100$ value of b_{xy}**

- (a) $-\frac{2}{3}$ (b) $-\frac{3}{2}$
 (c) $\frac{2}{3}$ (d) $\frac{100}{2}$

Answer: a**Explanation:**

The regression equation of x & y is

$$3x + 2y = 100$$

$$3x + 2y - 100 = 0$$

$$b_{xy} = -\frac{\text{Coefficient of } y}{\text{coefficient of } x} = -\frac{2}{3}$$

Question 21**In beauty contest there were 10 competitors of these candidates assigned by two judge A and b the sum of squares of difference of rank is 44. The value of rank correlation is:**

- (a) 0.70 (b) 0.73
 (c) 0.80 (d) 0.60

Answer: b**Explanation:**Sum of square of difference of rank $(\sum d^2) = 44$

$$r_R = ?$$

$$r_R = 1 - 6 \frac{\sum d^2}{n(n^2 - 1)}$$

$$1 - \frac{6 \times 4}{10(10^2 - 1)}$$

$$1 - \frac{6 \times 44}{10 \times 99}$$

$$= 1 - 0.267$$

$$= 0.733$$

So answer be 0.73

Question 22**If two regression lines are $x + y = 1$ and $x - y = 1$ then mean value of x and y will be:**

- (a) 0 and 1
 (c) 1 and 0
- (b) 1 and 1
 (d) None

Answer: c

Explanation:

Given Regression line

$$\Rightarrow x = \frac{2}{2} = 1$$

x = 1 in equation (1) we get

$$1 - y = 1$$

$$y = 0$$

Mean of x = $\bar{x} = 1$

Mean of y = $\bar{y} = 0$

Hence 1 and 0

Question 23

The coefficient of correlation between x and y is 0.6 If x and y value are multiplied by 1 then the coefficient will be

- (a) 0.6
 (c) 1/0.6
- (b) 1-0.6
 (d) -0.6

Answer: a

Explanation:

The coefficient of correlation between X and Y is 0.6 If x and y values are multiplied by 1 then coefficient remains unchanged then are coefficient of correlation will be 0.6

Question 24

The coefficient of correlation between the temperature of environment and power consumption is always:

- (a) +ve
 (c) 0
- (b) - ve
 (d) = 1

Answer: a

Explanation:

The coefficient of correlation between the temperature of environment and power consumption is always positive.

Question 25

Out of the following the one which the regression coefficient is

- (a) Change origin only
 (c) Change of scale and origin both
- (b) Change of scale only
 (d) Neither a nor b

Answer: b

Explanation:

By shifting the scale, coefficient of regression is changed.

Question 26

When the correlation coefficient r is equal to $+1$ all the point in a scatter diagram would be

- (a) On a straight line direct from upper left to lower right
 (b) On a straight direction from lower left to upper right
 (c) On a straight line
 (d) Both (a) and (b)

Answer: b

Explanation:

When the correlation coefficient r is equal to $+1$ all the point in a scatter diagram on a straight line directed from lower left to upper right.

Question 27

In case of "Insurance companies" profit and the number of claim they have to pay there is -----correlation.

- (a) +ve
 (b) -ve
 (c) No relation
 (d) None

Answer: b

Explanation:

In case of "Insurance companies" profit and the number of claim they have to pay there is Negative correlation:

Question 28

If the correlation coefficient between two variables is zero then the lines of regression are

- (a) Parallel
 (b) Perpendicular
 (c) Coincide
 (d) None

Answer: b

Explanation:

If the correlation coefficient between two variables is zero then the lines of regression are perpendicular

Question 29

Their competitors in a contest are ranked by two judges in the order 1,2,3 and 2,3,1 respective Calculate the spearman`s rank correlation coefficient.

- (a) -0.5
 (b) -0.8
 (c) 0.8
 (d) 0.5

Answer: a

Explanation:

Rank by 1 st judge R_1	Rank by 2 nd Judge R_2	Diff $D = R_1 - R_2$	D^2
--	--	----------------------	-------

1	2	-1	1
2	3	-1	1
3	1	+2	4
			$\sum d^2 = 6$

Here $n = 3$

$$\begin{aligned} \text{Spearman's Rank Correlation Coefficient} &= 1 - 6 \frac{\sum d^2}{n(n^2 - 1)} \\ &= 1 - \frac{6 \times 6}{3(3^2 - 1)} \\ &= -0.5 \end{aligned}$$

Question 30

The strength (degree) of the correlation between a set of independent variables X and dependent variable Y is measured by

- (a) Coefficient of Correlation (b) Standard error of estimate
(c) Coefficient Determination (d) All of these

Answer: d

Explanation:

The strength (degree) of the correlation between a set of independent variables X and dependent variable Y is measured through

- Coefficient of Correlation
- Standard error of estimate
- Coefficient Determination

Question 31

The percent of total variation of the dependent variable Y explained by the set of independent variables X is measured by:

- (a) Coefficient of Correlation (b) Standard error of estimate
(c) Coefficient Determination (d) Coefficient of skewness

Answer: c

Explanation:

The coefficient of determination (denoted by R^2) is a key output of regression analysis an R^2 of 0 means that the dependent variable cannot be predicted from the independent variable An R^2 of 1 means the dependent variable can be predicted without error from the independent variable

Question 32

A coefficient of correlation is computed to be -0.95 means that

- (a) The relationship between two variables is weak (b) The relationship two variables is strong and positive
(c) The relationship between two variables is weak (d) Correlation coefficient cannot

variables have this
is strong and but negative value

Answer: c

Explanation:

A coefficient of correlation is compute to be -0.95 means that relationship between two variables is strong and but negative

Question 33

Let the coefficient of determination computed to be 0.39 in a problem involving one independent variable and one dependent variable this result means that

- | | |
|---|---|
| (a) The relationship between two variables is negative | (b) The correlation coefficient is 0.39 also |
| (c) 39% of the total variation is explained by the independent variable | (d) 39% of the total variation explained by the dependent variables |

Answer: c

Explanation:

The coefficient of determination computed to be 0.39 in a problem involving one independent variable and one dependent variable. 39% of the total variation is explained by the independent variable.

Question 34

Relationship between correlation coefficient and coefficient of determination is that:

- | | |
|--|---|
| (a) The coefficient of determination is the square of coefficient of correlation | (b) The coefficient determination is the square root of the coefficient of correction |
| (c) Both are unrelated | (d) Both are equal |

Answer: a

Explanation:

Coefficient of correlation is "R" value which given in the summary table in the regression output. R square is called coefficient of determination multiply R times R to get the R value. In other word coefficient of correlation R square or Coeff. of determination shows percentage variation and in y which is explained by all the x variable together higher the better it is always between 0 and 1. it can never be negative – since is a squared value.

It is easy to explain the R square in term of regression it is not so easy to explain the R in terms of regression.

Question 35

For a bivariate data two lines of regression are $40x - 18y = 214$ and $8x - 10y + 66 = 0$ then find the value of x and y

- (a) 17 and 13
 (b) 13 and 17
 (c) 15 and 17
 (d) None

Answer: b

Explanation:

Given: $40x - 18y = 214$

$8x - 10y = -66$

on solving (1) and (2) we get

$x = 13$ and $y = 17$

$\therefore x = 13$ and $y = 17$

Question 36

In multiple regression when the global test of significance is rejected we can conclude that:

- (a) All of the net sample regression coefficient are equal to zero
 (b) All of the sample regression coefficient are not equal to zero
 (c) At least one sample regression coefficient is not equal to zero
 (d) The regression equation intersects the y -axis at zero

Answer: c

Explanation:

In multiple regression when the global test of significance is rejected we can conclude that at least one simple regression coefficient is not equal to zero.

Question 37

Correlation Coefficient value lies between

- (a) -1 and $+1$
 (b) 0 and 1
 (c) -1 and 0
 (d) None

Answer: a

Explanation:

The strength of the linear association between two variables is qualified by the correlation coefficient the correlation coefficient always takes a value between -1 and 1 with 1 or -1 indicating perfect correlation (all points would lie along a straight line in this case)

Question 38

In correlation both variables are always

- (a) Random
 (b) Non Random
 (c) Same
 (d) None

Answer: a

Explanation:

Complete correlation between two variables is expressed by either + 1 or -1 when one variable increases the correlation is positive when on decrease as the order increases it is negative complete absence of correlation is represented by 0.

Question 39

The table below shows the number of absence x, in a calculus course and the final exam grade y for 7 student find the correlation coefficient.

x	1	0	2	6	4	3	3
y	95	90	90	55	70	80	85

(a) 0.38

(b) -0.38

(c) 0.62

(d) -0.93

Answer: d

Explanation:

You may use the facts that (double check this for practice)

$$\sum x = 19, \sum y = 565, \sum x^2 = 75, \sum y^2 = 46,775, \sum xy = 1,380$$

Calculate the numerator:

$$n \sum(xy) - (\sum x)(\sum y) = 7.1380 - 19 \times 565 = -1075$$

Then the calculate the denominator;

$$\frac{\sqrt{[n(x^2) - (\sum x)^2]}\sqrt{[n(y^2) - (\sum y)^2]}}{(525 - 369) \cdot [327425 - 319225]}$$

Question 40

Two regression lines are parallel to each other if their slope is

(a) Random

(b) Non Random

(c) Same

(d) None

Answer: c

Explanation:

When there is a reasonable amount of scatter we can draw two different regression lines depending upon which variable we consider to be the most accurate. The first is a line of regression of y on x which can be used to estimate y given x, the other is a line of regression of x on y used to estimate x given y. Hence two regression lines are parallel to each other if their slope is same.

Question 41

When regression line passes through the origin then

(a) Regression coefficient is zero

(b) Correlation is zero

(c) Intercept is zero

(d) Association is zero

Answer: c

Explanation:

Prism linear regression analysis fits a straight line through your data and lets you force the line to go through the origin this is useful when you are sure that the line must begin at the origin ($x = 0$ and $y = 0$) Prism's nonlinear regression offers the equation line through origin.

Question 42

The table below shows the number of absence, x in a calculate course and the final exam grand, y for 7 student find the correlation coefficient.

x	1	0	2	6	4	3	3
y	85	80	70	55	90	90	95

(a) 0.38

(b) 0.6

(c) -0.38

(d) 0.62

Answer: c**Explanation:**

There are 7 ordered pairs (x, y) so $n = 7$ Calculate the needed sums:

X	Y	X ²	Y ²	xy
1	85	1	7225	85
0	80	0	6400	0
2	70	4	4900	140
6	55	36	3025	330
4	90	16	8100	360
3	90	9	8100	270
3	95	9	9025	285
X = 19	Y = 565	X ² = 75	Y ² = 46775	Xy = 1470

Calculation the numerator: $n \sum (xy) - (\sum x)(\sum y)$

$$= 7 \cdot 1470 - 19 \cdot 565$$

$$= -445$$

Then calculate the denominator:

$$\sqrt{n \sum x^2 - (\sum x)^2} \sqrt{n \sum y^2 - (\sum y)^2}$$

$$= \sqrt{7 \cdot 75 - (19)^2} \cdot \sqrt{7 \cdot 46775 - (565)^2}$$

$$= \sqrt{164} \cdot \sqrt{8200} = 1159.66$$

$$\text{Now, divide to get } r = \frac{-445}{1159.66} = -0.38$$

Question 43

If two variables oppose each other than the correlation will be

- (a) Positive Correlation
(c) Perfect Correlation

- (b) Negative Correlation
(d) None

Answer: b

Explanation:

A correlation of zero means there is no relationship between the two variables, when there is a negative correlation between two variables as the value of one variable increase the value of the other variable decrease and *vis- versa*

Question 44

The time x in years that an employee spent at a company and the employee's hourly pay, y for 5 employees are listed in the table below. Calculate and interpret the correlation coefficient r. Include a plot of the data in your discussion

- (a) 0.38
(c) 0.62

- (b) -0.97
(d) None

Answer: d

Explanation:

X	Y	X ²	Y ²	xy
5	25	25	625	125
3	20	9	400	60
4	21	16	441	84
10	35	100	1225	350
15	38	225	1444	570
X = 37	Y=139	X ² 375	Y ² = 4135	XY = 1189

Hint Calculate the numerator:

$$n \sum (xy) - (\sum x)(\sum y) = 5 \cdot 1189 - 37 \cdot 139 = 802$$

Then calculate the denominator

$$= \sqrt{n \sum x^2 - (\sum x)^2} \sqrt{n \sum y^2 - (\sum y)^2}$$

$$= \sqrt{5 \times 375 - (37)^2} \cdot \sqrt{5 \cdot 4135 - (139)^2}$$

$$= \sqrt{506} \cdot \sqrt{1354} = 827.72$$

$$\text{Now divide to get } r = \frac{802}{827.72} = 0.97$$

Question 45

Identify the true correlation

- (a) -1 & 1
(c) 0 & 1

- (b) -1 & 0
(d) All are true

Answer: a

Explanation:

- (a) Reduces to zero
(c) Minimize
- (b) Approaches to infinity
(d) Maximize

Answer: c

Explanation:

The method of least squares finds the best fit line that minimize the error between observed and estimate points on the line.

Question50

A regression model may be:

- (a) Linear
(c) Both (a) and (b)
- (b) Non - linear
(d) Neither (a) and (b)

Answer: a

Explanation:

In the regression it appears on the left side of the equal sign, while you can use regression to predict the dependent variable you always start with a set of known y value and use these to build (or to calibrate) the regression model may be linear and nonlinear both

PAST EXAMINATION QUESTION

MAY 2018

Question1

If the model points in a scatter diagram are evenly distributed then the correlation is:

- (a) 0
(c) +ve
- (b) -ve
(d) a or b

Answer: a

Explanation:

In the case of a positive correlation, the plotted points are distributed from lower left corner to upper right corner (in the general pattern of being evenly spread about a straight line with a positive slope), and in the case of a negative correlation, the plotted points are spread out about a straight line of a ...

Question2

If the plotted points in a scatter are evenly distributed, then the correlations are zero.

The covariance between variable is

- (a) Strictly positive (b) Strictly negative
(c) Always zero. (d) Either positive or negative zero.

Answer: d

Explanation:

The Co- variance between two variables is either positive or negative or zero.

Question3

The coefficient of determination is defined by the formula.

- (a) $r^2 = \frac{1 - \text{unexpalained variance}}{\text{Total variance}}$ (b) $r^2 = \frac{\text{expalained variance}}{\text{Total variance}}$
(c) Both (a) and (b) (d) None

Answer: c

Explanation:

The coefficient of determination

$$r^2 = \frac{1 - \text{unexpalained variance}}{\text{Total variance}}$$

$$r^2 = \frac{\text{expalained variance}}{\text{Total variance}}$$

Question4

In the method of concurrent deviations only the directions of change (positive direction/ Negative direction) in the variable are taken into account for calculation of

- (a) Coefficient of SD (b) Coefficient of regression
(c) Coefficient of correlation (d) None

Answer: c

Explanation:

The method of concurrent deviation only the direction of change (positive direction/ Negative direction) in the variables are taken into account for calculation of coefficient of correlation

Question5

Correlation coefficient is----of the units of measurement

- (a) Dependent (b) Independent
(c) Both (d) None

Answer: b

Explanation:

Correlation coefficient is Independent of the units of measurement.

Question 6

In case speed of an automatic and the distance required to stop the car after applying correlation is

- (a) +ve (b) -ve
(c) 0 (d) None

Answer: a

Explanation:

In case speed of an automatic and the distance required to stop the car after applying correlation is positive

Question7

A relationship $r^2 = 1 - \frac{500}{300}$ is possible

- (a) True (b) False
(c) Both (d) None

Answer: a

Explanation:

$r^2 = 1 - \frac{500}{300}$ is possible

$r^2 = 1 - \frac{-200}{300}$ is not possible

So it is true

Question8

Rank correlation coefficient lies between

- (a) -1 to +1 (b) 0 to 1
(c) -1 to 0 (d) Both

Answer: a

Explanation:

Rank correlation coefficient lies between -1 to + 1 inclusive of both value.

NOV 2018

Question1

The two lines of regression intersect at the point

- (a) Mean (b) Mode
(c) Median (d) None

Answer: a

Explanation:

The two lines of regression intersect at the point is Mean.

Question2

If the two line of regression are $x + 2y - 5 = 0$ and 0 , then the regression line of y on x s:

- (a) $x + 2y - 5 = 0$ (b) $2x + 3y - 8 = 0$
(c) $x + 2y = 0$ (d) $2x + 3y = 0$

Answer: a**Explanation:**

Given two regression line are

$$x + 2y - 5 = 0 \text{ and } 2x + 3y - 8 = 0$$

$$b_{yx} = \frac{-\text{coeff. of } x}{\text{coeff of } y} = \frac{-1}{2} \text{ and } b_{xy} = \frac{-\text{coeff. of } y}{\text{coeff of } x} = \frac{-3}{2}$$

Here, $b_{yx} \times b_{xy} \leq 1$ which is satisfiedSo, 1st equation $x + 2y - 5 = 0$ is the regression equation y on x **Question3****If the two regression line lines are $3x = y$ and $8y = 6x$ the value of correlation coefficient is:**

- (a) 0.5 (b) -0.5
(c) 0.75 (d) -0.80

Answer: a**Explanation:****Given**

Regression line

$$3x = y \text{ and } 8y = 6x$$

$$3x - y = 0 \text{ and } 6x - 8y = 0$$

$$b_{yx} = \frac{-\text{coeff. of } y}{\text{coeff of } x} \text{ and } b_{xy} = \frac{-\text{coeff. of } x}{\text{coeff of } y}$$

$$\frac{-(-1)}{3} = \frac{-6}{-8} = \frac{3}{4}$$

$$b_{yx} = \frac{1}{3} \text{ and } b_{xy} = \frac{3}{4}$$

Coff. of correlation is given by

$$r = \pm \sqrt{b_{yx} \times b_{xy}}$$

$$= \pm \sqrt{\frac{3}{4} \times \frac{1}{3}}$$

$$= \pm \frac{1}{2}$$

$$= +1/2$$

$$= 0.5$$

Question4**The regression coefficient is independent of the change of**

- (a) Scale (b) Origin
(c) Scale and Origin both (d) None

Answer: b**Explanation:**

The regression coefficient is independent of the change of 'Origin'

Question5

If the correlation coefficient between the variable X and Y is 0.5, then the correlation between the variable $2x-4$ and $3-2y$

Answer:

$$2x-u-4=0 \quad \text{and} \quad 2y+v-3=0$$

$$b = \frac{-\text{coeff. of } u}{\text{coeff. of } x} \quad \text{and} \quad d = \frac{-\text{coeff. of } v}{\text{coeff. of } y}$$

$$d = \frac{1}{2} \quad \quad \quad d = \frac{-1}{2}$$

Here, b and d both have different sign so $r_{uv} = -r_{xy}$
 $= -0.5$

MAY 2019

Question1

Given that

x	-3	-3/2	0	3/2	3
y	9	9/4	0	9/4	9

(a) Positive

(b) Zero

(c) Negative

(d) None

Answer: b

Explanation:

x	y	X ²	Y ²	xy
-3	9	9	81	-27
-3/2	9/4	9/4	81/16	-27/8
0	0	0	0	0
3/2	9/4	9/4	81/16	27/8
3	9	9	81	27
0	$\frac{90}{4}$	$\frac{90}{4}$	$\frac{2754}{16}$	0
	$= \frac{45}{2}$	$= \frac{45}{2}$	$\frac{1377}{8}$	

Hence Answer 0

Question2

Given the following series:

x	10	13	12	15	8	15
y	12	6	18	16	7	18

The rank correction coefficient $r =$

$$(a) 1 - \frac{6 \sum d^3 + \sum_{i=d}^2 \frac{m_2(m_2^3-1)}{12}}{m(n^2-1)}$$

$$(b) 1 - \frac{6 \left[\sum d^2 + \sum_{i=1}^3 \frac{m_2(m_1^2-1)}{12} \right]}{n(n^2-1)}$$

$$(c) 1 - \frac{6 \left[\sum d^2 + \sum_{i=1}^3 m_2(m_1^3-1) \right]}{n(n^2-1)}$$

(d) None

Answer: b**Explanation:**

$$1 - \frac{6 \left[\sum d^2 + \sum_{i=1}^3 \frac{m_2(m_1^2-1)}{12} \right]}{n(n^2-1)}$$

Question3

If the regression line of y on x is given by $y = x + 2$ and Karlperson's coefficient of correlation is 0.5 then $\frac{\sigma_y^2}{\sigma_x^2}$

- (a) 3 (b) 2
(c) 4 (d) None

Answer: c**Explanation:**

$$y \text{ on } x = > y = x + 2$$

$$R = 0.5$$

$$b_{yx} = r \times \frac{\sigma_y}{\sigma_x}$$

$$b_{yx} = \frac{2}{0.5}$$

Question4**A .M. OF regression coefficient is:**

- (a) Equal to r (b) Great than or equal to r
(c) Half of r (d) None of these

Answer: b**Explanation:**

Regression coefficient is a statistical measure of the average functional relationship between two or more variable In regression analysis one variable is considered as dependent and other as independent, Thus it measure the degree of dependence of one variable on the order (s)

Question5

If the two regression lines are $x + y = 1$ and $x - y = 1$ then \bar{x} and \bar{y} are

- (a) 1,0 (b) 0,1
(c) 1,1 (d) None of these

Answer: d**Explanation:**

Consider $x - y = 1$ as equation (1) as equation (2)

Now add both (1) and (2)

You get $2x = 2$ i.e. $x = 1$

Now put $x = 1$ in either of equation (1) or (2)

You get $y = 0$

Question6

Coefficient of correlation between X and Y is 0.6 if both X and Y are multiplied then resultant coefficient of correlation:

- (a) 0.6 (b) 1/0.6
(c) Both (d) None of these

Answer: a

Explanation:

Value of Correlation will -0.6 as if you multiply x & y by -1 then this will show negative sign and as per property b_{yx} , b_{xy} & r sign should be equal / same

NOV 2019

Question1

If two of regression are $x + 2y - 5 = 0$ and $2x + 3y - 8 = 0$ So $x + 2y - 5 = 0$ is

- (a) y on x (b) x on y
(c) Both (d) None

Answer: a

Explanation:

$$x + 2y - 5 = 0 \text{ - Eq 1 } \quad 2x + 3y - 8 = 0 \text{ - Eq2}$$

Let Eq 1 be y on x from Eq2

$$b_{yx} = \frac{-\text{coefficient of } x}{\text{coefficient of } y} \quad b_{xy} = \frac{-\text{coefficient of } x}{\text{coefficient of } y}$$

$$b_{yx} = \left(\frac{-1}{2}\right) \times \left(\frac{-3}{2}\right) = \frac{3}{4}$$

So, $b_{yx} \times b_{xy} < 1$

So, $x + 2y - 5 = 0$ is y on x

and $2x + 3y - 8 = 0$ is x on y

Question2

Find the coefficient of regression.

$$2x + 3y = 2$$

$$4x + 3y = 4$$

- (a) 0.5 (b) -0.5
(c) 0.25 (d) -0.25

Answer: b

Explanation:

$$2x + 3y = 2 \text{ - Eq 1 } \quad ax + 3y = 4 \text{ - Eq 2}$$

Let Eq1 be y on x

From Eq1

$$b_{yx} = \frac{-\text{coefficient of } x}{\text{coefficient of } y} = \frac{-2}{3}$$

From Eq2

$$b_{xy} = \frac{-\text{coefficient of } x}{\text{coefficient of } y} = \frac{-3}{4}$$

So above assumption hold true.

$$r = \pm \sqrt{b_{yx} \times b_{xy}}$$

$$r = \pm \sqrt{\left(\frac{-2}{3}\right) \times \left(\frac{-3}{4}\right)}$$

$$r = \frac{-1}{2}$$

$$r = -0.5$$

Question3

What is the coefficient of correlation from the following data?

X:	1	2	3	4	5
Y:	5	4	3	2	6

- (a) 0
(b) -0.75
(c) -0.85
(d) 0.82

Answer: a

Explanation:

X	Y	Xy
1	5	5
2	4	8
3	3	9
4	2	8
5	6	30
$\Sigma x = 15$	$\Sigma y = 20$	$\Sigma xy = 60$

$$\text{cov}(x,y) = \frac{\Sigma xy}{n} - \bar{x} \cdot \bar{y}$$

$$= \frac{60}{5} - \left(\frac{15}{5}\right) \times \left(\frac{20}{5}\right)$$

$$= 12 - 12$$

$$\text{cov}(x,y) = 0$$

$$r = \frac{\text{cov}(x,y)}{\sigma_x \sigma_y}$$

$$r = 0$$

Question4

If the plotted points in a scatter diagram lie from upper left to lower right, then correlation is:

- (a) Positive
(b) Negative
(c) Zero
(d) None of these

Answer: b

Explanation:

If the points in a scatter diagram lie from upper to left lower right then correlation is negative.

DEC 2020**Question 1**

Which of the following is spurious correlation?

- (a) Correlation between two variables having no causal relationship (b) Negative Correlation
- (c) Bad relation between two variables (d) Very low correlation between two variables

Answer: a

Explanation:

Correlation between two variables having no causal relationship

Question 2

Scatter diagram does not help us to

- (a) Find the type of correlation (b) Identify whether variables correlated or not
- (c) Determine the linear (or) non-linear correlation (d) Find the numerical value of correlation coefficient

Answer: d

Explanation:

To Find the numerical value of correlation coefficient

Question 3

The Covariance between two variables is

- (a) Strictly Positive (b) Strictly Negative
- (c) Always Zero (d) Either positive (or) Negative (or) Zero

Answer: d

Explanation:

Covariance can be positive, zero, or negative. ... If X and Y are independent variables, then their covariance is 0: $\text{Cov}(X, Y) = E(XY) - \mu_X\mu_Y = E(X)E(Y) - \mu_X\mu_Y = 0$ The converse, however, is not always true. $\text{Cov}(X, Y)$ can be 0 for variables that are not independent. Hence, either positive (or) Negative (or) Zero

IAN 2021**Question 1**

For the set of observations $\{(1, 2), (2, 5), (3, 7), (4, 8), (5, 10)\}$, the value of Karl-

person's coefficient is approximately given by

- (a) 0.755 (b) 0.655
(c) 0.525 (d) 0.985

Answer: d

Explanation:

x	y	xy	x ²	y ²
1	2	2	1	4
2	5	10	4	25
3	7	21	9	49
4	8	32	16	64
5	10	50	25	100
Total 15	32	115	55	242

$$5 \times 115 - 15 \times 32$$

$$\frac{\sqrt{5 \times 55 - (15)^2} \sqrt{5 \times 242 - (32)^2}}{95}$$

$$\frac{\sqrt{50} \sqrt{186}}{95}$$

$$\frac{7.07106 \times 13.638}{95} = 0.985105$$

Question 2

The coefficient of correlation between x and y is 0.5, the covariance is 16, and the standard deviation of x is 4. Then the standard deviation of y is

- (a) 4 (b) 8
(c) 16 (d) 64

Answer: b

Explanation:

$$r_{xy} = \frac{\text{cov}(x, y)}{\sqrt{\text{Var}(x) \cdot \text{Var}(y)}}$$

$$r_{xy} = 0.5$$

Question 3

The intersecting point of the two regression lines: y on x and x on y is

- (a) (0₁ 0) (b) (\bar{x} , \bar{y})
(c) (b_{yx} , b_{xy}) (d) (1, 1)

Answer: b

Explanation:

Properties of Regression Lines There are two lines of regression. Both these lines are known to intersect at a specific point (\bar{x} , \bar{y}) Here the variables under consideration are x and y.

Question 4

Given that the variance of x is equal to the square of standard deviation by and the regression line of y on x is $y = 40 + 0.5(x - 30)$. Then regression line of x on y is

- (a) $y = 40 + 4(x - 30)$ (b) $y = 40 + (x - 30)$
 (c) $y = 40 + 2(x - 30)$ (d) $x = 30 + 2 + 2(x - 40)$

Answer: d

Explanation:

Question 5

The regression coefficient remain unchanged due to

- (a) A shift of scale (b) A shift of origin
 (c) Replacing x - values by $\frac{1}{x}$ (d) Replacing y values by $\frac{1}{y}$

Answer: b

Explanation:

The regression coefficient remain unchanged due to A shift of origin

By properties of regression line we have, The regression coefficients remain unchanged due to a shift of origin but change due to a shift of scale.

JULY 2021

Question 1

If the sum of the product of the deviation of and Y from their means is zero correlation coefficient between X and Y is:

- (a) Zero (b) Positive
 (c) Negative (d) 10

Answer: Options (a)

Explanation:

Given: sum of the product of deviations of x and y series from their mean is zero,

To Find: the coefficient of correlation

$r =$ coefficient of correlation

$r = S_{xy} / (S_x \cdot S_y)$

Correlation coefficient = $\text{cov}(x,y) / (\text{std deviation}(x) \times \text{std deviation}(y))$

product of deviations of x and y series from their mean is zero

$\Rightarrow S_{xy} = 0$

$\Rightarrow r = 0$

Coefficient of correlation = 0

Ans: If the sum of the product of deviations of x and y series from their mean is zero, then the coefficient of correlation will be ZERO

Question 2

If the slope of the regression line is calculated to be 5.5 and the intercept 15 then the value of Y when X is 6 is

- (a) 88 (b) 48
(c) 18 (d) 78

Answer: Options (b)

Explanation:

The value of Y when X is 6

$a+bX$

$15+5.5(6)$

Ans: 48

Question 3

If $y = 9x$ and $X = 0.01Y$, then r is equal to:

- (a) -0.1 (b) 0.1
(c) 0.3 (d) -0.3

Answer: Options (c)

Question 4

The straight - line graph of the linear equation $Y = a + b X$, slope is horizontal if:

- (a) $b = 1$ (b) $b \neq 0$
(c) $b = 0$ (d) $a = b \neq 0$

Answer: Options (c)

Question 5

If $b_{xy} = -1.6$ and $b_{yx} = -0.4$, then r_{xy} will be

- (a) 0.4 (b) -0.8
(c) 0.64 (d) 0.8

Answer: Options (b)

DEC 2021**Question 1**

If the data points of (X,Y) series on a scatter diagram lie along a straight line that goes downwards as X-values move from left to right, then the data exhibit -----
-----correlation.

- (a) Direct (b) Imperfect indirect
(c) Indirect (d) Imperfect direct

Answer: c

Explanation:

The regression coefficients remain unchanged due to

- (a) Shift of origin (b) Shift of scale
(c) Always (d) Never

Answer: a

Explanation:

The regression coefficient remain uncharged due to shift of origin.

JUNE 2022

Question 1

If Coefficient of correlation for $3X+ 4y = 6$ is 0.5. Find the coefficient of correlation for of $3u+ 9v = 7$ for u and v.

- (a) -(0.5) (b) (0.5)
(c) \neq 0.5 (d) 0.25

Answer: b

Explanation:

We know that shift of scale coefficient of (under consideration) then $r_{xy} = r_{uv} = 0.5$ correlation is change

Question 2

Karl Pearson Correlation Coefficient method is used for -

- (a) Any data (b) Scattered data
(c) Grouped data (d) Ungrouped data

Answer: d

Explanation:

Karl Pearson Correlation Coefficient method is used for ungrouped data.

Question 3

If the plotted point in a scatter diagram lie from lower left to upper right then correction is:

- (a) Positive (b) Negative
(c) Perfectively Negative (d) Zero

Answer: a

Explanation:

If the plotted point in a scatter diagram lie from lower left to upper right then it is said to be positive correlation.

Question 4

If concurrent coefficient is $\frac{1}{\sqrt{3}}$. If sum of deviation is n 6 for n pairs of data?

- (a) 9 (b) 8
(c) 10 (d) 11

Answer: c

Explanation:

Given $r_c = \frac{1}{\sqrt{3}}$, $n = ?$

$C = 6$

Coeff of concurrent deviation

$$r_c = \pm \sqrt{\frac{2c - m}{m}}$$

$$\frac{1}{\sqrt{3}} = \pm \sqrt{\frac{2 \times 6 - m}{m}}$$

On squaring both side

$$\left[\frac{1}{\sqrt{3}}\right]^2 = \left[\pm \sqrt{\frac{12 - m}{m}}\right]^2$$

$$\frac{1}{3} = \frac{12 - m}{m}$$

$$m = 36 - 3m$$

$$m + 3m = 36$$

$$4m = 36$$

$$m = \frac{36}{4} = 9$$

$$n = m + 1 = 9 + 1 = 10$$

Question 5

Which of the following is used to find correlation between two qualitative characteristics

- (a) Karl Pearson
(b) Spearman rank correlation
(c) Concurrent deviation
(d) Scatter diagram

Answer: b

Explanation:

Spearman's rank correlation coefficient is used to find correlation between two qualitative characteristics.

Question 6

Scattered diagram is used to plot

- (a) Quantitative data
(b) Qualitative data
(c) Discrete data
(d) Continuous data

Answer: a

Explanation:

Scattered diagram is used to plot quantitative data.