

NORMAL DISTRIBUTIONS If a continuous random variable has a distribution with a graph that is symmetric and Curve is bell-shaped NORMAL and symmetric bell-shaped and can be DISTRIBUTIONS described by the equation  $y = \frac{e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}}{\sigma\sqrt{2\pi}}$ M Value we say that it has a normal distribution. **Properties of the Normal Distribution** The normal distribution curve is bell-shaped. The mean, median, and mode are equal and located at the center of the distribution. The normal distribution curve is unimodal (single mode). The curve is symmetrical about the mean. The curve is continuous. The curve never touches the x-axis. The total area under the normal distribution curve is equal to 1 or 100%. **The Standard Normal Distribution STANDARD** If each data value of a normally distributed random **NORMAL** variable x is transformed into a z-score, the result will be the standard normal distribution. DISTRIBUTION Standard Normal Normal Distribution Distribution  $z = \frac{x - \mu}{2}$ a LL. μ=0 Use the Standard Normal Table to find the cumulative area under the standard normal curve.

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### **POISSON DISTRIBUTION:**

### **Question1**

In a Poisson Distribution, if 'n' is the number of trials and 'p' is the probability of success, then the mean value is given by (b) m =  $(np)^2$ (a) m = n p

(c) m = n p (1-p)

(d) m = p

### Answer: a

**Explanation**:

For a discrete probability function, the mean value or the expected value is given by

Mean  $(\mu) = \sum_{x=0}^{n} xp(x)$ 

For Poisson Distribution P(x) =  $\frac{e^{-m_m x}}{x!}$  substitute in above equation and solve to get  $\mu$  = m = n p.

### **Question2**

If 'm' is the mean of A Poisson Distribution, then variance is given by (a)  $m^2$ (b)  $m_{\frac{1}{2}}^{1}$ (d)  $m_{/2}^2$ (c) m **Answer: c** 

### **Explanation:**

For a discrete probability function, the variance is given by Variance (v) =  $\sum_{x=0}^{n} x^2 p(x) - \mu^2$ 

Where  $\mu$  is the mean, substitute P(x) =  $\frac{e^{-m_m x}}{x!}$ , in the above equation and put  $\mu$  = m to obtain V = m

### **Ouestion 3**

The p.d.f of Poisson Distribution is given by (a)  $\frac{e^{-m_m x}}{m_m x}$ (b)  $\frac{e^{-m}x!}{m^x}$ (a)  $\frac{x!}{x!}$ (c)  $\frac{x!}{m^x e^{-m}}$ (d)  $\frac{e^m m^x}{m^x}$ Answer: a

### **Explanation**:

This is a standard formula for Poisson distribution, is needs no explanation. Even though if you are interested to know the derivations in detail, you can refer to any of the books or source on internet that speaks of this matter.

### Question 4

If 'm' is the mean of a Poisson distribution, the standard deviation is given by

(a) $m^{1/2}$	<b>(b)</b> m <sup>2</sup>
(c) m	(d) $m/_2$

### Answer: a

Explanation:

The variance of a Poisson distribution with mean 'm' is given by V = m, hence standard Deviation =  $(Variance)^{1/2} = m^{1/2}$ 

### **Question 5** In a Poisson distribution the mean and variance are equal (b) False (a) True (d) Not justifiable (c) Can't say Answer: a **Explanation**: Mean = mVariance = m $\therefore$ Mean = Variance. **Ouestion 6** In a Poisson distribution, if mean (m) = e, then P(x) is given by (b) $\frac{e^{-m_{x!}}}{m^x}$ (d) $\frac{e^{m_m x}}{x!}$ (a) $\frac{e^{-m_m x}}{\frac{x!}{x!}}$ (c) $\frac{x!}{m^x e^{-m}}$ **Answer:** a **Explanation:** Put m = e. $P(x) = \frac{e^m m^x}{x!}$ **Ouestion 7 Poisson distribution is applied for** (a) Continuous Random variable(b) Discrete Random variable(c) Irregular Random variable(d) Uncertain Random Variable (c) Irregular Random variable (d) Uncertain Random Variable **Answer: b Explanation:**

Poisson distribution along with Binomial Distribution is applied for discrete Random variable. Speaking more precisely, Poisson Distribution is an extension of Binomial Distribution for larger values 'n'. since Binomial Distribution is of discrete nature, so is its extension Poisson Distribution.

### **Question 8**

If 'm' is the mean of Poisons Distribution, the P(0) is given by

(a) e<sup>-m</sup> (c) e **Answer:** a **Explanation:**  $P(x) = \frac{e^{-m_m x}}{x!}$ Put x = 0, to obtain  $e^{-m}$ .

**Question 9** In a Poisson distribution, the mean and standard deviation are equal (a) True (b) False (c) Can't say (d) Not justified

### **Answer: b**

**Explanation:** In a Poisson distribution, Mean = m Standard deviation =  $m^{1}/_{2}$ : Mean and Standard deviation are not equal.

### **Question 10**

For a Poisson distribution, if mean (m) = 1, then P(1) is (a)  $\frac{1}{-}$ (b) e (c)  $\frac{\breve{e}}{2}$ (d) Indeterminate Answer: a **Explanation:**  $P(x) = \frac{e^{-m_m x}}{x!}$ Put m = x = 1, (given) to obtain 1/e.

### **Ouestion 11**

The recurrence relation between P(x) and P(x+1) in a Poisson distribution is given by (a) P(x+1) - m P(x) = 0(b) m P(x+1) - P(x) = 0

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(b) e<sup>m</sup> (d) m<sup>-e</sup>

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(c) (x+1) P(x+1) -m P(x) = 0 **Answer: c Explanation:**   $P(x) = \frac{e^{-m_m x}}{x!}$  $P(x+1) = e^{-m \frac{m^{x+1}}{(x+1)!}}$ 

Divide P(x + 1) by P(x) and rearrange to obtain (x+1) P(x+1) - m P(x) = 0.

### Question 12

The mean value for an event X to occur is 2 in a day. Find the probability of event X to occur thrice in a day.

(a) 0.1804
(c) 0.18
Answer: b
Explanation:
Mean, m=2 x = 3

(b) 0.1804465 (d) None

Probability of the event to occur thrice, P (3; 2) =  $e^{-2} \frac{2^3}{3!} = 0.1804465$ 

### **Question 13**

A man was able to complete 3 files a day on an average. Find the probability that he can complete 5 files the next day.

(a) 0.108	(b) 0.1008
(c) 0.008	(d) None
Answer: b	

### **Explanation**:

Here we know this is a Poisson experiment with following values given:  $\mu = 3$ , average number of files completed a day

X = 5, the number of files required to be completed next day

And e = 2.71828 being a constant

On substituting the values in the Poisson distribution formula mentioned above we get the Poisson probability in this case.

We get

P(x, 
$$\mu$$
) =  $\frac{(e^{-\mu})(\mu^{x})}{x!}$   
→ P (5, 3) =  $\frac{(2.71828)^{-3}(3^{5})}{5!}$ 

= 0.1008 approximately.

Hence the probability for the person to complete 5 files the next day is 0.1008 approximately.

### Question 14

The number of calls coming per minute into a hotels reservation center is Poisson random variable with mean 3. Find the probability that no calls come in a given 1-minute period

(a)  $e^{-3}$  (b)  $e^{3}$  (c) e (d)  $m^{-e}$ **Answer: a** 

### **Explanation**:

Let x denote the number of calls coming in that given 1 minute period. X ~ Poisson(3)

 $P(x = 0) = \frac{e^{-3}3^{0}}{0!}$  $= e^{-3}$ 

### Question 15

If the random variable X follows a Poisson distribution with mean 3,4, find P(x=6)

(a) 0.071604409
(c) 0.0023698
A

(b) 0.00125948 (d) 0.015792

### Answer: a

**Explanation**:

This can be written more quickly as : if X = Po(3,4) Find (x = 6) Now  $P(x = 6) = \frac{e^{-\lambda}\lambda^6}{6!}$ 

 $=\frac{e^{-3.4}(3.4)^6}{6!} \text{ (mean, } \lambda = 3.4\text{)}$ = 0.071604409 or 0.072(to 3 d.p.)

### **BINOMIAL DISTRIBUTION:**

### Question 1

In a binomial Distribution, 'if 'n' is the number of trials and 'p' is the probability of success, then the mean value is given by

(a) np (b) n (c) p (d) np(1 - p) Answer: a

### Explanation:

For a discrete probability function, the mean value or the expected value is given by

Mean ( $\mu$ )  $\sum_{x=0}^{n} xp(x)$ 

For Binomial Distribution  $P(x) = {}^{x}C_{x} p^{x} q^{(n-x)}$ , substitute in the above equation and solve to get  $\mu = np$ .

### **Question 2**

### In the Binomial Distribution, If p, q and n are probability of success, failure and number of trials respectively then variance is given by

(a) np (b) npq (c) np<sup>2</sup>q (d) npq<sup>2</sup> **Answer: b Explanation:** For a discrete probability function, the variance is given by Variance  $(V) = \sum_{x=0}^{n} x^2 p(x) - \mu^2$ Where  $\mu$  is the mean, substitute  $P(x) = P(x) = {}^{x}C_{x} p^{x} q^{(n-x)}$ , in the above equation and put  $\mu$  = np to obtain V = npq.

### **Question 3**

If 'x' is a random variable, taking values 'x' probability of success and failure being 'p' and 'q' respectively and 'n' trials being conducted, then what is the probability that 'x' takes values 'x'? Use Binomial Distribution

(a)  $P(X = x) = {}^{n}C_{x} p^{x}q^{x}$  (b)  $P(X = x) = {}^{n}C_{x} p^{x} q^{(n-x)}$ (c)  $P9X = x) = {}^{n}C_{x} p^{x} q^{(n-x)}$  (d)  $P(x = x) = {}^{x}C_{n}p^{x}q^{x}$  **Answer: b Explanation:** It is the formula for Binomial Distribution that is asked here which is given by P(X)

 $= x) = {}^{n}C_{x} p^{x} q^{(n-x)}$ 

### **Question 4**

If 'p', 'q' and 'n' are probability of success, failure and number of trials respectively in a Binomial Distribution, what is its standard Deviation?

(a) $(np)^{1/2}$	(b) $(pq)^{1/2}$
(c) $(np)^2$	(d) $(npq)^{1/2}$
Answer: d	
Explanation:	
The variance (V) for a Binomial Distribution	ition is given by V = npq

### **Question 5**

(a) True	(b) False
(c) can't say	(d) Not justifiable

### Answer: b

Explanation: Mean = np Variance = npq ∴ Mean and Variance are not equal.

### Question 6

### It is suitable to use Binomial Distribution only for

(a) Large value of 'n'(c) Small values of 'n'

(b) Fractional values of 'n'(d) Any values 'n'

#### Answer: c Explanation:

As the value of 'n' increase, It becomes difficult and tedious to calculate value of  ${}^{n}C_{x}$ .

### **Question 7**

### For larger values of 'n' Binomial Distribution

(a) Loses its discreteness
(b) Tends to Poisson Distribution
(c) Stays as it is
(d) Gives oscillatory values

Answer: b
Explanation:
Where m = np is the mean of Poisson Distribution.

### **Question 8**

### In a Binomial Distribution, if **p** = **q**, then P(X = x) is given by

(a)  ${}^{n}C_{x}(0.5)^{n}$ (c)  ${}^{n}C_{x}p^{(n-x)}$  (b)  ${}^{x}C_{n}(0.5)^{n}$ (d)  ${}^{x}C_{n}p^{(n-x)}$ 

### Answer: a

**Explanation:** If p = q then p = 0.5Substituting in  $P(x) = {}^{n}C_{x} p^{x} q^{(n-x)}$  we get  ${}^{n}C_{x} (0.5) {}^{n}$ .

Question 9Binomial Distribution is a(a) Continuous distribution(b) Discrete distribution(c) Irregular distribution(d) Not a Probability distributionAnswer: bExplanation:It is applied to a discrete Random variable, hence it is discrete distribution

### **Question 10**

# 15 dates are selected at random, what is the probability of getting two Sundays?

(a) 0.29	(b) 34
(c) 56	(d) 78

### Answer: a

### **Explanation**:

If X denotes the number at Sundays. Then it is obvious that X follows binomial distribution with parameter n = 15 and p = probability of a Sunday in a week =  $\frac{1}{7}$ 

and 
$$q = 1 - p = \frac{6}{7}$$
  
Then f (x) =  $15_{c_x} \left(\frac{1}{7}\right)^x \cdot \left(\frac{6}{7}\right)^{15-x}$   
For x = 0, 1, 2 ...... 15.  
Hence the probability of getting two Sundays  
= f(2)  
=  $15_{c_2} \left(\frac{1}{7}\right)^2 , \left(\frac{6}{7}\right)^{15-2}$   
=  $\frac{10^5 \times 6^{13}}{7^{15}}$   
= 0.29

### **Question 11**

# The incidence of occupational disease in an industry is such that the workmen have a 10% chance of suffering from it. What is the probability that out of 5 workmen, 3 or more will contract the disease?

(a) 890

(c) .00086

(b) .0086 (d) None

#### Answer: c Explanation:

Let x denote the number of workmen in the sample. X follows binomial with parameters n = 5 and p = probability that a workman suffers from the occupational disease = 0.1 Hence q = 1 - 0.1 = 0.9 Thus f (x) =  $5_{c_x}$  (0.1)<sup>x</sup> . (0.9)<sup>5-x</sup> For x = 0, 1, 2 .....5. The probability that 3 or more workmen will contract the disease = P (x  $\ge$  3) = f (3) + f (4) + f (5) =  $5_{c_3}$  (0.1)<sup>3</sup> (0.9)<sup>5-3</sup> +  $5_{c_4}$  (0.1)<sup>4</sup> . (0.9) <sup>5-4</sup> +  $5_{c_5}$  (0.1) <sup>5</sup> = 10 × 0.001 × 0.814 + 5 × 0.0001 × 0.9 + 1 × 0.00001

= 0.0081 + 0.00045 + 0.00001

= 0.0086.

### **Question 12**

Find the probability of a success for the binomial distribution satisfying the following relation 4 P (x = 4) = P (x = 2) and having the parameter n as six. (a)  $P \neq 1$ (b)  $P \neq -1$ (d) P = 0(c) P = 1**Answer: b Explanation**: We are given that n = 6. The probability mass function of x is given by  $F(x) = n_{c_x} p^x q^{n-x} = 6_{c_x p^x q^{n-x}}$ For  $x = 0, 1 \dots, 6$ , Thus P(x = 4) = f(4); $= 6_{c_4} p^4 q^{6-4} = 15 p^4 q^2$ And P(x = 2) = f(2) $= 6_{c_4} p^2 q^{6-2} = 15 p^2 q^4$ Hence 4 P (x = 4) = P (x = 2) $= 60 p^4 q^2 = 15 p^2 q^4$  $= 15 p^2 q^2 (4p^2 - q^2) = 0$  $=4p^2 - q^2 = 0$  (as p ? 0, q ? 0)  $=4p^{2} - (1 - p)^{2} = 0$  (as q = 1 - p) = (2p + 1 - p) = 0 or (2p - 1 + p) = 0 $= p = -1 \text{ or } p = \frac{1}{2} \text{ thus } p = \frac{1}{2} (\text{as } p \neq -1)$ 

### **NORMAL DISTRIBUTION:**

### **Question 1**

### Normal distribution is applied for

(a) Continuous Random Distribution(c) Irregular Random VariableAnswer: a

(b) Discrete Random Variable(d) Uncertain Random Variable

### Explanation:

Normal Distribution is applied for Continuous Random Distribution. A discrete probability distribution is a probability distribution characterized by a probability mass function. Thus, the distribution of a random variable x is discrete, and x is called a discrete random variable, if, as u runs through the set of all possible values of x.

### **Question 2**

# **The shape of the Normal curve is** (a) Bell shaped

(c) Circular Answer: a (b) Flat (d) Spiked

### **Explanation**:

Due to the nature of the probability Mass function, a bell shaped curve is obtained.

### **Question 3**

### Normal Distribution is symmetric is about

(a) Variance	(b) Mean
(c) Standard deviation	(d) Covariance
Answer: b	

### Explanation:

Due to the very nature of p.m.f of Normal Distribution, the graph appears such that it is symmetric about its mean.

### **Question 4**

### For a standard normal variate, the value of mean is

(a) ∞	(b) 1
(c) 0	(d) Not defined
Answer: c	

### Explanation:

For a normal variate, if its mean = 0 and standard deviation = 1, then its called as standard Normal variate. Here, the converse is asked.

### **Question 5**

### The area under a standard normal curve is (a) 0 (b) 1 (c) $\infty$ (d) Not defined Answer: b Explanation:

For any probability distribution, the sum of all probabilities is 1. Area under normal curve refers to sum of all probabilities.

### **Question 6**

### The standard normal curve is symmetric about the value.

(a) ∞	(b) 0
(c) 0.5	(d) 1
Americans	

### Answer: b

**Explanation**:

Normal curve is always symmetric about mean, for standard normal curve or variate mean = 0.

### Question 7

### For a standard normal variate. The value of standard deviation is

	(b) 1 (d) Not defined
(c) ∞ Answer: b	(d) Not defined
Explanation:	
-	ion of a normal variate are 0 and 1 respectively, it
is called as standard normal var	
Ouestion 8	
Normal Distribution is also kr	iown as
(a) Cauchy's Distribution	(b) Laplacian Distribution
(c) Gaussian Distribution	(d) Lagrangian Distribution
Answer; c	
Explanation:	
Named after the one who propo	sed it. For further details, refer to books or
internet.	
Question 0	
Question 9 Skewers of Normal distribution	on is
(a) Negative	(b) Positive
(c) 0	(d) Undefined
Answer: c	
Explanation:	
Since the normal curve is symm	etric about its mean, its skewness is zero. This is a
theoretical explanation for math	nematical proofs, you can refer to books or
website that	
Speak on the same in detail.	
Question 10	
Question 10 For a normal distribution its I	nean, median, mode are equal
-	<b>nean, median, mode are equal</b> (b) False
For a normal distribution its i	
<b>For a normal distribution its i</b> (a) True	(b) False
For a normal distribution its i (a) True (c) Not defined	(b) False
For a normal distribution its i (a) True (c) Not defined Answer: a Explanation:	(b) False
For a normal distribution its it (a) True (c) Not defined Answer: a Explanation: It has theoretical evidence that it	(b) False (d) Can't say
For a normal distribution its it (a) True (c) Not defined Answer: a Explanation: It has theoretical evidence that it	(b) False (d) Can't say requires some serious background on several
For a normal distribution its in (a) True (c) Not defined Answer: a Explanation: It has theoretical evidence that in topics for more details you can in same.	(b) False (d) Can't say requires some serious background on several
For a normal distribution its in (a) True (c) Not defined Answer: a Explanation: It has theoretical evidence that is topics for more details you can in same. Question 11	(b) False (d) Can't say requires some serious background on several refer to any book or website that speaks on the
For a normal distribution its in (a) True (c) Not defined Answer: a Explanation: It has theoretical evidence that is topics for more details you can it same. Question 11 In Normal distribution, the high	(b) False (d) Can't say requires some serious background on several refer to any book or website that speaks on the ghest value of ordinate occurs at
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For a normal distribution its i (a) True (c) Not defined Answer: a Explanation: It has theoretical evidence that is topics for more details you can is same. Question 11 In Normal distribution, the his (a) Mean (c) Extremes	(b) False (d) Can't say requires some serious background on several refer to any book or website that speaks on the ghest value of ordinate occurs at (b) Variance

This is due the behavior of the pdf of Normal distribution.

<u>Question 12</u> The shape of the normal curve de	nends on its
(a) Mean deviation	(b) Standard deviation
(c) Quartile deviation	(d) None
Answer: b	
Explanation:	
This can be seen in the pdf on the no is a variable.	ormal distribution where standard deviation
Question 12	

#### Question 13

### The value of constant 'e' appearing in normal distribution is

(b) 2.7836
(d) None

#### **Explanation**:

This is a standard constant.

### **Question 14**

### In standard normal distribution, the value of median is

(a) 1	(b) 0
(c) 2	(d) Not fixed

### Answer: b

### **Explanation**:

In a standard normal distribution the value of mean is 0 and in normal distribution mean, median and mode coincide.

#### Question 15

### In a certain book, the frequency distribution of the number of words per page may be taken as approximately normal with mean 800 and standard deviation 50. If three pages are chosen at random, what is the probability that none of them has between 830 and 845 words each?

(a) 0.7536	(b) .7654
(c) .9084	(d) .8733

# Answer: a Explanation:

Let X be a normal variate which denotes the number of words per page. It is given that X – N (800, 50).

The probability that a page, select at random, does not have number of words between 830 and 845, is given by

1-P (830< X < 845) 1 - P  $\left(\frac{830-800}{50} \le < \frac{845-800}{50}\right)$  $= 1 - P(0.6 \le 0.9) = 1 - P(0 \le 0.9) + P(0 \le 0.6)$ = 1 - 0.3159 + 0.2257 = 0.9098 = 0.91

Thus, the probability that none of the three pages, selected at random, have number of words lying between 830 and 845 = (0.91)3 = 0.7536.

### **Ouestion 16**

The distribution of 1,000 examines according to marks percentage is given **below**:

% Marks	less than 40	40-75	75 or more	Total
No. ofexamines	430	420	150	1000

Assuming the marks percentage to follow a normal distribution, calculate the mean and standard deviation of marks. If not more than 300 examines are to fail, what should be the passing marks?

•	
(a) 30%	(b) 40%
(c) 50%	(d) None

### **Answer:** a

### **Explanation**:

Let X denotes the percentage of marks and its mean and S.D. be m and s respectively. From the given table, we can write

P(x < 40) = 0.43 and  $P(X \ge 75) = 0.15$ , which can also be written as

$$P\left(=<\frac{40-\mu}{\sigma}\right) = 0.43 \text{ and } P\left(=\geq \frac{75-\mu}{\sigma}\right) = 0.15$$

The above equations respectively imply that

$$\frac{40-\mu}{\sigma} = -0.175 \text{ or } 40 - \mu = -0.175\sigma \qquad \dots (1)$$

$$\frac{75-\mu}{\sigma} = 1.04 \text{ or } 75 - \mu = 1.040' \qquad \dots (2)$$

And  $\frac{75-\mu}{\alpha} = 1.04 \text{ or } 75 - \mu = 1.040^{\circ}$ 

Solving the above equations simultaneously, we get  $\mu$  = 45.04 and O = 28.81 Let x, be the percentage or marks required to pass the examination.

Then we have P (x < x<sub>1</sub>) = 0.3 or P (= 
$$<\frac{x_1 - 45.04}{28.81}$$
) = 0.3  
 $\therefore \frac{x_1 - 45.04}{28.81}$  = - 0.525  $\rightarrow x_1$  - 29.91 or 30% (approx)

### **Ouestion 17**

At a petrol station, the mean quantity of petrol sold to a vehicle is 20 litres per day with a standard deviation of 10 liters. If on a particular day, 100 vehicles took 25 or more litres of petrol, estimate the total number of vehicles who took petrol from the station on the day. Assume that the quantity of petrol taken from the station by a vehicle is a normal variate. (a) 333 (b) 343

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(c) 324 (	d) 567
Answer: c	
Examination:	
Let X denote the quantity of petrol taken	by a vehicle. It is given that X – N (20,
10).	
∴ P (X ≥ 25) = P (= ≥ $\frac{25-20}{10}$ ) = P (= ≥ 0.5	5)
$= 0.5000 - P(0 \le = \le 0.5)$	) = 0.5000 - 0.1915 = 0.3085
Let N be the total number of vehicles taki	ng petrol on that day.
:. $0.3085 \times N = 100 \text{ or } N = \frac{100}{0.3085} = 324 \text{ (a)}$	pprox.)

<u>Question 18</u> Using the table areas under the standard normal curve, find the following probabilities:

(i) P ( $0 \le z \le 1.3$ ) (ii) P ( $-1 \le z \le 0$ ) (iii) P ( $-1 \le z \le 12$ ) (a) 0 0.4032, 0.3413,0.8185 (c) 0.40456, 0.3456,0.8155

(b) 0.4072, 0.4413,0.8185 (d) None

### Answer: a

**Explanation**:

The required probability, in each question, is indicated by the shaded are of the corresponding figure.

(a) From the table.

(b) (i) we can write  $P(0 \le z \le 1.3) = 0.4032$ .

(c) (ii) we can write  $P(-1 \le z \le 1)$ , because the distribution is symmetrical.

### Question 19

### Determine the value or values of z in the following situations: (i) Area between 0 and z is 0.4495.

(ii) Area between -  $\infty$  to z is 0.1401.

(a) -1.64, -1.08	(b) -1.08, -1.64
(c) 1.64, 1.08	(d) -1.64, 1.08
Answer: a	
Explanation:	
(i) On locating the value of z correspon	nding to an entry of area 0.4495 in the table
of areas under the normal curve, we h	ave z = 1.64 we note that same situations
may correspond to a negative value of	z. Thus, z can be 1.64 or – 1.64.

(ii) Since the area between  $-\infty$  to z<0.5, z will be negative. Further, the area between z and 0 = 0.5000 – 0.1401 = 0.3599. On locating the value of z corresponding to this entry in the table, we get z = -1.08



# <u>MAY 2018</u>

Question 1	
The variance of a binomial distribut	
(a) $np^2(1-p)$	(b) $nq(1-q)$
(c) $\sqrt{np - (1-p)}$	(d) $n^2 p^2 (1-p)^2$
Answer: b	
Explanation:	
= npq	
= nqp	
= nq(1-q)	
Question 2	
X is a passion variate satisfying the f	ollowing condition 9 P(X = 4) + 90 (X = 6) = P
(X = 2). What is the value of P (X $\leq$ 1)	)?
(a) 0.5655	(b) 0.5655
(c) 0.7358	(d) 0.8835
Answer: c	
Explanation:	
Given $X \sim P(m)$	
P(x = 2) = 9 P(x = 4) + 90 P(x = 6)	
$\frac{e^{-m}.m^2}{2!} = +\frac{9.e^{-m}.m^4}{4!} + \frac{90.e^{-m}.m^e}{2!}$	
2. 1. 2.	
$\frac{90.e^{-m}.m^{e}}{2!} + \frac{9.e^{-m}.m^{4}}{4!} - \frac{e^{-m}.m^{2}}{2!} = 0$	
2! 4! 2!	
$e^{-m} \cdot m^2 \left[ \frac{90 \cdot m^4}{6!} + \frac{9m^2}{4!} - \frac{1}{2!} \right] = 0$	
$\begin{bmatrix} 2 & 1 \\ 6 \end{bmatrix} \begin{bmatrix} 4 \\ 2 \end{bmatrix} \begin{bmatrix} 2 \\ 0 \end{bmatrix}$	
$e^{-m} \cdot m^2 \left[ \frac{90 \cdot m^4}{6!} + \frac{9m^2}{4!} - \frac{1}{2} \right] = 0$	
$e  .m  \left[ \frac{-6!}{6!} + \frac{-4!}{4!} - \frac{-2}{2} \right] = 0$	
$e^{-m} \cdot m^2 \left[ \frac{90 \cdot m^4}{6!} + \frac{9m^2}{4!} - \frac{1}{2} \right] = 0$	
$e^{-m} \cdot m^2 \left[ \frac{m^4}{8} + \frac{3m^2}{8} - \frac{1}{2} \right] = 0$	
$\frac{e^{-m}}{2} \left[ \frac{m^4 + 3m^2 - 4}{4} \right] = 0$	
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 $\frac{e^{m} \cdot m^2}{8} (m^4 + 3m^2 - 4) = 0$  $m^4 + 4m^2 - m^2 - 4 = 0$  $m^2 (m^2 + 4) - 1 (m^2 + 4) = 0$  $(m^2 + 4) (m^2 - 1) = 0$ If  $m^2 + 4 = 0$  if  $m^2 - 1 = 0$  $m^2 = -4$  if  $m^2 = +1$  $m^2 = \neq \sqrt{1}$ m = (:: m > 0) $P(x \le 1) = P(x = 0) + P(x = 1)$  $=\frac{e^{-1} \cdot 1^{0}}{0!} + \frac{e^{-1} \cdot 1!}{1!} = \frac{1}{e} + \frac{1}{e} = \frac{2}{e}$  $\frac{2}{2.7182} = 0.7358$ 

### **Question 3** What is the first quartile of x having the following probability of function?

 $f(x) \frac{1}{\sqrt{72x}} e^{-(x-10)^{\frac{2}{72}}}$  for - $\infty < x < \infty$ (a)4 (b) 5 (c) 5.95 (d) 6.75 Answer: c **Explanation:** Given:  $f(x) \frac{1}{\sqrt{72x}} e^{-(x-10)^{\frac{2}{72}}}$  for -∞<x<∞  $f(x) \frac{1}{\frac{6}{\sqrt{2x}}} e^{-(x-10)^{\frac{2}{72}}}$ on company  $f(x) \frac{1}{\sqrt[6]{2x}} e^{\frac{-(x-\mu)^2}{2(o')^2}}$ we get  $0' = 6, \mu = 10$ First quartile  $Q_1 = \mu - 0.6750^{\circ}$ = 10-0.675×6 = 10-4.05= 5.95 **Question 4** An example of bi-parametric discrete probability distribution is (a) Binomial distribution (c) Normal distribution

(b) Poisson distribution (d) Both a and b

#### Answer: d

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Explanation:			
-	an example of a bi- parametric dis	crete probability distribution.	
Our action F			
Question 5 Probability distribution	n may ha		
<b>Probability distribution</b> (a) Discrete	(b) Continuous		
(c) Infinite	(d) a or b		
Answer: d			
Explanation:			
-	nay be discrete or continuous.		
Question 6			
	normal curve between <b>z</b> = 0 to <b>z</b>	x = 1 is 0.3413, then the	
<b>value of ø (1) is.</b>			
(a) $0.5000$	(b) 0.8413 (d) 1		
(c) -0.5000 Answer: b	(d) 1		
Explanation:			
The area of standard of normal curve between $z = 0$ to $z = 1$ is 0.3413 then			
$\emptyset(1) = 0.3413 + 0.5$			
0.8413			
	<b>NOV 2018</b>		
Question 1			
For a poisson variate X,	P(X = 2) = 3P(X = 4), then the s	standard deviation of X is	
(a) 2	(b) 4		
(c) $\sqrt{2}$	(d) 3		

Answer: c Explanation:

For Poisson Variate X,  $\frac{e^{-mm^{2}}}{2!} = \frac{3e^{-mm^{4}}}{4!}$   $\frac{m^{2}}{2} = \frac{3m^{4}}{4!}$   $6m^{4} = 24 m^{2}$   $m^{2} = \frac{24}{6}$   $m^{2} = 4$ 

m = 2<br/>S.D. =  $\sqrt{m} = \sqrt{2}$ 

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### Question 2

The mean of the Binomial distribution B  $(4, \frac{1}{3})$  is equal to (a)  $\frac{3}{5}$  (b)  $\frac{8}{3}$ (c)  $\frac{3}{4}$  (d)  $\frac{4}{3}$ 

(c)  $\frac{3}{4}$ Answer: d

Explanation: X<sub>4</sub> B (n, P) = B  $\left(4, \frac{1}{3}\right)$ We get n = 4, P =  $\frac{1}{3}$ Mean = np = 4 ×  $\frac{1}{3}$  =  $\frac{4}{3}$ 

#### **Question 3**

If for a normal distribution  $Q_1$  = 54.52 and  $Q_3$  = 78.86, then the median of the distribution is

(a) 12.17 (b) 12.17 (c) 66.369 (d) None **Answer: c Explanation:**   $Q_1 = 54.52 \text{ and } Q_3 = 78.86$ We know that  $Q_1 = \mu - 0.675 = 54.52$  (1)  $Q_3 = \mu - 0.675 = 78.86$  (2) On adding  $2\mu = 133.38$   $\mu = \frac{133.28}{2}$   $\mu = 66.69$ In normal distribution Mean, Median and mode are equal. So, Median = Mean = 66.369

#### **Question 4** What is the mean of X having the following density function?

 $F(X) = \frac{1}{\sqrt[4]{2X}} e\left(\frac{x-10}{32}\right)^e \text{for } -\infty < x < \infty$ (a) 10
(c) 40
Answer: a

**Explanation:** Given Normal distribution

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(b) 4 (d) None

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 $F(x) = \frac{1}{\sqrt[4]{2x}} e\left(\frac{x-10}{32}\right)^{e} \text{ for } -\infty < x < \infty$ On comparing from  $f(x) = \frac{1}{\sqrt[4]{2x}} e\left(\frac{x-10}{32}\right)^{e} \text{ for } -\infty < x < \infty$ on comparing from  $f(x) = \frac{1}{\sqrt[6]{2x}} e^{\frac{x-\mu}{2(0^{2})^{2}}}$ we get Mean  $(\mu) = 10$ 0' = 4

### <u>Question 5</u>

The probability that a student is not a Swimmer is  $\frac{1}{5}$ , then the probability that out of five student four are swimmer is

(d) None

(b)  $5_{C_1} \left(\frac{1}{5}\right)^4 \left(\frac{4}{5}\right)$ 

(a) $\left(\frac{4}{5}\right)$	(0)	
(c) 5 <sub>c4</sub>	$\left(\frac{4}{5}\right)^{1}$	$\left(\frac{1}{5}\right)^4$

Answer: c Explanation:

Given:

Probability that a student is not a swimmer (q) =  $\frac{1}{5}$ 

Probability that a student is a swimmer (P) =  $1 - q = 1 - \frac{1}{5} = \frac{4}{5}$ 

Total No. of student (n) = 5

P (Exactly 4 student are swimmer)

= P (x=4)  $5_{c_4} \left(\frac{4}{5}\right)^1 \left(\frac{1}{5}\right)^4 \{ \therefore P (x = n) = n_{c_{n,p^x}, q^{n-x}} \}$ 

### **MAY 2019**

 Question 1

 If mean and variance are 5 and 3 respectively then relation between p & q is

 (a) p > q
 (b) p < q</td>

 (c) p = q
 (d) p is symmetric

 Answer: b

 Explanation:

 If mean and variance are 5 and 3 respectively then relation between p & q is p < q</td>

 Question 2

FOR ENQUIRY – 6262969604		6262969699
If $V > x$ then mathematical expectation	nic	
If $Y \ge x$ then mathematical expectatio		
(a) $E(X) > E(Y)$	(b) $E(X) \le E(Y)$	
(c) $E(x) = E(Y)$	(d) $E(X)$ . $E(Y) = 1$	
Answer: b		
Explanation:		
$\mathrm{E}(\mathrm{X}) \leq E(Y)$		
Question 3		
4 coins were tossed 1600 times. What	t is the probability that all 4 coir	ns do not turn
head upward at a time?		
(a) $1600e^{-100}$	(b) $1000e^{-100}$	
(c) $100e^{-1600}$	(d) $e^{-100}$	
Answer: d		
Probability of Head $= 1/2$		
Probability of not head = $1/2$ = $1/2$ = $1/2$		
probability that all 4 coins do not turn he	and unward at a time	
= 1 - Probability that 4 coins turn head $u$		
	Ipwaru at a time	
$= 1 - {}^{4}C_{4}(1/2)^{4}(1/2)^{0}$		
= 1 - 1/16		
= 15/16		
15/16 is the probability that all 4 coins	do not turn head upward at a time	3
1600 * 15/16 = 1500		
1500 times all 4 coins do not turn head u	ipward at a time	
Question 4		
In distribution, mean = v	ariance:	
(a) Binomial	(b) Poisson	
(c) Normal	(d) None of these	
Answer: b	(u) Hole of these	
Explanation:		
Poisson; np=npq		
Np = mean		
Npq = variance		
Question 5		
In a Binomial Distribution, if p = q, the	en P(X = x) is given by	
(a) $n_{C_x}(0.5)^n$	(b) <sup>n</sup> C <sub>n</sub> (0.5) <sup>n</sup>	
(c) ${}^{n}C_{x} p^{(n-x)}$	(d) ${}^{n}C_{n}p^{(n-x)}$	
Answer: a	()r	
Explanation:		
If $p = q$ , then $p = 0.5$		
	$C  (O \in \mathbb{D})_n$	
Substituting in $P(x) = {}^{n}C_{x} p^{x}q^{(n-x)}$ we get ${}^{n}$		
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# <u>NOV 2019</u>

Question 1	
Area under $U = 30'$	
	(b) 99%
	(d) 99.37%
Answer: a	
<b>Explanation:</b>	$ u_{\alpha\alpha} _{\alpha\beta}$ of a normal variable lies between $(u_{\alpha}, 20)$
and $(u + 30')$ .	lues of a normal variable lies between (u - 30')
Thus probability that a value of x lies. Out	tside the limit is as low as
(100 - 99.73) = 0.27%	iside the milit is as low as
Question 2	
For a Poisson distribution:	
	(b) mean and variance are equal
	(d) Both a and b
Answer: b	
Explanation:	
(b) Poisson distribution is theoretical dis	crete probability distribution which can
describe many processes	
Mean is given by m i.e. $U = m$	
Variance is also given by m i.e. o <sup>2</sup> = m So in pass on distribution mean and varia	anco aro oqual
50 m pass on distribution mean and varia	ance are equal.
Question 3	
Find mode when n = 15 and p = $\frac{1}{4}$ in bir	nomial distribution?
(a) 4	(b) 4 and 3
	(d) 3.7
Answer: b	
Explanation:	
(b) In binomial distribution,	
m = (n + 1) p	
$m = (15 + 1) \times \frac{1}{4}$	
m = 4	
Since 4 is a integer so there will 2 modes	
4 and (4 – 1)	
Mode = 4 and 3	

**Ouestion 4** In Poisson distribution, if P (x = 2) =  $\frac{1}{2}$  p (x = 3) find m? (a) 3 (b)  $\frac{1}{6}$ (d)  $\frac{1}{3}$ (c) 6 Answer: c **Explanation**: (c) In Poisson distribution  $P(x = x) = \frac{e^{-m} m^2}{r!}$ Here P (x = 2) =  $\frac{1}{2}$  P(x = 3)  $\frac{e^{-m} m^2}{2!} = \frac{1}{2} \times \frac{e^{-m} m^3}{3!}$  $\frac{e^{-m} \cdot m^2}{2!} = \frac{1}{2} \times \frac{e^{-m} \cdot m^3}{3!}$  $\frac{m^2}{2} = \frac{1}{2} \times \frac{m^3}{6}$  $m^2 = \frac{2}{12} = \frac{1}{6}m^3$  $m^{-1}\frac{1}{6}$  $\frac{1}{m} = \frac{1}{6} = m = 6$ **Question 5** In a binomial distribution B(n, p)  $n = 4 P(x = 2) = 3 \times P(x = 3)$  find P (a)  $\frac{1}{2}$ (b)  $\frac{2}{3}$  $(d)\frac{4}{2}$  $(c) \frac{1}{4}$ Answer: a **Explanation**: We know  $P(x = 1) = {}^{n}C_{r}(p)^{r}(q)^{n-r}$ Here p(x = 2) = 3 P(x = 3) $\frac{4_{c_2}(p)^2(q)^{4-2} = 3 \times {}^4c_3(p)^3(q)^1}{\frac{4!}{(4-2)1\times 2!}(p)^2(1-p^2 = 3 \times \frac{4!}{(4-3)1\times 3!} \times (p)^3(1-p))}$ Since  ${}^{n}C_{r} = \frac{n!}{(n-r)!1 \times r!}$  $6 \times (1 - p) = 3 \times 4 p$ 6 - 6p = 12p18 p = 6 $P = \frac{1}{2}$ For more Info Visit - www.KITest.in

$q=1-\frac{1}{3}=\frac{2}{3}$	
What is the SD and mean	
X if $f(x) = \frac{\sqrt{2}}{\sqrt{11}} \cdot e^{\frac{x - \mu}{2 o'^2}}$	(1)
Here, $\sqrt{\frac{2}{\pi}} \cdot e^{-2}(x-3)^2$	
$=\sqrt{\frac{2}{\Pi}} \cdot e - \left(\frac{1-3}{\frac{1}{2}}\right)^2$	
	(4)
On comparing with equation	
$2 0^2 = \frac{1}{2} u = 3$	
$O^2 = \frac{1}{4}$	
$0 = \frac{1}{2}$	
So SD = $\frac{1}{2}$ , mean = 3	
2	
_	
	<u>EC 2020</u>
Question1	
Which of the following is uni-param (a) Normal	(b) Poisson
(c) Binomial	(d) Hyper geometric
Answer: b	
Explanation:	
Poisson distribution is uniparametric ( mean=np	distribution. the parameter is m which is
incan-np	
Question2	
	omial distribution is less than one – half, then
the binomial distribution (a) Is skewed to left	(b) Is skewed to right
(c) Has two modes	(d) Has median at a point > mean +
	1/2
Answer: b	
Explanation:	
Is skewed to right	
Question3	
	distribution the Sharpe of probability
<b>curve does not change.</b> (a) Binomial	(b) Normal
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(c) Poisson	(d) Non – Gaussian
Answer: b	
Explanation:	
-	rmal distribution the Sharpe of probability curve
does not change.	
Question4	
Which one of the following has Poiss	
(a) The number of days to get a	(b) The number of defects per meter
complete	on
cure	Long rollOf coated polythene sheet.
(c) The errors obtained in repeated	(d) The number of claims rejected
Measuring of The length of a rod.	by an Insurance agency.
Answer: b	insurance agency.
Explanation:	
The number of defects per meter on lo	ng roll of coated polythene sheet.
Question5	
-	$X_{1}$ , we hve $P(X = 7) = 8$ . $P(X = 9)$ , the mean of the
distribution is	
(a) 4	(b) 3
(c) 7	(d) 9
Answer: b	
Explanation:	
$P(X = n) = \frac{\lambda^7 e^{-\lambda}}{7!} = \frac{8 \cdot \lambda^9 e^{-\lambda}}{9!} \frac{9!}{7! \times 8} \lambda^2$	
$\lambda = 3$	
Question6	
-	listribution with mean 10 and standard
deviation 4 is	(h) 22 20
(a) 54.24 (c) 0.275	(b) 23.20 (d) 2.70
Answer: d	(u) 2.70
Explanation:	
In normal distribution, quartile deviati	ion is related to standard deviation as
Q.D. = $0.675 \sigma$	
$Q.D. = 0.675 \times 4$	
Q.D. = 2.70	
Therefore, quartile deviation is 2.70.	
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Question7 If the parameter of poison distribution is m and (mean + S.D.= 25 6 ther	ı find m.		
(a) $\frac{3}{25}$ (b) $\frac{1}{25}$			
(c) $\frac{\frac{24}{25}}{25}$ (d) $\frac{\frac{3}{5}}{5}$			
Answer: b			
Explanation:			
Let, Mean of the Poisson distribute =µ For a Poisson distribution,			
Standard Deviation (SD)= $\sqrt{mean}$			
$\Rightarrow SD = \sqrt{\mu}$ Mean+SD = $\frac{6}{25}$ (Given)			
$Mean+SD=\frac{6}{25}$ (Given)			
$\mu + \sqrt{\mu} = \frac{6}{25}$ $\Rightarrow \sqrt{\mu} = \frac{6}{25} - \mu$			
On squaring both sides, $(- \sum_{n=1}^{\infty} (e^{-n})^{2})^{2}$			
$(\sqrt{\mu})^2 (\frac{1}{25} - \mu)$			
$(\sqrt{\mu})^{2} \left(\frac{6}{25} - \mu\right)^{2}$ $\mu = \mu^{2} - \frac{12}{25}\mu + \frac{36}{625}$ $\Rightarrow 0 = \mu^{2} - \frac{37}{25}\mu + \frac{36}{625}$			
$\Rightarrow 0 = \mu^2 - \frac{37}{25}\mu + \frac{36}{625}$			
$\Rightarrow 0 = \left(\mu - \frac{1}{25}\right) \left(\mu - \frac{36}{25}\right)$ $\Rightarrow \mu = \frac{1}{25}, \frac{36}{25}$			
$\Rightarrow \mu = \frac{1}{25}, \frac{36}{25}$			
Maximum likelihood estimate of a sample from Poisson Distribution is the sa	mple mean		
which is equal to parameter of Poisson's Distribution. $\Rightarrow \mu = m = \frac{1}{25}$			
$\therefore$ The correct option is B $\frac{1}{25}$			
<sup>25</sup>			
<u>JAN 2021</u>			
Question1			
If X is a poisson variable, and P (X = 1 = P(X = 2), then P(X = 4) is (a) $\frac{2}{3}a^{2}$			
(a) $\frac{2}{3}e^2$ (b) $\frac{2}{3}e^4$ (c) $\frac{3}{2}e^2$ (d) $\frac{3}{2}e^4$			
(c) $\frac{1}{2}e^{2}$ (d) $\frac{1}{2}e^{4}$ Answer: a			
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Explanation:
$P(x;\mu) = \frac{e^{-u}\mu^x}{x!}$
P(X = 1) = P(X = 2)
$e^{-u}\mu^1 = e^{-u}\mu^2$
-1! = -2!
$\mu = 2$
$P(X = 4) = \frac{e^{-u}\mu^{x}}{4!} = \frac{2}{3}e^{2}$

### **Question2**

### Which one of the following is an uniparametric distribution?

(a) Poisson(c) Binomial

(b) Normal(d) Hyper geometric

### Answer: a

**Explanation**:

Poisson distribution is uniparametric distribution. The parameter is m which is mean=np. Bcz it has  $\lambda$  as a parameter.

### Question3

#### For a normal distribution, the value of third moment about mean is

(a) 0	(b) 1
(c) 2	(d) 3

### Answer: a

#### **Explanation**:

 $E[(X-\mu)3]=0$  since  $X-\mu$  is normally distributed with mean zero, then expand out the cube. If the distribution of a random variable X is symmetric about 0, meaning Pr(X>x)=Pr(X<-x) for every x>0, then its third moment, if it exists at all, must be 0, as must all of its odd-numbered moments.

### JULY 2021

<b>Question</b> 2	<u>1</u>							
	The value of K for the probability density function of a variate X is equal to							
X	0	1	2	3	4	5	6	
<b>P (X)</b>	5K	3К	4K	6K	7K	9K	11K	
(a) 39 (b) 1/40								
(a) 39 (c) 1/49 (b) 1/40 (d) 1/45								
Answer: Options (c)								
Explanation								
Note: - Sum of all probabilities = 1								
Therefore, $5k + 3k + 4k + 6k + 7k + 9k + 11k = 1$								
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∴k=149

### Question 2

If is a Position variate such that I (x = 1) = 0.7, P (x = 2) = 0.3, then P (x = 0) =(a)  $e^{6/7}$ (b)  $e^{-6/7}$ (c)  $e^{-2/3}$ (d)  $e^{-1/3}$ Answer: Options (b)

### **Question 3**

If X is a binomial variate with p = 1/3 for, the experiment of 90 trials, then the standard deviation is equal to

(a) $-\sqrt{5}$	(b) √5
(c) $2\sqrt{5}$	(d) $\sqrt{15}$
Answer: Options (c)	

### Question 4

For a certain type of mobiles, the length of time between charges of the battery is normally distributed with a mean of 50 hours and a standard deviation of 15 hours. A person owns one of these mobiles and want to know the probability the Length of time will be between 50 and 70 hours is (Given  $\Phi$  (1.33) = 0.9082,  $\Phi$  (0) = 0.5)

0.5)	
(a) -0.4082	(b) 0.5
(c) 0.4082l	(d) -0.5
Answer: Options (c)	
Explanation:	
Given,	
μ=50 (mean)	
$\sigma$ =15 (standard/deviation)	
find the probability for 50 <x<70< td=""><td></td></x<70<>	
Converting the problem in standard form	
$Z = \frac{(x - \mu)}{2}$	
for x=50,	
Z=0	
For x=70,	
Z = (70-50)/15 = 1.33	
For finding the probability for 50 <x<70< td=""><td></td></x<70<>	
In the standard form $0 < z < 1.33$	
using Z-table, the area is equal to 0.4082	

### **DEC 2021**

FOR ENQUIRY – 6262969604	6262969699
Question 1 The average number of adverticements	nor nago annoaring in a nourchanor is 2
The average number of advertisements What is the probability that in a particul	
(a) e <sup>-3</sup>	(b) e <sup>-1</sup>
(c) e <sup>3</sup>	(d) $e^0$
Answer: a	
Explanation:	
Given m = 3; x = 0 $e^{-m_m x}$	
As per Poisson Distribution, $P(x) = \frac{e^{-m}m^x}{x!}$	
$P(x=0) = \frac{e^{-3}m^0}{0!} = e^{-3}$	
Question 2	
	eously. The expected number of heads is:
(a) 1 (c) 3	(b) 2 (d) 4
Answer: b	(u) 4
Explanation:	
Since four coins are being tossed, we have r	n = 4.
Probability of getting a "heads" in each trial	$(p) = \frac{1}{2}$
Expected number of Heads = $np = 4 \times \frac{1}{2} = 2$	) ••
Question 3	
	ble X, the probability for X taking value 2
is 3 times the probability for X taking val	
(a) 4	(b) 3
(c) 2	(d) 5
Answer: c	
<b>Explanation:</b> $e^{-m_m x}$	
Poisson Distribution, $P(x) = \frac{e^{-m}m^x}{x!}$	
P(x = 2) = 3P(x = 4)	
$\frac{e^{-m}m^2}{2!} = 3 \times \frac{e^{-m}m^4}{4!}$ $\frac{1}{2} = \frac{3m^2}{24}$	
2! 4!	
$\frac{1}{2} = \frac{5m}{24}$	
$2 \qquad 24 \\ 6m^2$	
$\frac{1}{24} = 1$	
$m^2 - 24 - 4$	
$\frac{2}{6m^2} = 1$ $m^2 = \frac{24}{6} = 4$ $m = \sqrt{4} = 2$	
$m = \sqrt{4} = 2$	

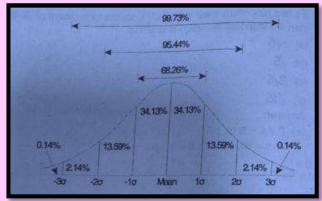
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### Question 4

Let X be normal distribution with mean 2.5 and variance 1. If P[a < X < 2.5] = 0.4772 and that the cumulative normal probability value at 2 is 0.9772, then a =? (a) 0.5 (b) 3 (c) -3.5 (d) -4.5 Answer: a Explanation: We know that for a standard normal deviate,  $z = \frac{x-\mu}{\sigma}$ 

Therefore, for × = 2.5,  $z = \frac{2.5 - 2.5}{1} = 0$ 

Therefore, we need the area of 0.4772 from the mean till a certain point on the left-hand side.



From the graph above, we can see that the area from mean till -2  $\sigma$  is 47.72%, i.e., 0.4772.

Thus, the corresponding z for the value of x = a should be -2.

Therefore,  $-2 = \frac{a-2.5}{1}$ = -2 = a - 2.5= 2.5 - 2 = a= a = 0.5

### Question 5

he manufacturer of a certain electronic component is certain that 2% of his product is defective. He sells the components in boxes of 120 and guarantees that not more than 2% in any box will be defective. Find the probability that a box, selected at random would fail to meet the guarantee? (Given that e<sup>-2.4</sup> = 0.0907)

(a) 0.49	(b) 0.39
(c) 0.37	(d) 0.43
Answer: d	
Explanation:	
Here, n = 120; p =2/ 100 = 0.02	
$m = np = 120 \times 0.02 = 2.40$	

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As per Poisson Distribution,  $P(x) = \frac{e^{-m}m^x}{x!}$ 

A box, selected at random would fail to meet the guarantee if more than 2.40 components turn out to be defective.

 $P(\times > 2.40) = 1 P(\times \le 2.40)$   $P(\times > 2.40) = 1 - [P(x = 0) + P(x = 1) + P(\times = 2)]$   $P(\times > 2.40) = 1 - \left[\frac{e^{-240}.(2.40)^2}{0!} + \frac{e^{-240}.(2.40)^2}{1!} + \frac{e^{-240}.(2.40)^2}{2!}\right]$   $P(\times > 2.40) = 1 - \left[\frac{0.0907 \times 1}{1} + \frac{0.0907 \times 2.40}{1} + \frac{0.097^{-240}.(2.40)^2}{2}\right]$   $P(\times > 2.40) = 0.43$ 

### Question 6

A renowned hospital usually admits 200 patients everyday. One percent patients, on an average, require special room facilities. On one particular morning, it was found that only one special room is available. What is the probability that more than 3 patients would require special room facilities?

than 5 patients would require special room facilities:
(a) 0.1428 (b) 0.1732
(c) 0.2235 (d) 0.3450
Answer: a
Explanation:
Here n = 200; p =1/100
Therefore, $m = np = 200 \times 1/100 = 2$
As per Poisson Distribution, $P(x) = \frac{e^{-m}m^x}{x!}$
$P(x > 3) = 1 - P(x \le 3)$
P(x > 3) = 1 - [P(x = 0) + P(x = 1) + P(* = 2) + P(x = 3)]
$P(x > 3) = 1 - \frac{e^{-2} \times 2^{0}}{0!} + \frac{e^{-2} \times 2^{1}}{1!} + \frac{e^{-2} \times 2^{2}}{2!} + \frac{e^{-2} \times 2^{3}}{3!}$
$P(x > 3) = 1 - \frac{271828^{-2} \times 2^{0}}{0!} + \frac{271828^{-2} \times 2^{1}}{1!} + \frac{271828^{-2} \times 2^{2}}{2!} + \frac{271828^{-2} \times 2^{2}}{3!}$
$P(x > 3) = 1 - \frac{1}{271828^2} + \frac{2}{271828^2} + \frac{4}{2 \times 271828^2} + \frac{4}{3 \times 271828^2}$
$P(x > 3) = 1 - \left[\frac{1}{(2.71828)^2} \left\{1 + 2 + \frac{4}{2} + \frac{8}{6}\right\}\right]$
P(x > 3) = 1 - [0.8571] = 0.1428

### **JUNE 2022**

Question 1If Standard Deviation is 1.732 then what is the value of poisson distribution. The P[- 2.48 < × < 3.54] is</td>(a) 0.73(b) 0.65

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### (c) 0.86

(d) 0.81

3)

Answer: b
Explanation:
Given S.D = 1.732
S.D. = $\sqrt{3}$
In Poison distribution
S.D. = $\sqrt{m}$
$\sqrt{3} = \sqrt{m}$
m = 3
= P(x = 0) + P(x = 1) + P(x = 2) + P.(x = 1)
$\left[\frac{e^{-3} \cdot 3^{0}}{0!} + \frac{e^{-3} \cdot 3^{1}}{1!} + \frac{e^{-3} \cdot 3^{2}}{2!} + \frac{e^{-3} \cdot 3^{3}}{3!}\right]$
0! + 1! + 2! + 3!
$e^{-3}\left[\frac{1}{0!} + \frac{3}{1!} + \frac{9}{2!} + \frac{27}{3!}\right]$
$e^{-3}\left[1+3+\frac{9}{2}+\frac{27}{6}\right]$
$e \left[ 1 + 3 + \frac{1}{2} + \frac{1}{6} \right]$
$\frac{1}{e^3}  1+3+4.5+4.5 $
$e^{3}$
$=\frac{1}{(2.72)^3} = \frac{13}{20.12} = 0.6461 = 0.65$
(2.72) 20.12

### Question 2

In a normal distribution, variance is 16 then the value of mean deviation is. (a) 4.2 (b) 3.2 (c) 4.5 (d) 2.5 Answer: b Explanation: Variance = 16 (In Normal Distribution) S.D =  $\sqrt{16} = 4$ M.D = 0.8 S.D = 0.8 x 4 = 3.2

### Question 3

For a binomial	distribution,	there may b	e
(a) One mode			(b) Multi

(c) Two mode

(b) Multi mode(d) No mode

### Answer:

**Explanation:** a For a binomial distribution, there may be multimode